

Statistical models on phylogenetic networks

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University of Wisconsin-Madison
Wisconsin Institute for Discovery
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May 30, 2023



<https://solislemuslab.github.io/>



mstdn.social/@solislemuslab

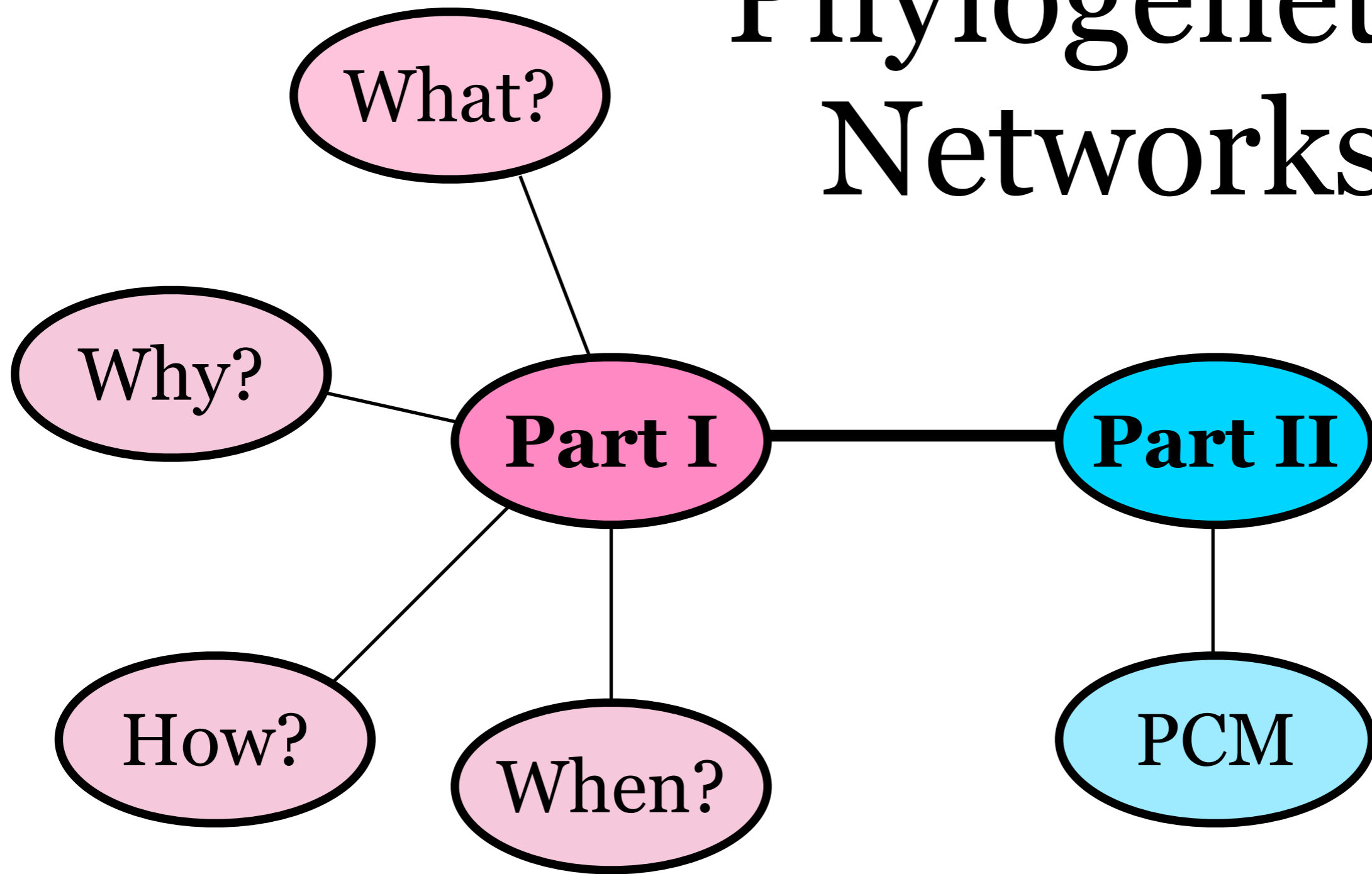


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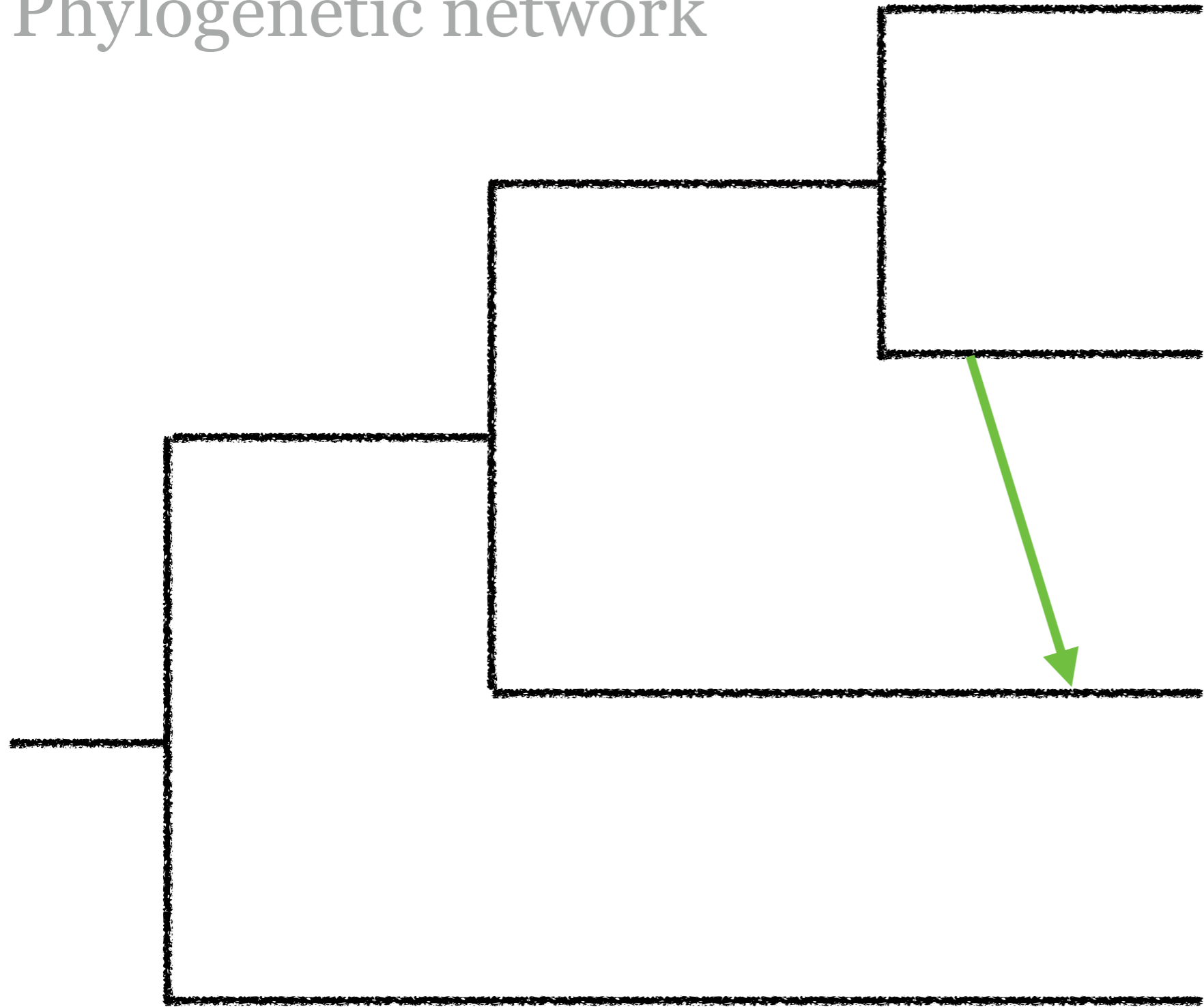
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Phylogenetic Networks



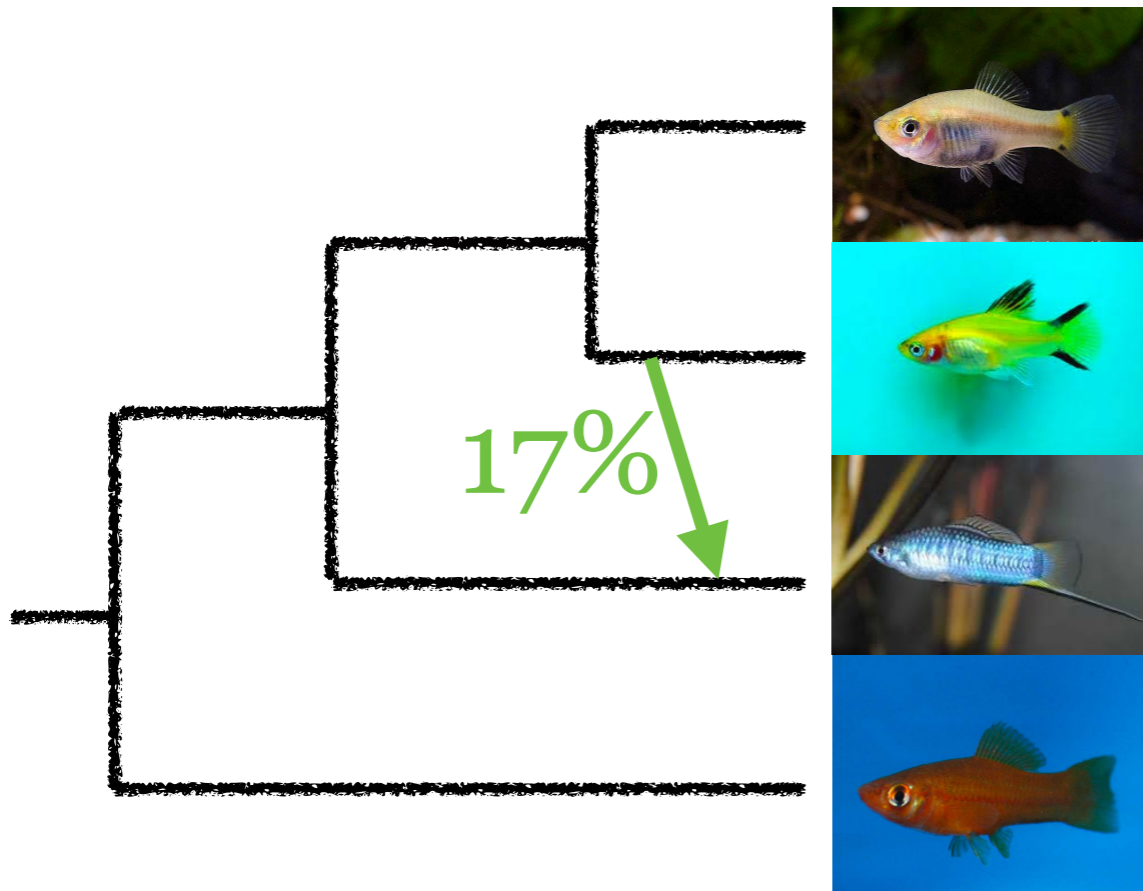
What?

Phylogenetic network

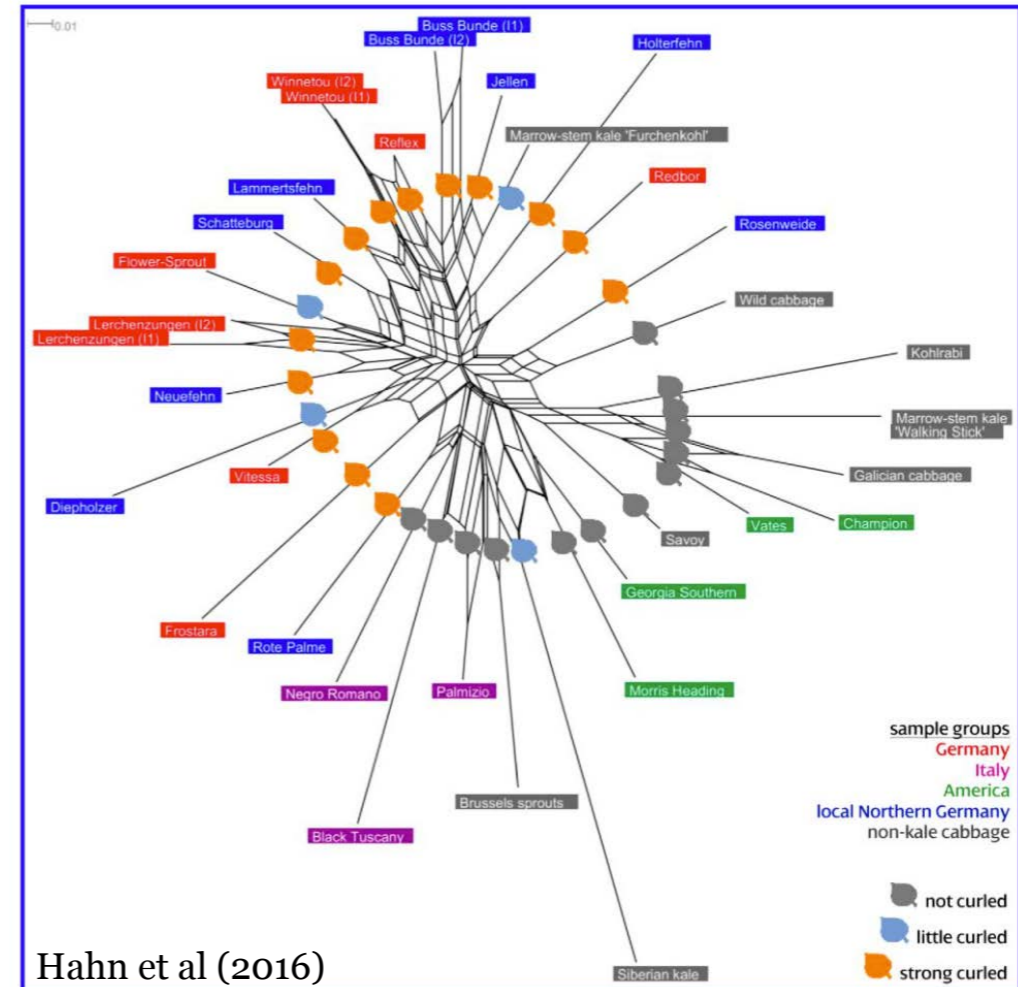


What?

Phylogenetic network



Explicit



Implicit

Why?

Phylogenetic network

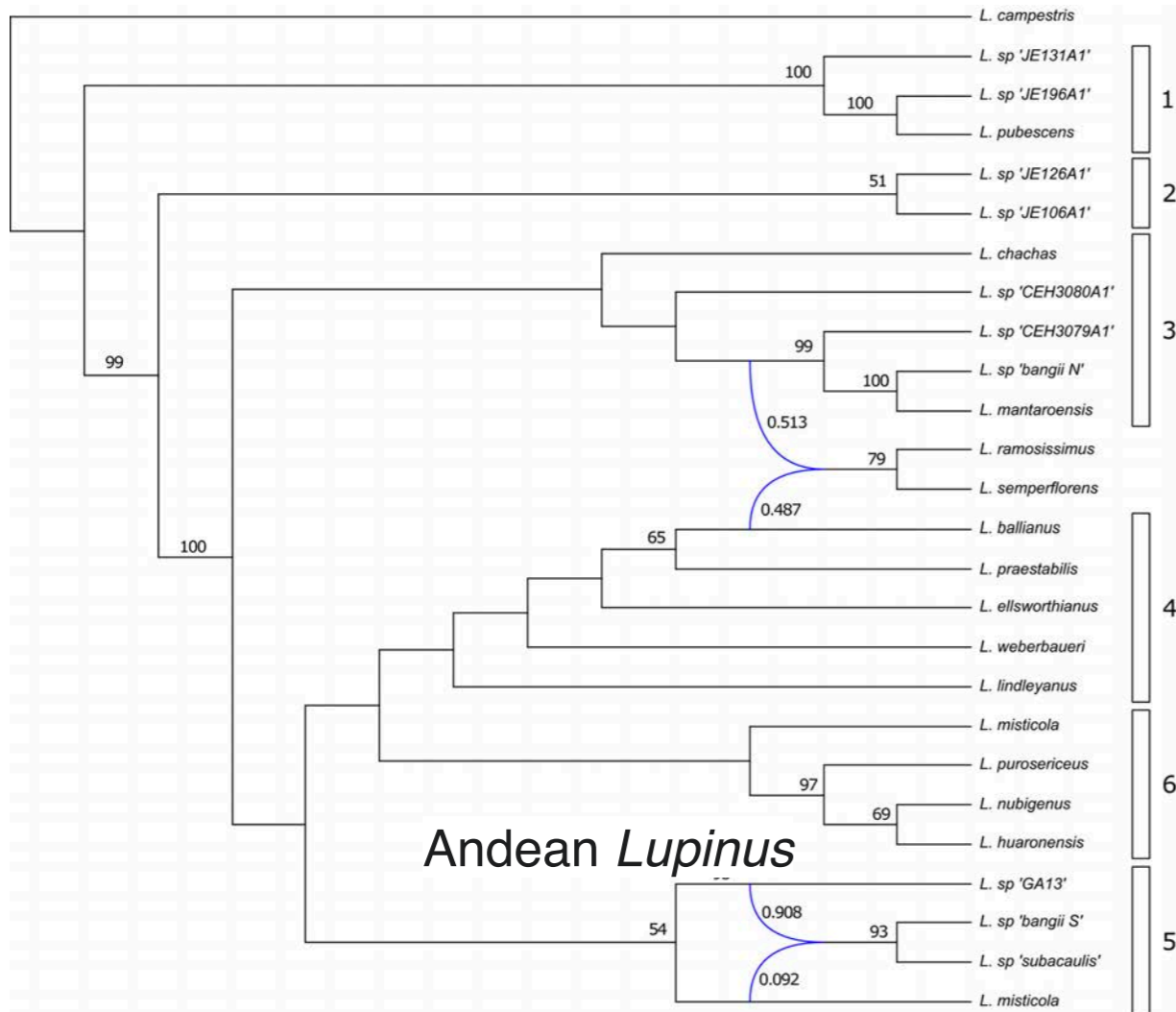


New Phytologist

Full Paper | [Free Access](#)

Pleistocene glacial cycles drive isolation, gene flow and speciation in the high-elevation Andes

Bruno Nevado , Natalia Contreras-Ortiz, Colin Hughes, Dmitry A. Filatov



Current Biology

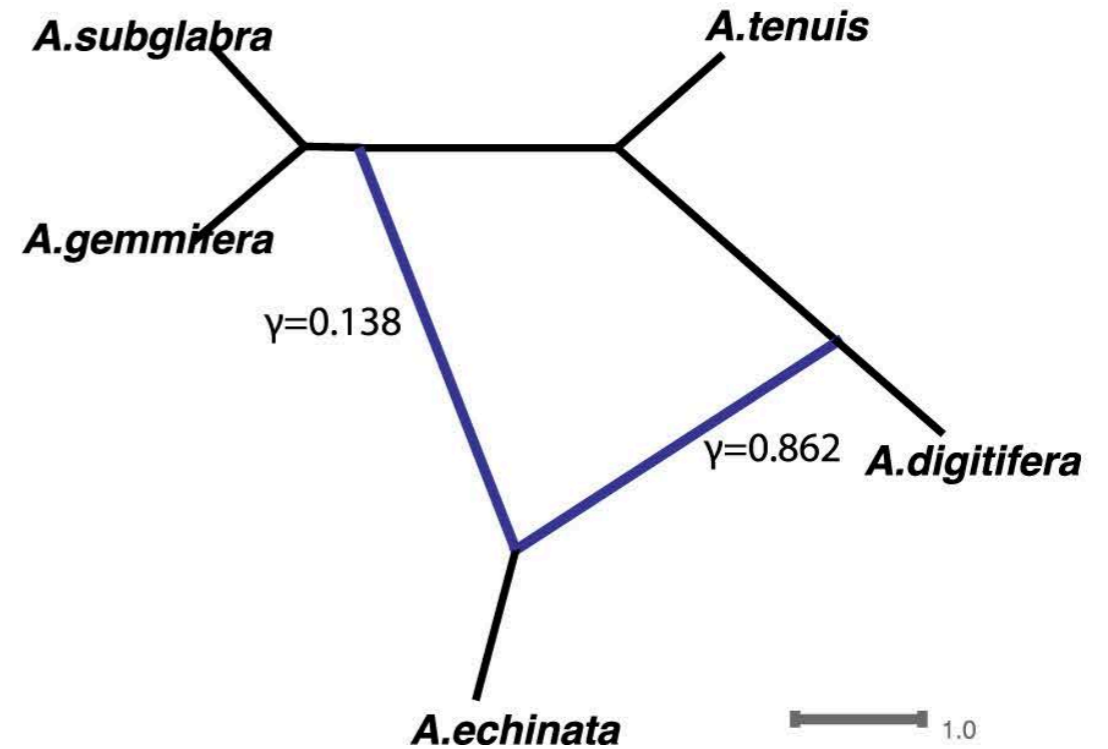
Volume 28, Issue 21, 5 November 2018, Pages 3373-3382.e5

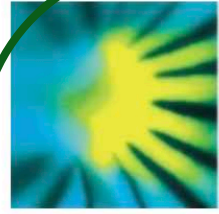


Article

The Roles of Introgression and Climate Change in the Rise to Dominance of *Acropora* Corals

Yafei Mao ^{1,2,3} , Evan P. Economo ² , Noriyuki Satoh ¹ 

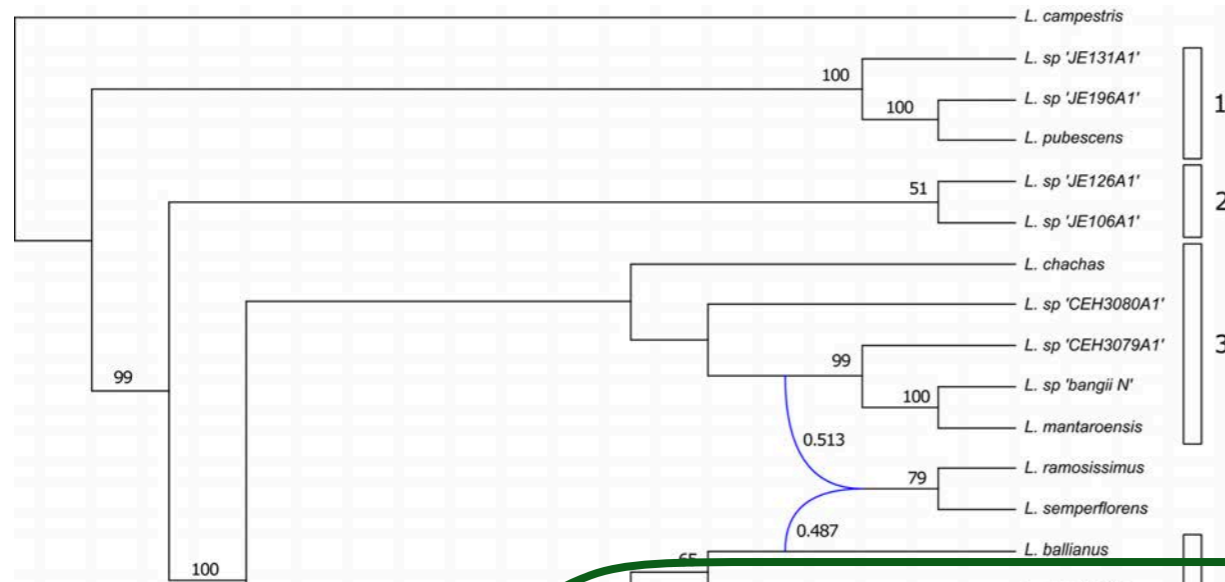




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Pleistocene glacial cycles drive isolation, gene flow and speciation in the high-elevation Andes

Bruno Nevado , Natalia Contreras-Ortiz, Colin Hughes, Dmitry A. Filatov



ORIGINAL ARTICLE | [Open Access](#) |

Embracing discordance: Phylogenomic analyses provide evidence for allopolyploidy leading to cryptic diversity in a Mediterranean *Campanula* (Campanulaceae) clade

Andrew A. Crowl , Cody Myers, Nico Cellinese

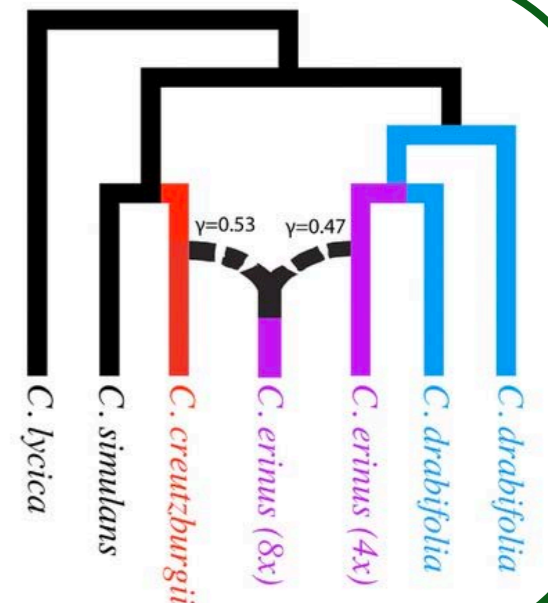
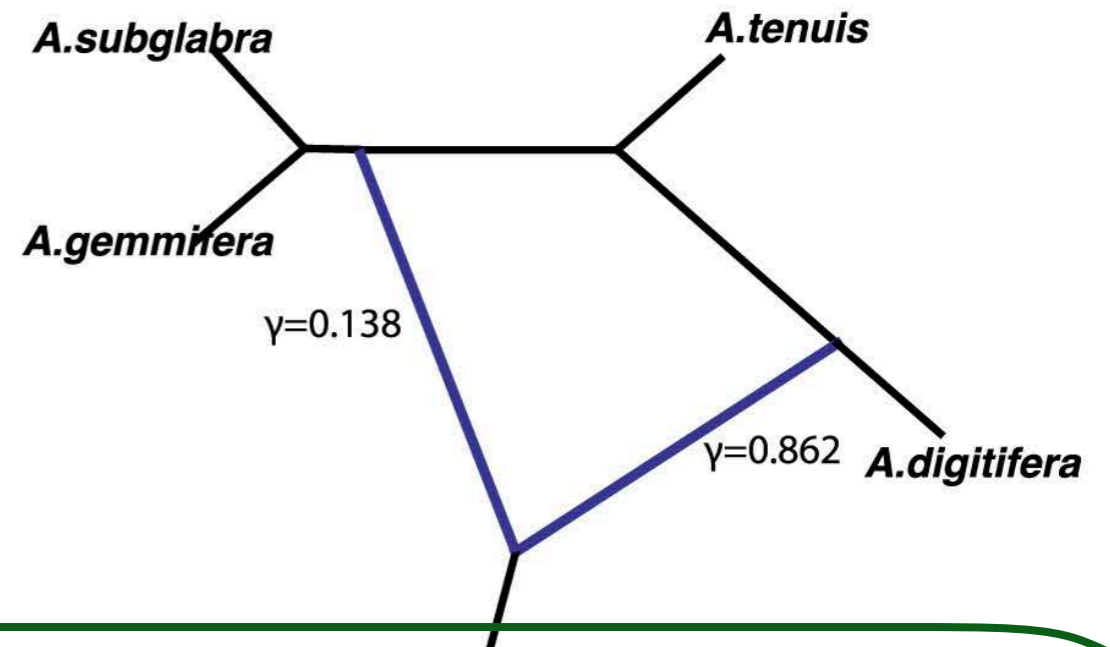
Volume 28, Issue 21, 5 November 2018, Pages 3373-3382.e5

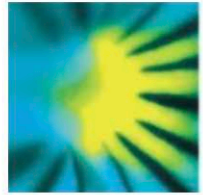


Article

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Yafei Mao ^{1, 2, 3} , Evan P. Economo ² , Noriyuki Satoh ¹



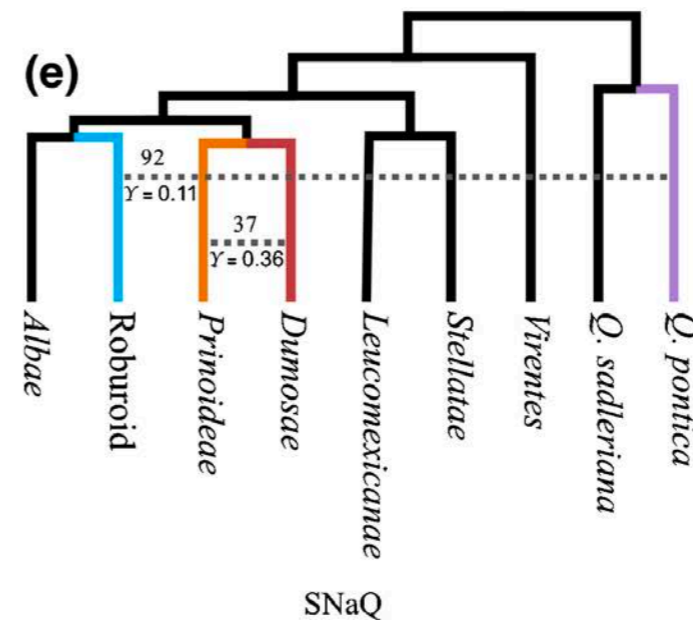


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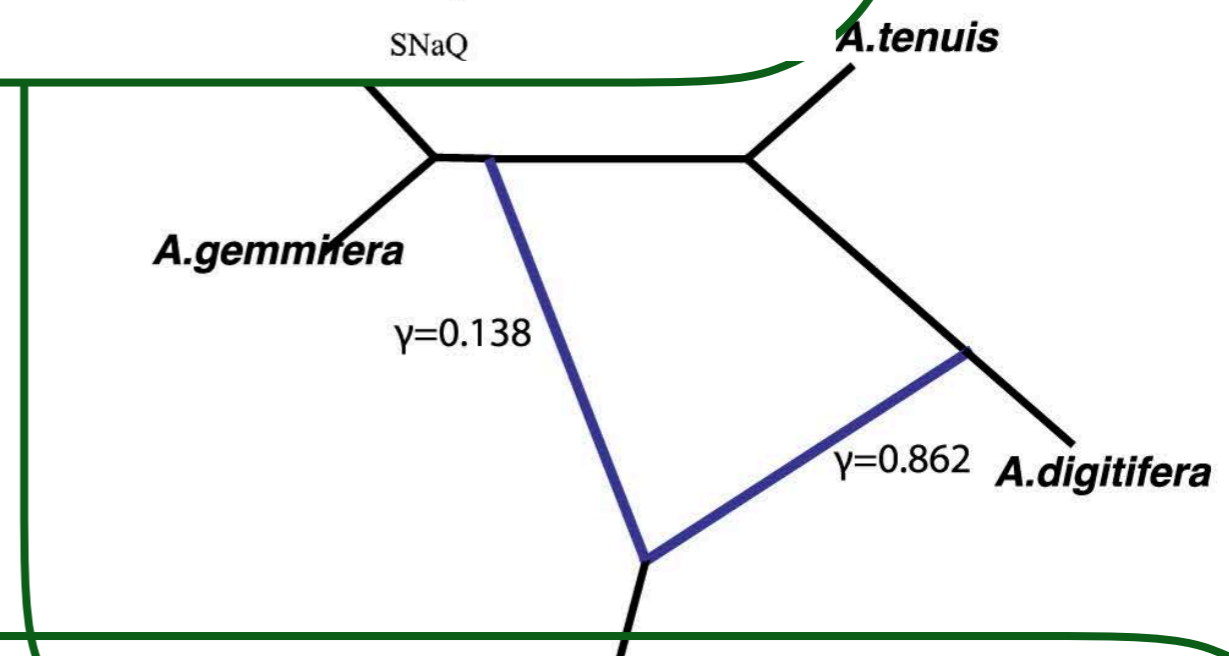
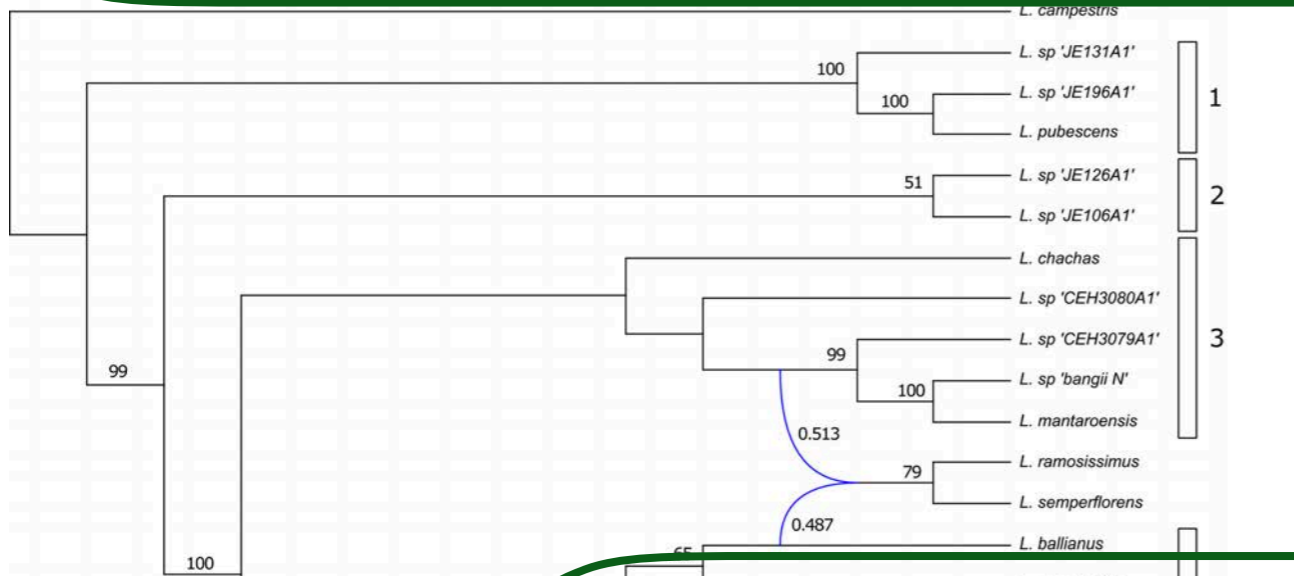
Uncovering the genomic signature of ancient introgression between white oak lineages (*Quercus*)

Andrew A. Crowl Paul S. Manos, John D. McVay, Alan R. Lemmon, Emily Moriarty Lemmon, Andrew L. Hipp ... [See fewer authors](#) ^

First published: 08 April 2019 | <https://doi.org/10.1111/nph.15842> | Citations: 32



Climate Change in Corals



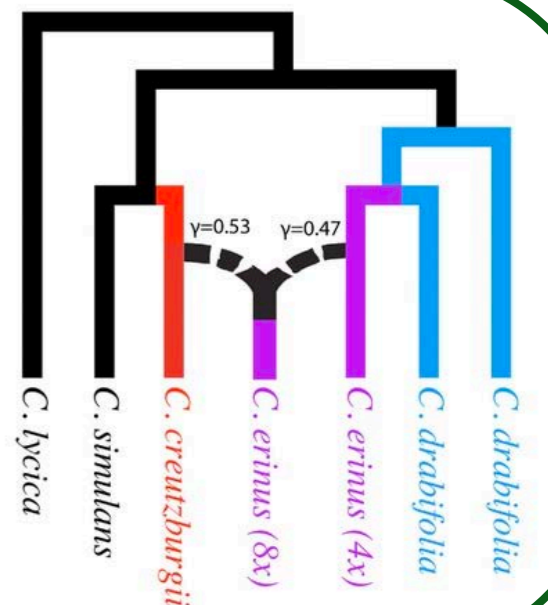
EVOLUTION

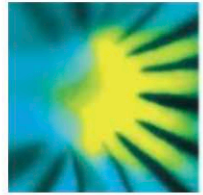
INTERNATIONAL JOURNAL OF ORGANIC EVOLUTION

ORIGINAL ARTICLE | [Open Access](#) |

Embracing discordance: Phylogenomic analyses provide evidence for allopolyploidy leading to cryptic diversity in a Mediterranean *Campanula* (Campanulaceae) clade

Andrew A. Crowl Cody Myers, Nico Cellinese





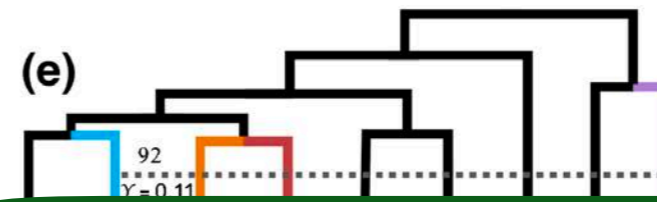
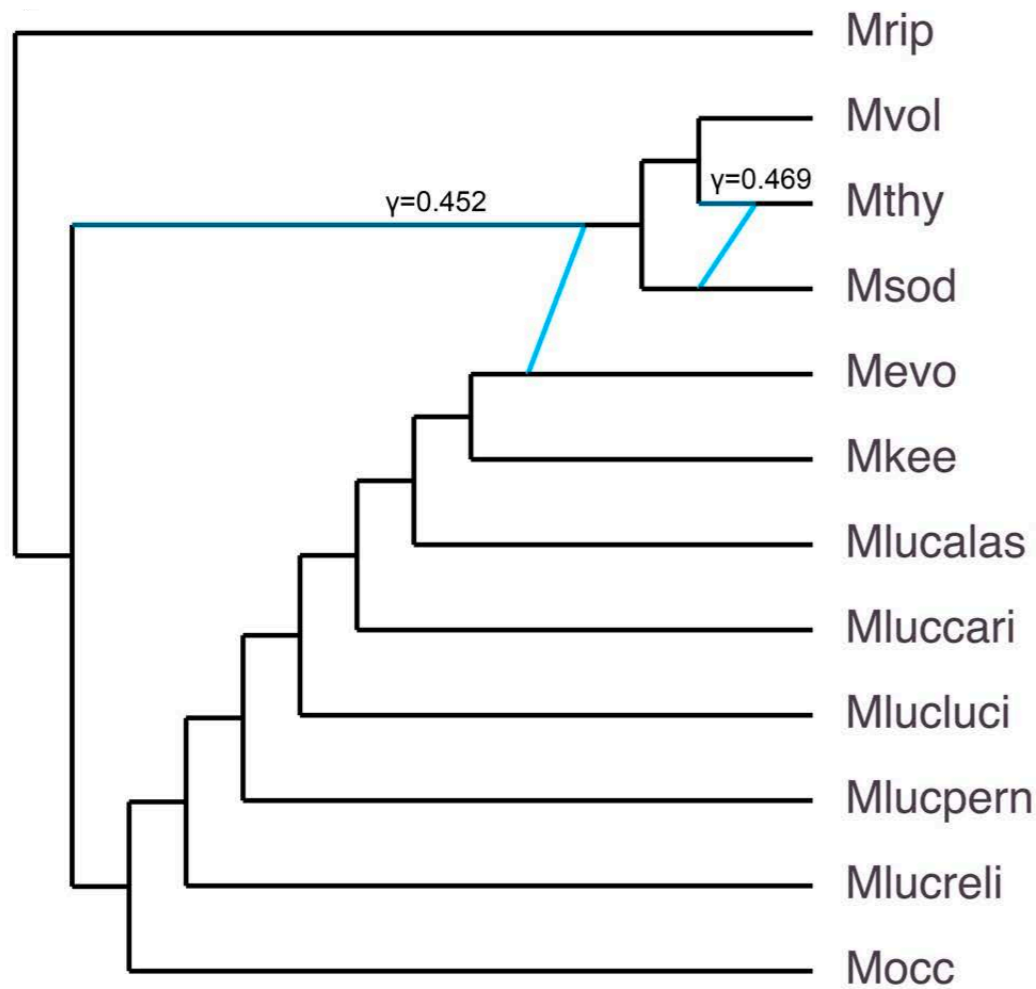
Evidence that *Myotis lucifugus* “Subspecies” are Five Nonsister Species, Despite Gene Flow FREE

Ariadna E Morales ✉, Bryan C Carstens

Systematic Biology, Volume 67, Issue 5, September 2018, Pages 756–769,

<https://doi.org/10.1093/sysbio/syy010>

Published: 15 February 2018 [Article history](#) ▼



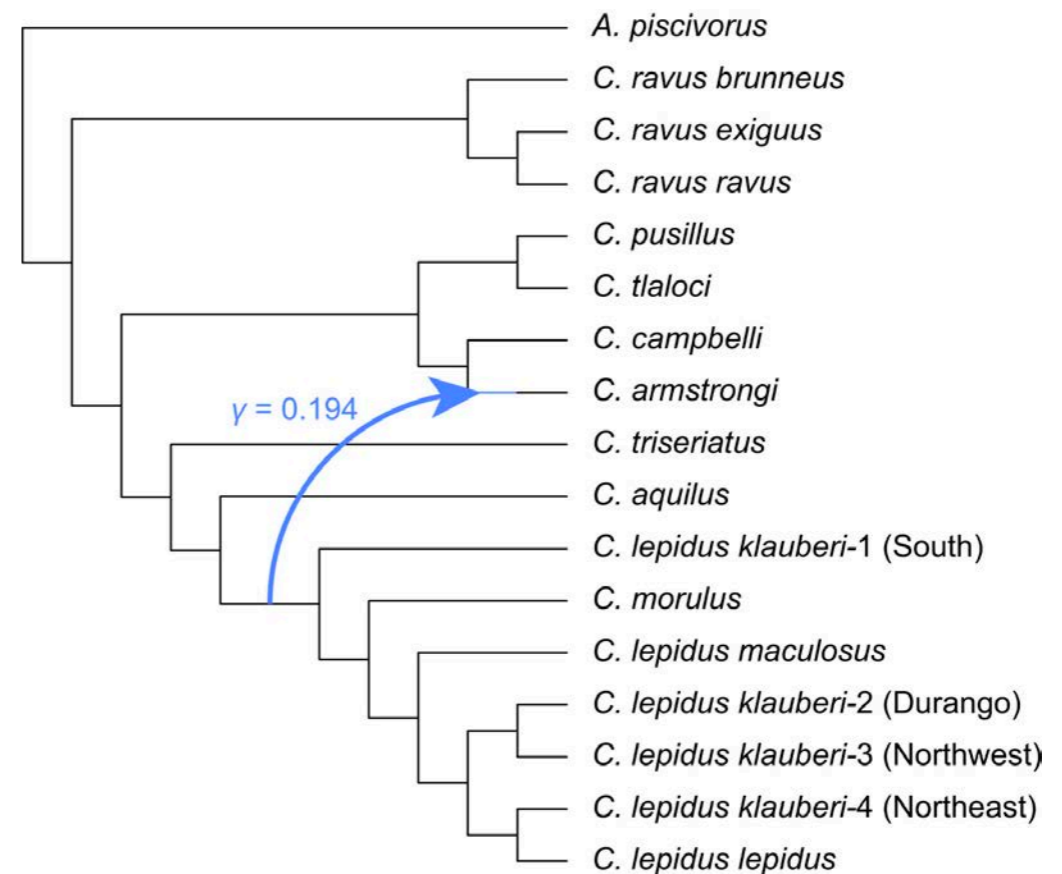
MOLECULAR ECOLOGY RESOURCES

RESOURCE ARTICLE | [Full Access](#)

Cryptic diversity in the Mexican highlands: Thousands of UCE loci help illuminate phylogenetic relationships, species limits and divergence times of montane rattlesnakes (Viperidae: *Crotalus*)

Christopher Blair ✉, Robert W. Bryson Jr, Charles W. Linkem, David Lazcano, John Klicka, John E. McCormack ... [See fewer authors](#) ^

First published: 22 November 2018 | <https://doi.org/10.1111/1755-0998.12970> | Citations: 20



Mediterranean *Campanula* (Campanulaceae)

Andrew A. Crowl ✉, Cody Myers, Nico Cellinese

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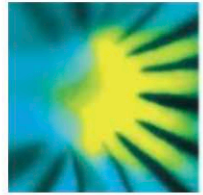
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Evidence that *Myotis lucifugus* “Subspecies” are Five Nonsister Species, Despite Gene Flow

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Phylogenomic Signatures of Ancient Introgression in a Rogue Lineage of Darters (Teleostei: Percidae)

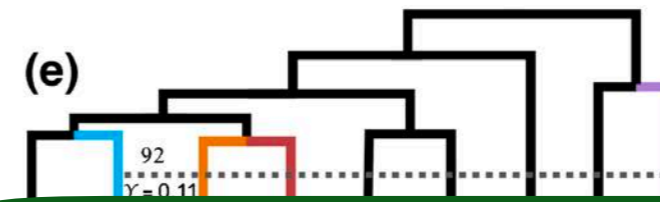
FREE

Daniel J MacGuigan, Thomas J Near

Systematic Biology, Volume 68, Issue 2, March 2019, Pages 329–346,

<https://doi.org/10.1093/sysbio/syy074>

Published: 03 December 2018 Article history

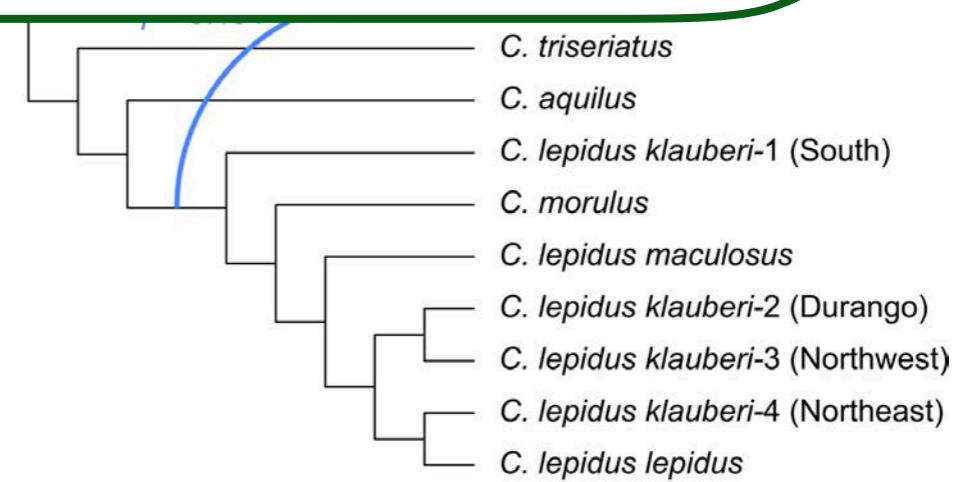
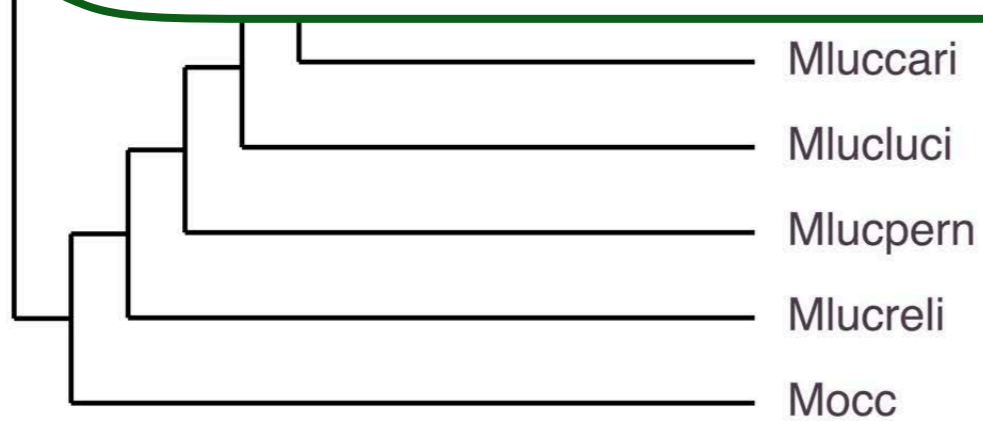
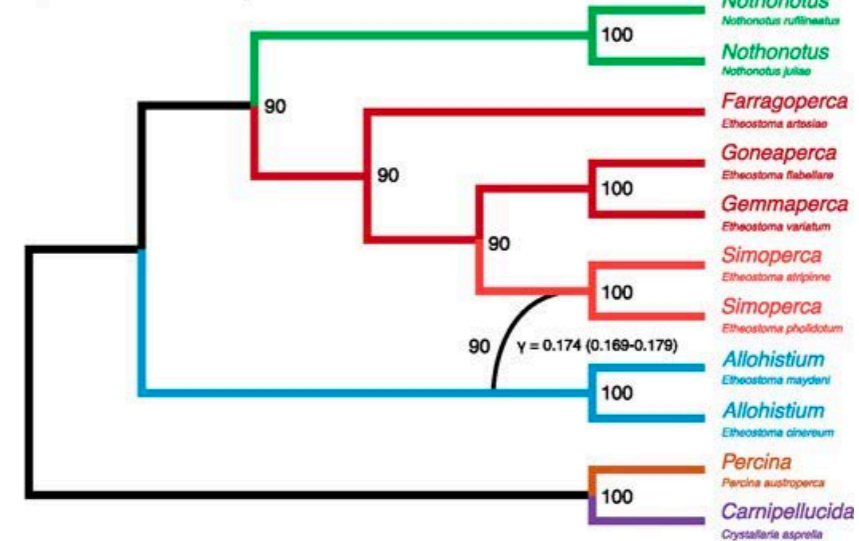


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Cryptic diversity in the Mexican highlands: Thousands of UCE loci

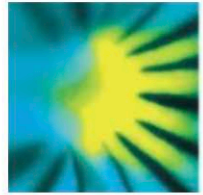
a) Maximum pseudolikelihood network



Mediterranean *Campanula* (Campanulaceae)

Andrew A. Crowl, Cody Myers, Nico Cellinese

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Full paper

Evidence that *Myotis lucifugus* “Subspecies” are Five Nonsister Species, Despite Gene Flow FREE

Ariadna E Morales ✉, Bryan C Carstens

Systematic Biology

<https://doi.org/10.1111/syb.13301>

Published online

Phylogenomic Signatures of Ancient Introgression in a Rogue Lineage of Darters (Teleostei: Percidae)

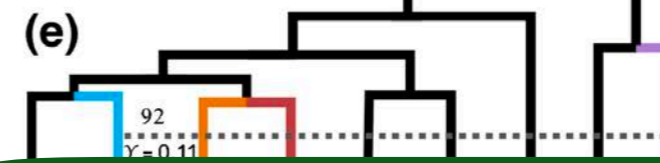
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Systematic Biology, Volume 68, Issue 2, March 2019, Pages 329–346,

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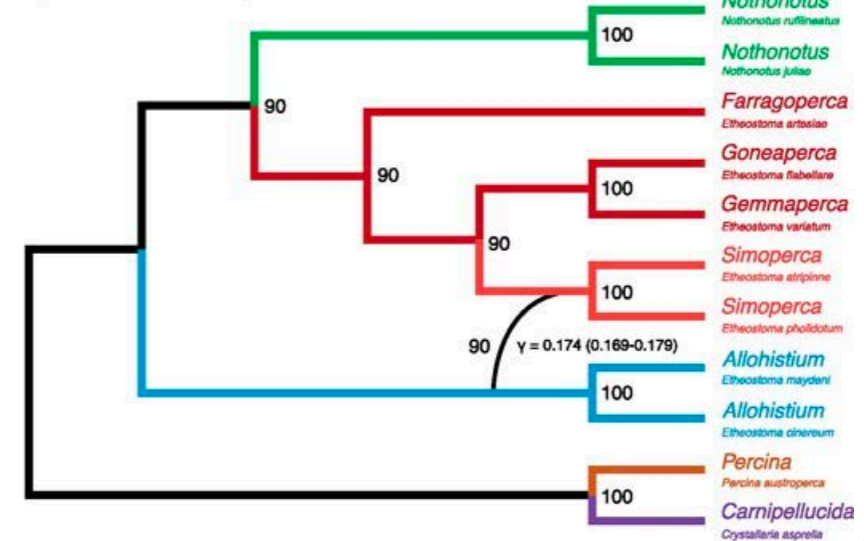


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Cryptic diversity in the Mexican highlands: Thousands of UCE loci

a) Maximum pseudolikelihood network



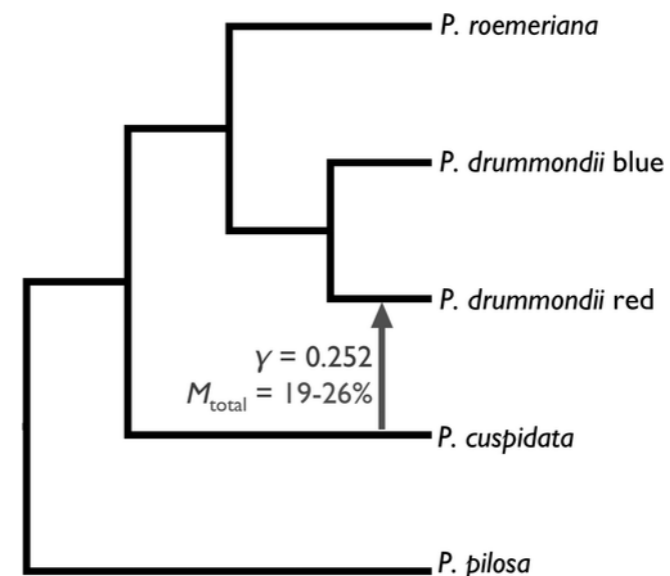
MOLECULAR ECOLOGY

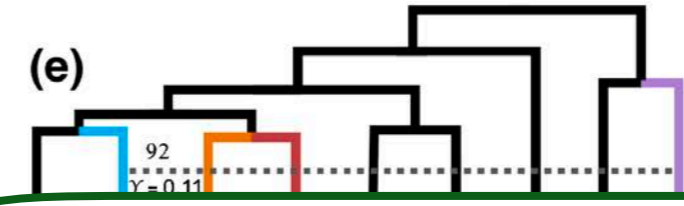
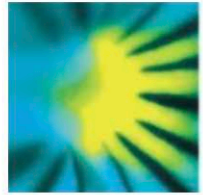
Original Article | [Full Access](#)

Genomic evidence of gene flow during reinforcement in Texas *Phlox*

Federico Roda ✉, Fábio K. Mendes, Matthew W. Hahn, Robin Hopkins

First published: 31 January 2017 | <https://doi.org/10.1111/mec.14041> | Citations: 15





MOLECULAR ECOLOGY RESOURCES

Evidence that *Myotis lucifugus* “Subspecies” are Nonsister Species, Despite Gene Flow

Ariadna E Morales, Bryan C Carstens

Systematic Biology

https://doi.org/10.1093/sysbio/syy073

Published: 03 December 2018

Phylogenomic Signatures of a Rogue Lineage of *Adansonia*

FREE

Daniel J MacGuigan, Thomas J Newbery

Systematic Biology, Volume 68, Issue 12

https://doi.org/10.1093/sysbio/syy073

Published: 03 December 2018

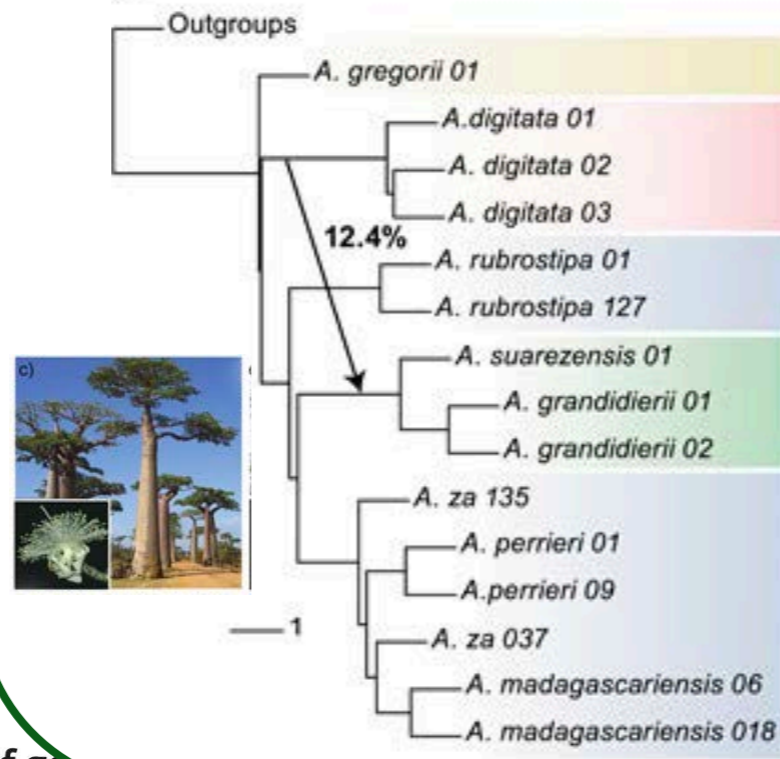
Reticulate Evolution Helps Explain Apparent Homoplasy in Floral Biology and Pollination in Baobabs (*Adansonia*; Bombacoideae; Malvaceae)

Nisa Karimi, Corrinne E Grover, Joseph P Gallagher, Jonathan F Wendel, Cécile Ané, David A Baum

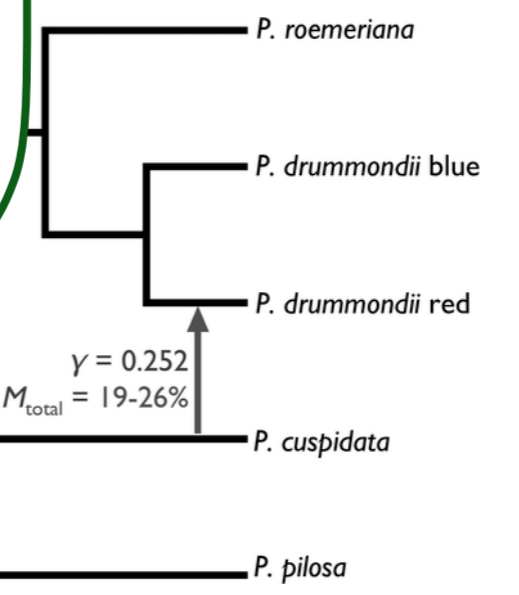
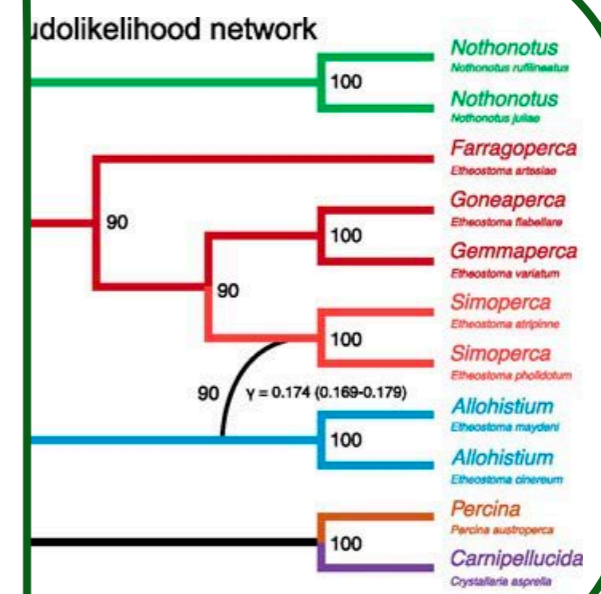
Systematic Biology, Volume 69, Issue 3, May 2020, Pages 462–478,

https://doi.org/10.1093/sysbio/syz073

Published: 06 November 2019 Article history



Mexican highlands: Thousands of UCE loci



MOLECULAR ECOLOGY

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Genomic evidence of gene flow in *Phlox*

Federico Roda, Fábio K. Mendes, Matthew W. Hahn, Robin Hopkins

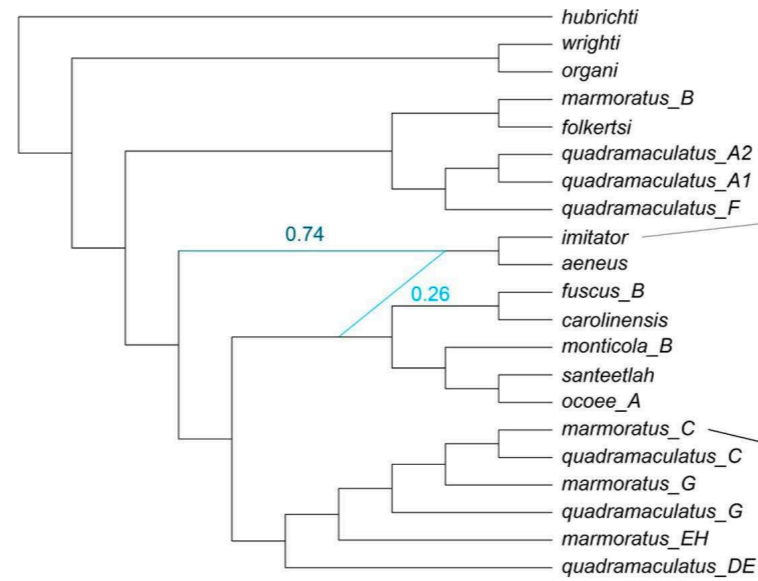
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Phylogenomic data reveal reticulation and incongruence among mitochondrial candidate species in Dusky Salamanders (*Desmognathus*)

R. Alexander Pyron ^{a, b, c}, Kyle A. O'Connell ^{a, b, c}, Emily Moriarty Lemmon ^d, Alan R. Lemmon ^e, David A. Beamer ^f

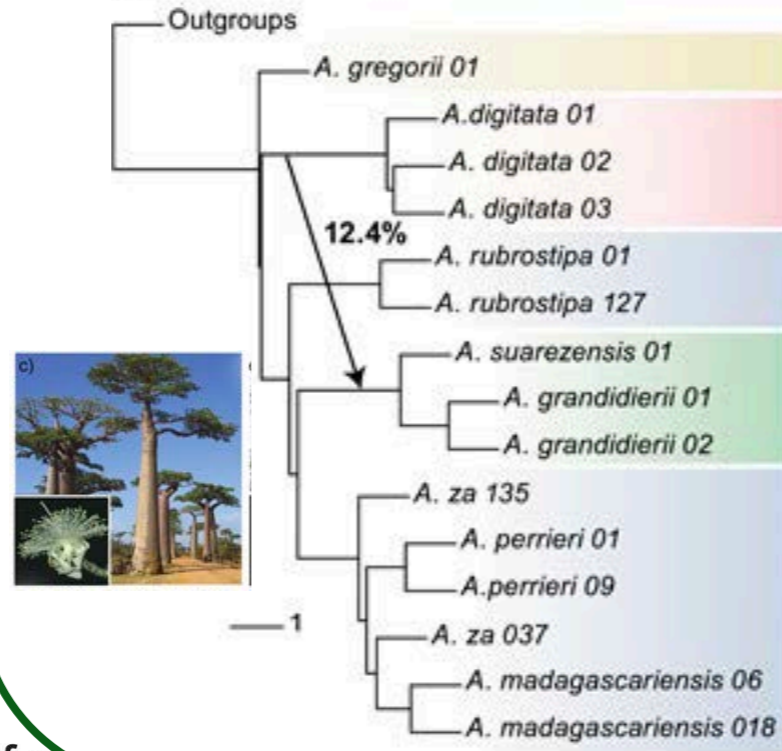


Daniel J MacGuigan [✉], Thomas J N

Systematic Biology, Volume 68, Issue

<https://doi.org/10.1093/sysbio/syy0>

Published: 03 December 2018



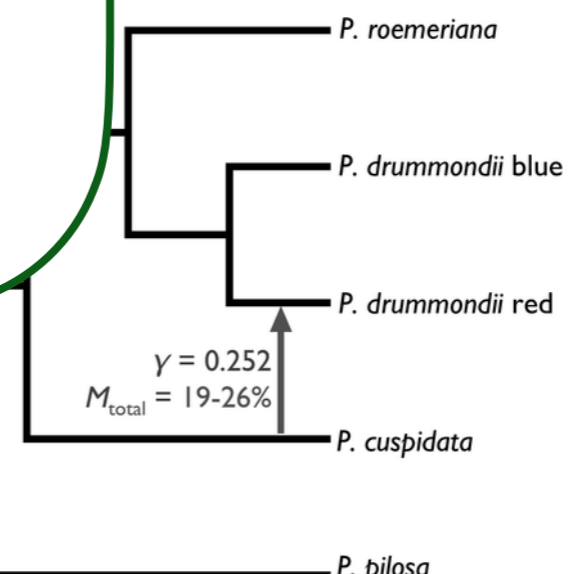
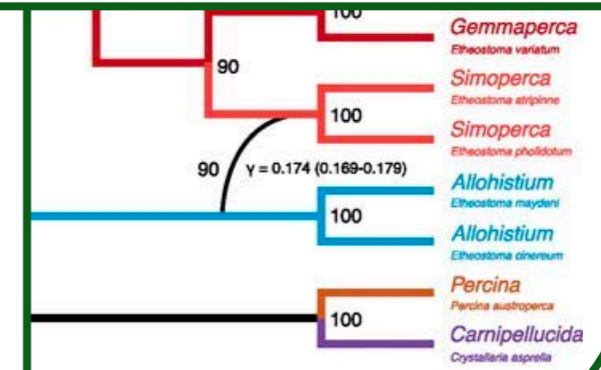
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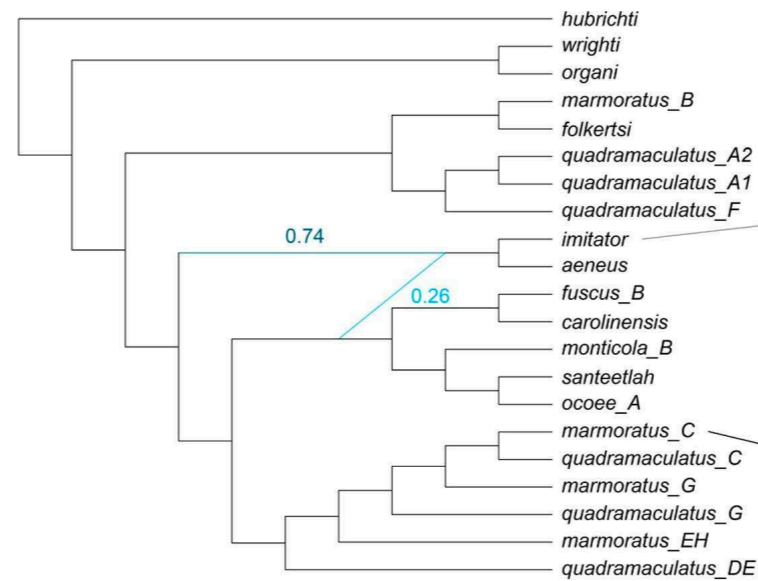


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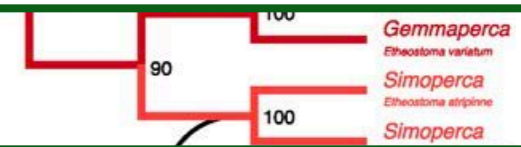
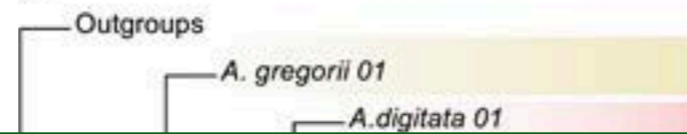
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Daniel J MacGuigan, Thomas J N

Systematic Biology, Volume 68, Issue



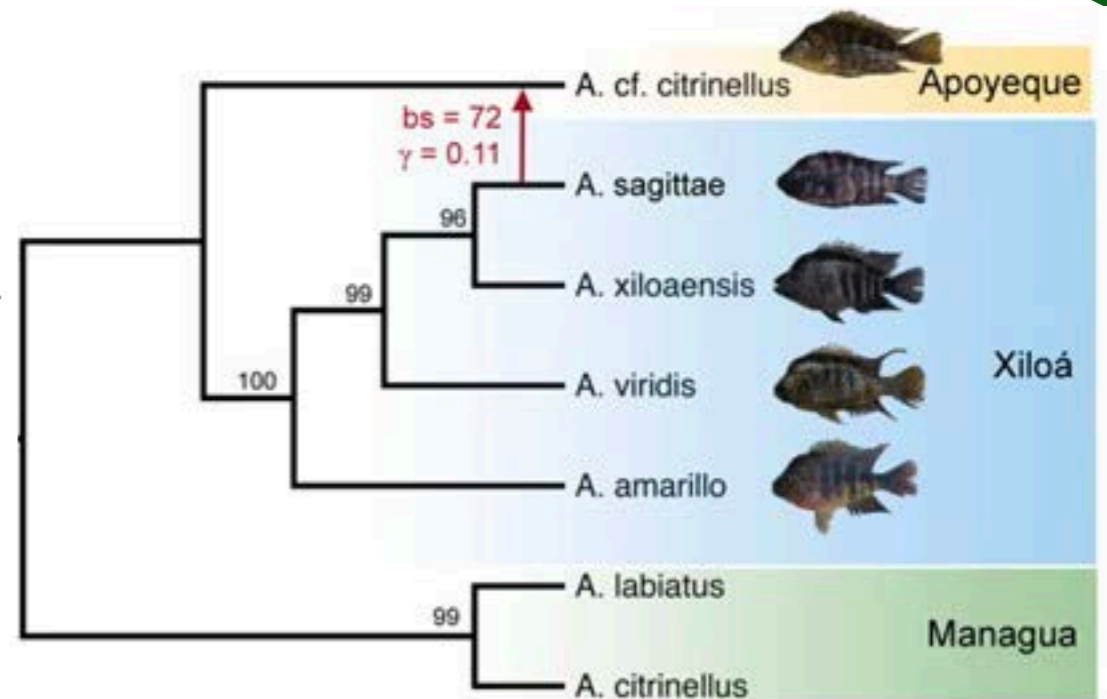
Implementing Large Genomic Single Nucleotide Polymorphism Data Sets in Phylogenetic Network Reconstructions: A Case Study of Particularly Rapid Radiations of Cichlid Fish

Melisa Olave, Axel Meyer

Systematic Biology, Volume 69, Issue 5, September 2020, Pages 848–862,

<https://doi.org/10.1093/sysbio/syaa005>

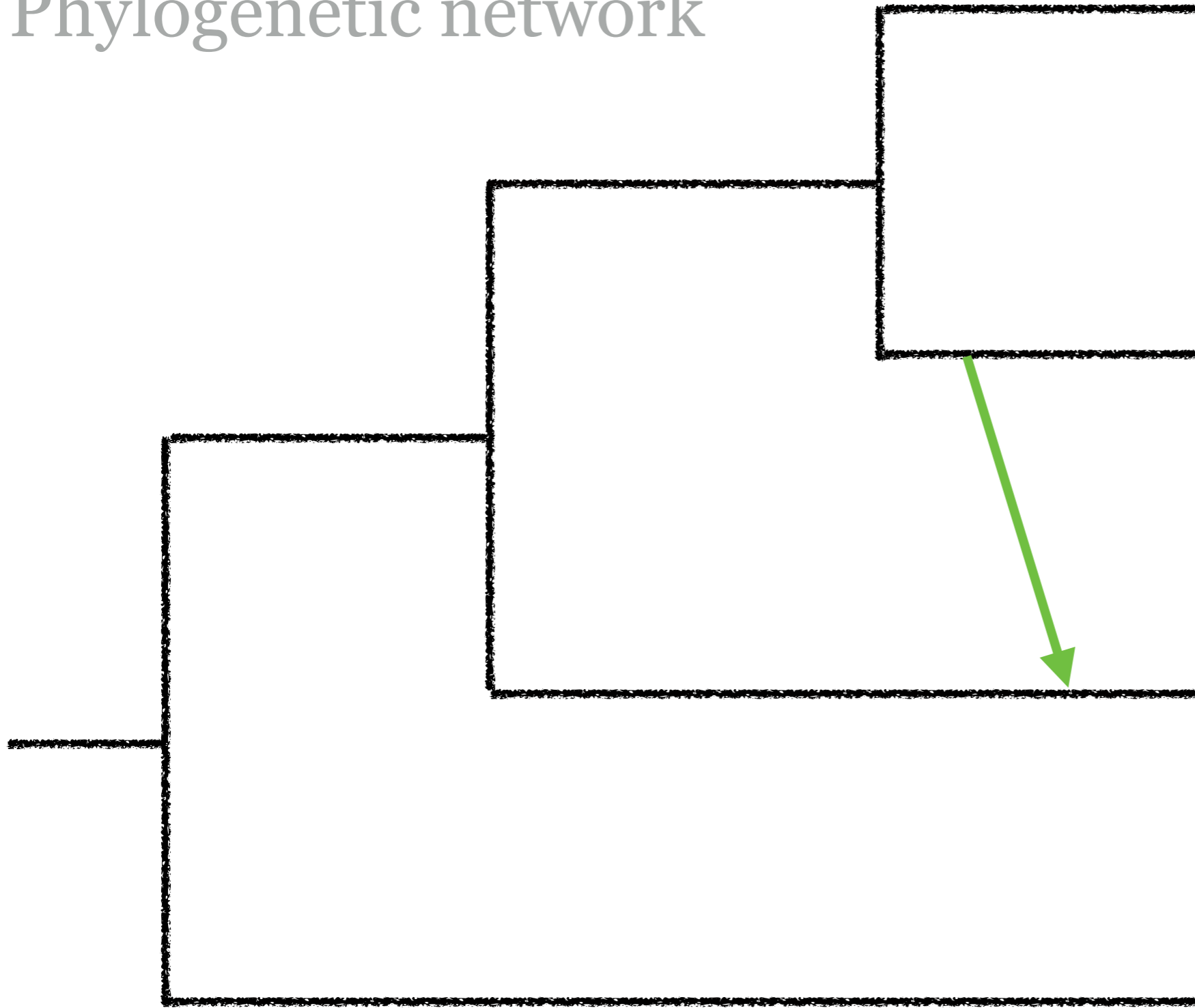
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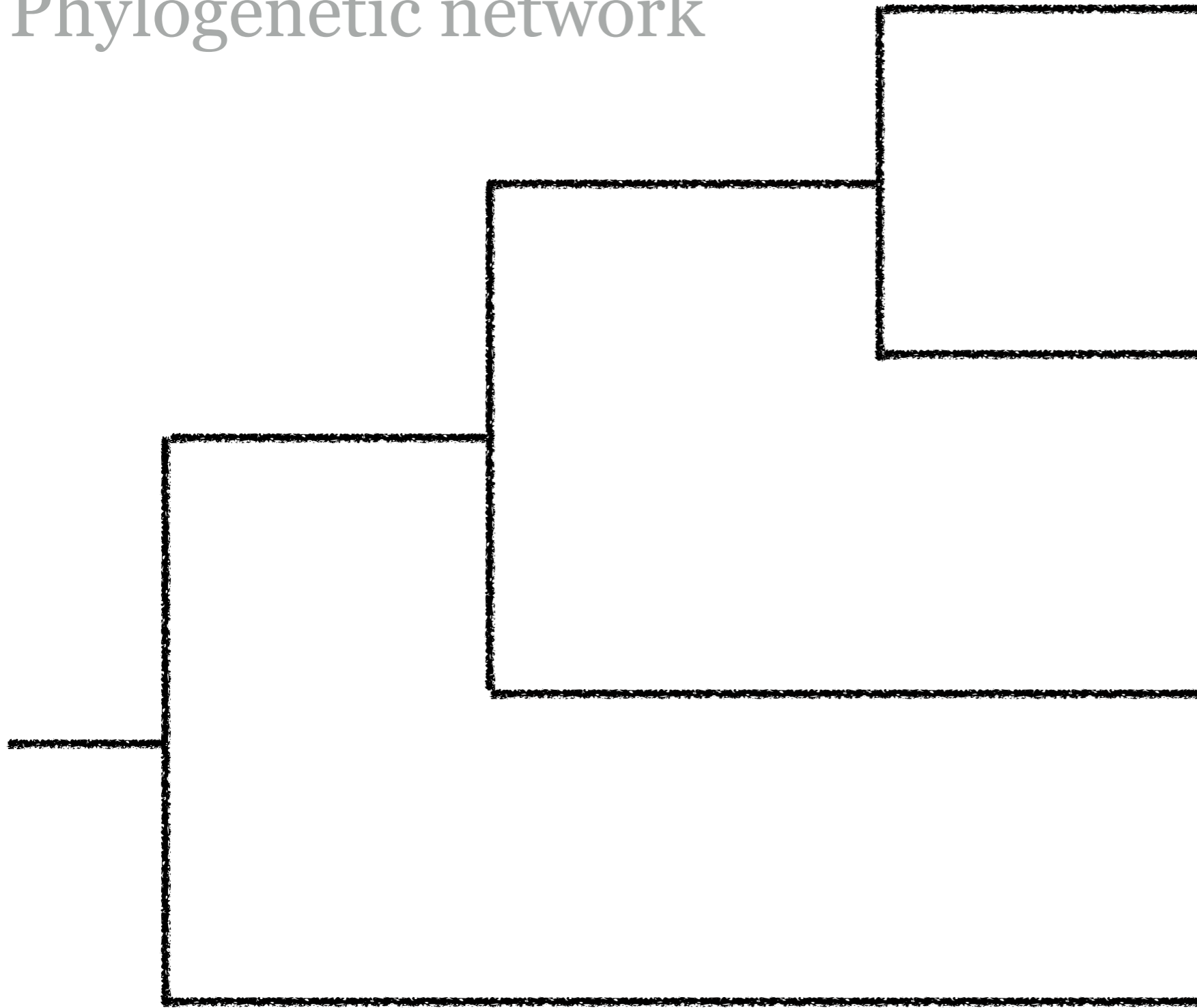
Why?

Phylogenetic network



Why?

Phylogenetic network



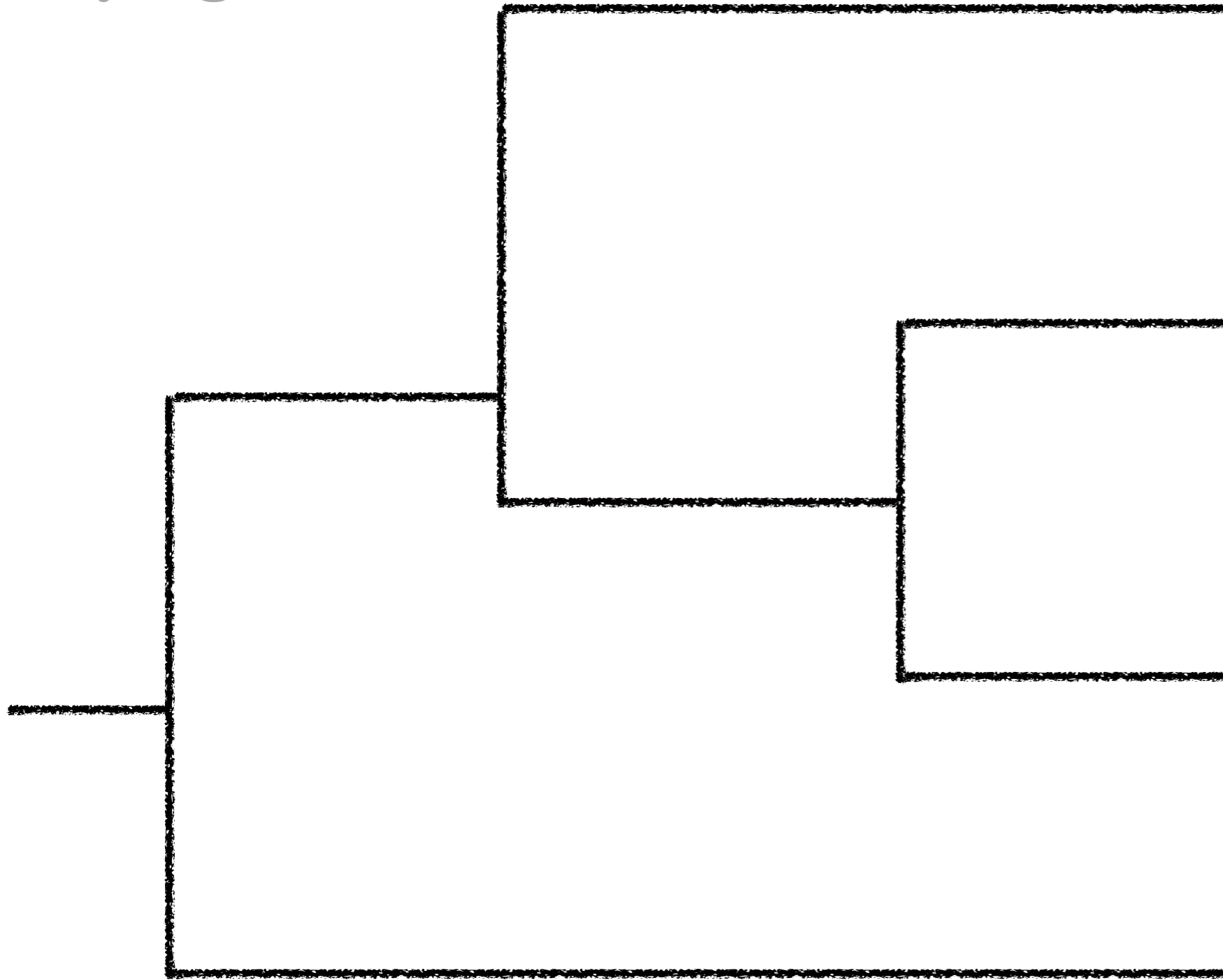
Main tree



Why?

Phylogenetic network

Ignore gene flow
=> Wrong tree!

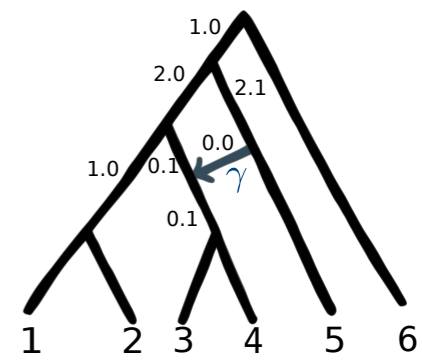


(S.-L., Yang, Ané, 2016, Syst Bio)

Why?

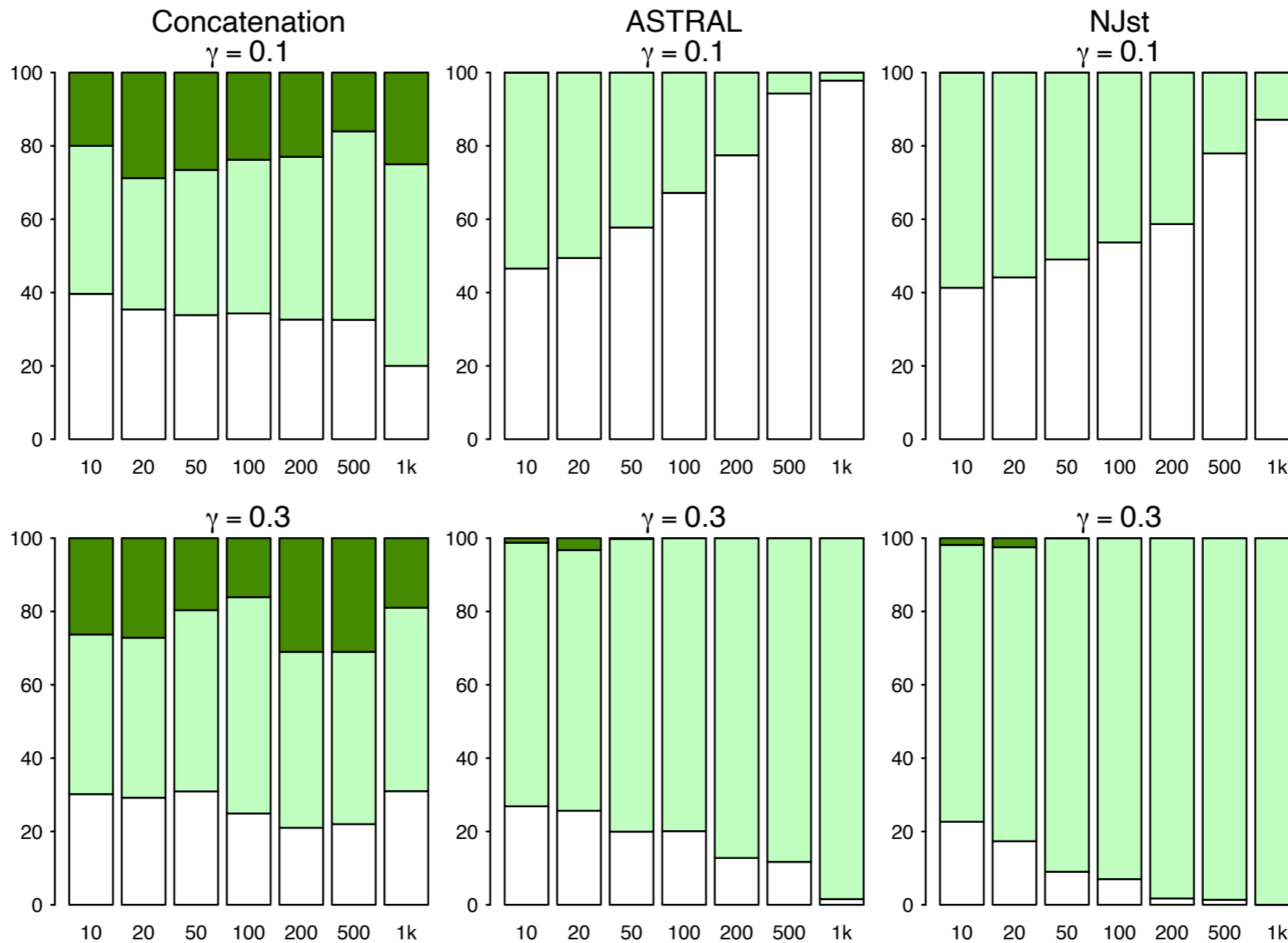
Phylogenetic network

Coalescent tree methods
not robust to gene flow



White:
true tree

Bootstrap support



Number of genes

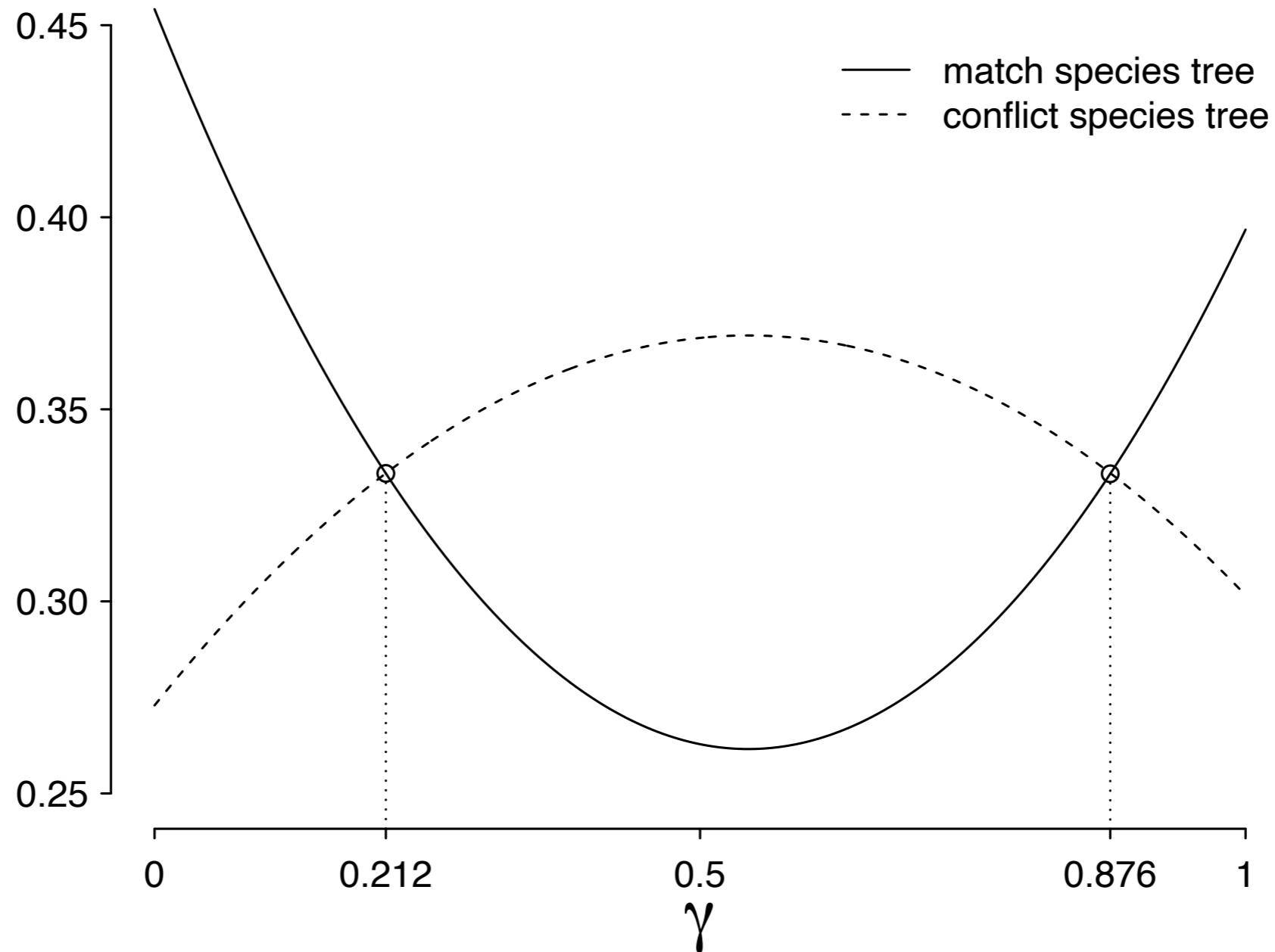
(S.-L., Yang, Ané, 2016, Syst Bio)

ASTRAL (Mirarab et al, 2014)
NJst (Liu&Yu,2011)

Why?

Phylogenetic network

Anomaly zone with
gene flow

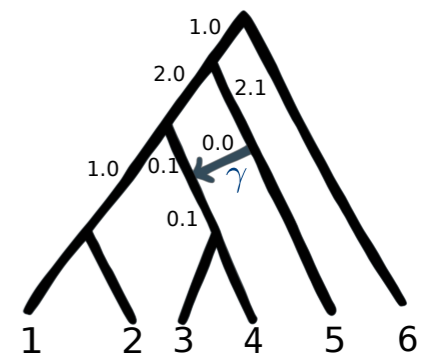


(S.-L., Yang, Ané, 2016, Syst Bio)

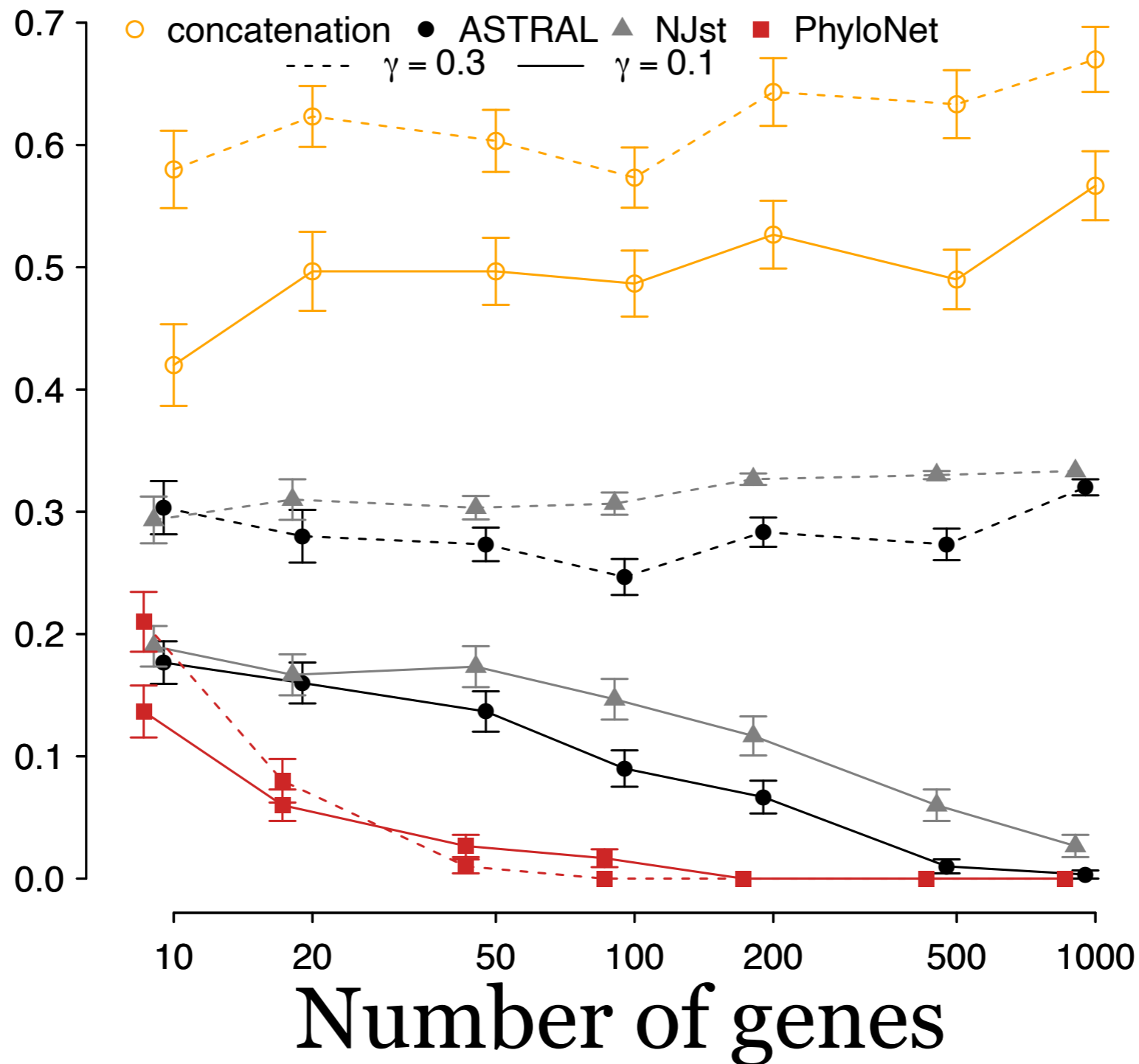
Why?

Phylogenetic network

Coalescent tree methods
not robust to gene flow



Mean RF distance



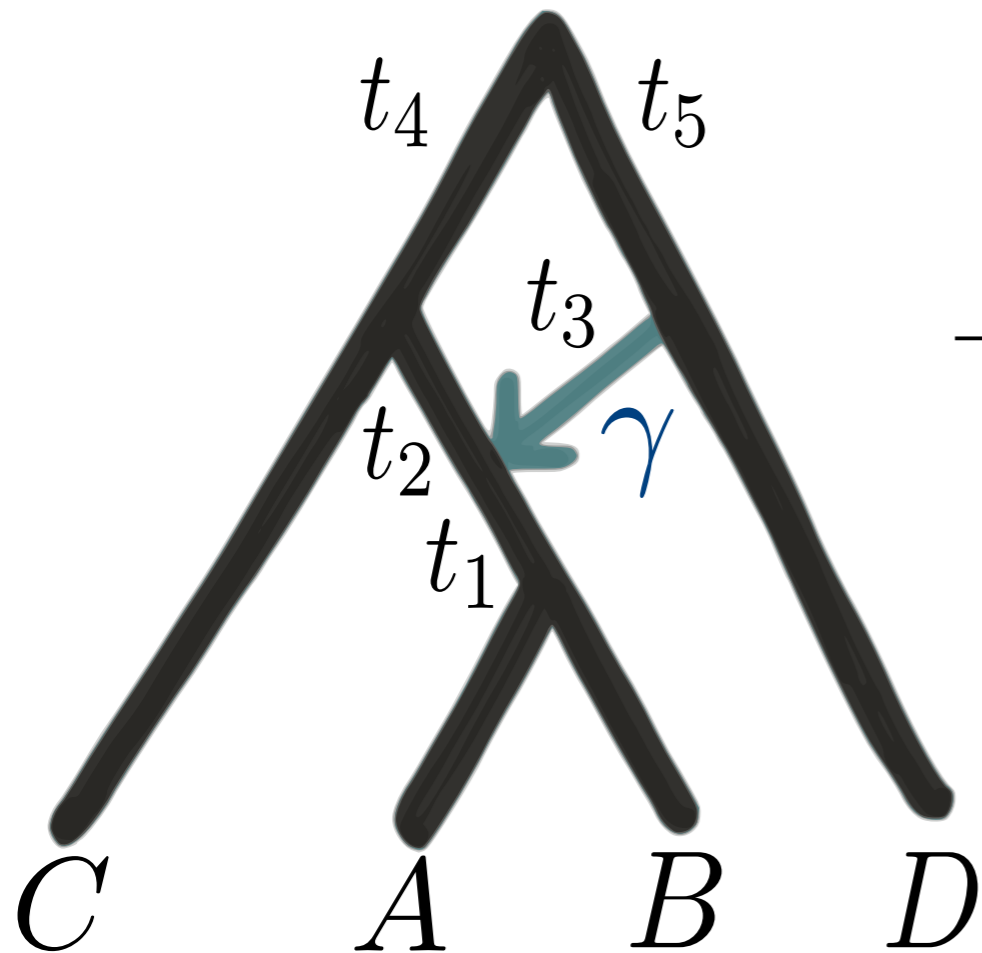
(S.-L., Yang, Ané, 2016, Syst Bio)

ASTRAL (Mirarab et al, 2014)
NJst (Liu&Yu,2011)
PhyloNet (Yu et al 2012, 2014)

Why?

Phylogenetic network

Anomalous unrooted gene trees with gene flow



Frequency among gene trees

Quartet	$\gamma = 0.0$	$\gamma = 0.1$	$\gamma = 0.3$
$AB CD$	0.347	0.298	0.260
$CA BD$	0.327	0.351	0.370
$CB AD$	0.327	0.351	0.370

$$t_1 = t_2 = 0.01, t_3 = t_4 = t_5 = 1$$

- **ILS**: no AUGT on 4 taxa (Degnan, 2013)
- **ILS+HGT**: AUGT on 4 taxa (S.-L., Yang, Ané, 2016, Syst Bio)

See also Long & Kubatko (2018) for AUGT under continuous gene flow between sister species

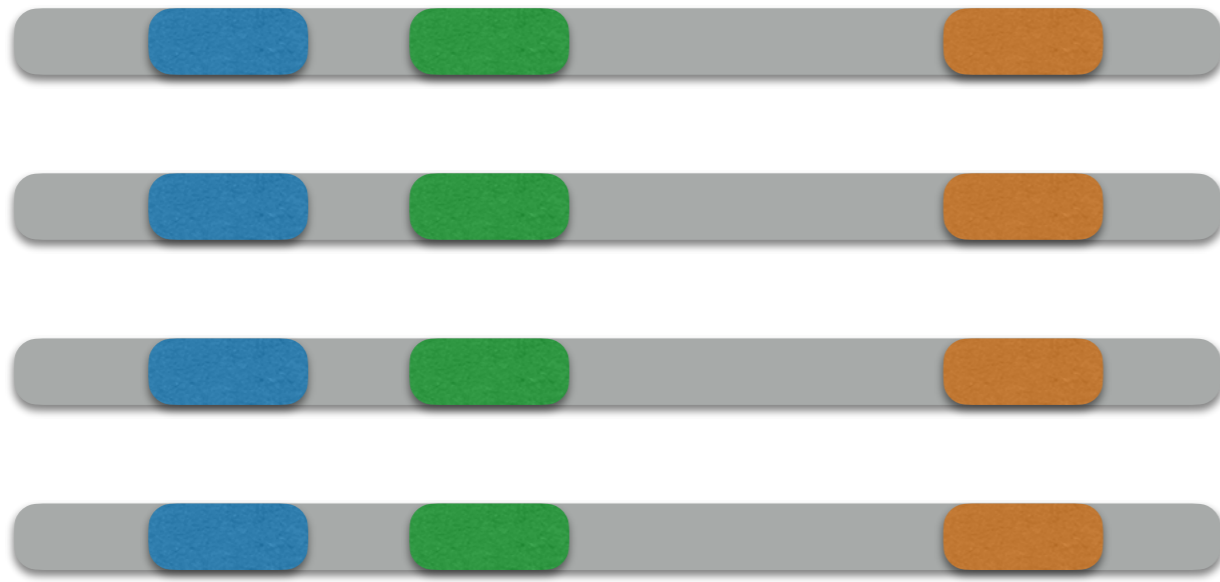
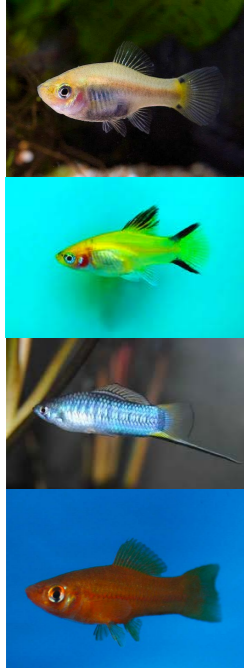
So far...

- Networks are good
- Explicit networks are better
- If you ignore gene flow, you can estimate the wrong tree

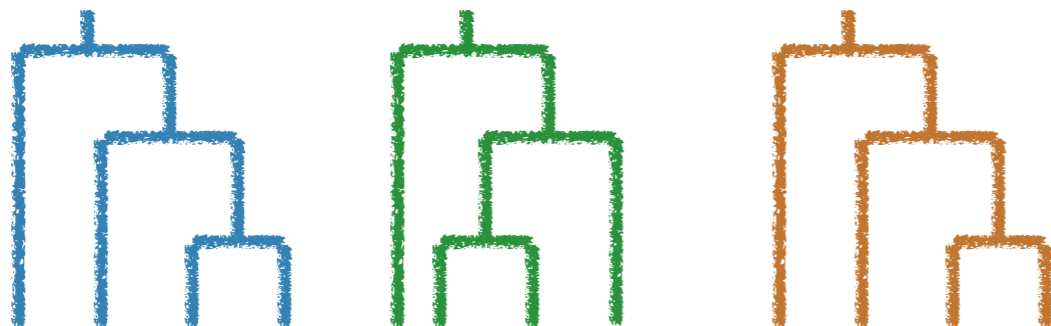


How?

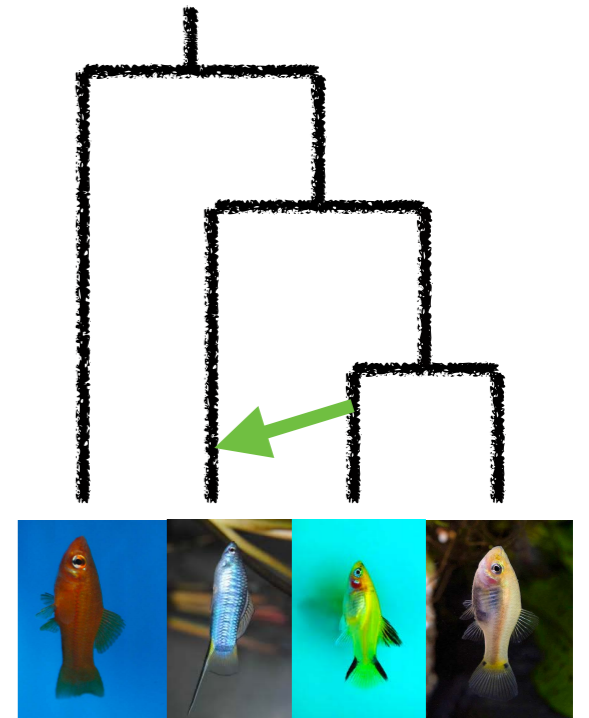
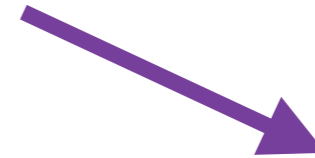
Phylogenetic network



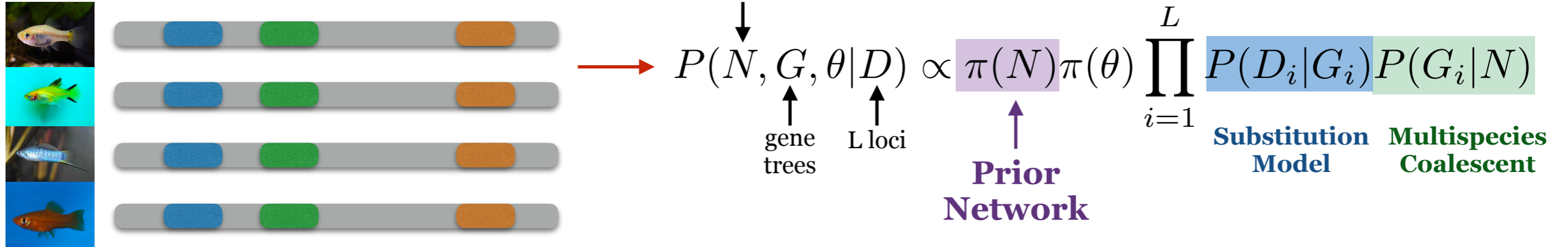
MrBayes
(Huelsenbeck, Ronquist, 2001)
RAxML
(Stamatakis, 2014)
PhyML
(Guindon et al, 2010)
RevBayes
(Hoehna et al, 2016)
IQ-TREE
Nguyen et al. (2015)



BEAST2
(Zhang et al, 2017)
PhyloNet
(Wen et al, 2016)



SNaQ
(S.-L., Ane, 2016)
PhyloNet
(Yu et al, 2014)

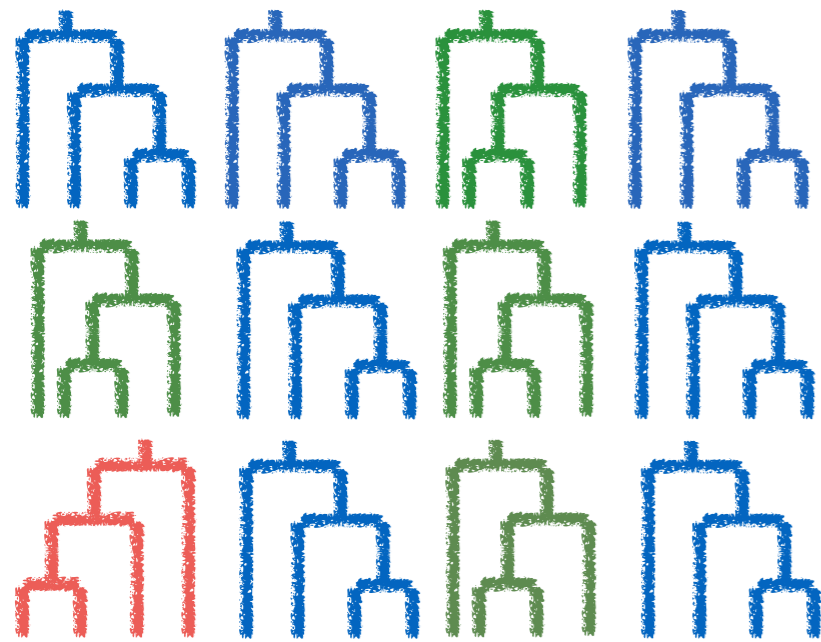


Birth-hybridization process

BEAST2
(Zhang et al, 2017)

reticulations, cycle diameter

PhyloNet
Bayesian
(Wen et al, 2016)

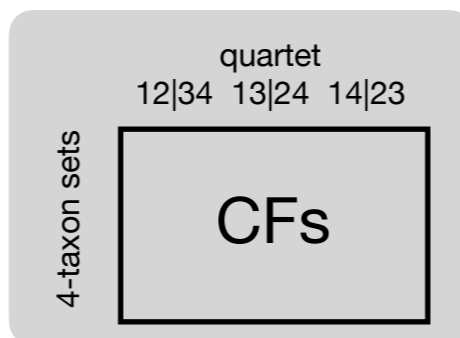


$$P(N, \theta | G) \propto \pi(N) \pi(\theta) \prod_{i=1}^L P(G_i | N, \theta)$$

PhyloNet
Bayesian
(Wen et al, 2016)

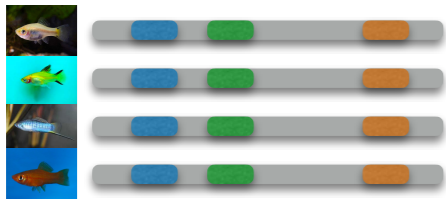
$$L(N, \theta) = \prod_{i=1}^L P(G_i | N, \theta)$$

PhyloNet
Likelihood
(Yu et al, 2014)



$$\tilde{L}(N, \theta) \propto \prod_q L(q | N, \theta)$$

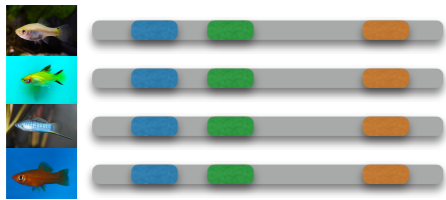
SNaQ
(S.-L., Ane, 2016)



BEAST2
(Zhang et al, 2017)

Birth-
hybridization
process

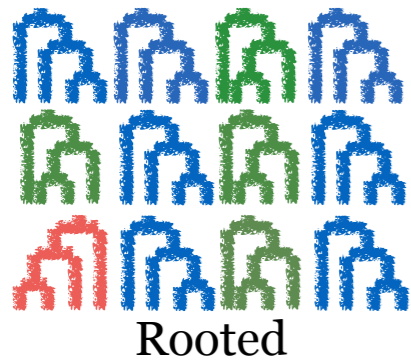
Most accurate,
not scalable



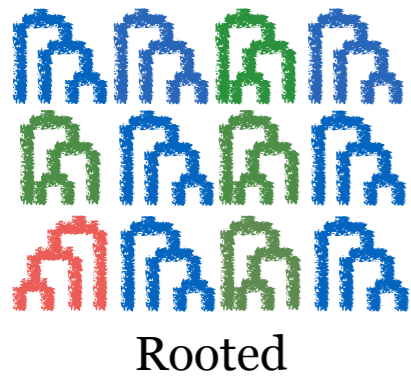
**PhyloNet
Bayesian**
(Wen et al, 2016)

MCMC:
Network
moves,
mixing

reticulations,
cycle diameter

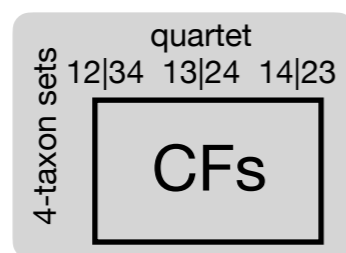
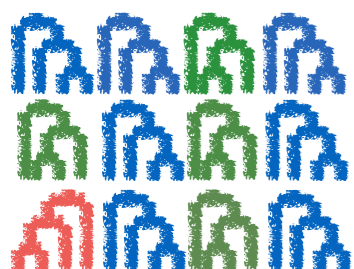


**PhyloNet
Bayesian**
(Wen et al, 2016)



**PhyloNet
Likelihood**
(Yu et al, 2014)

**Heuristic
search:**
Network
moves



SNaQ
(S.-L., Ane, 2016)

Level-1
networks

More scalable,
Robust

STEM-hy	gene trees rooted, BL	likelihood	hybridization b/w sister lineages
PhyloNet <i>InferNetwork_ML</i>	gene trees rooted	likelihood	
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Hybrid detection methods

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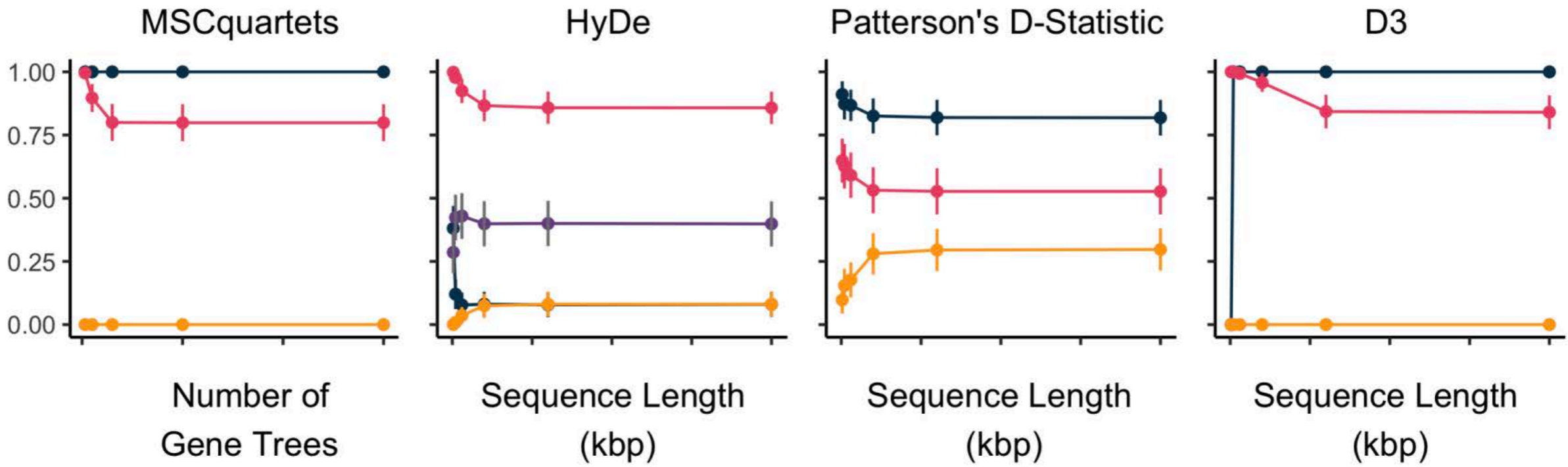
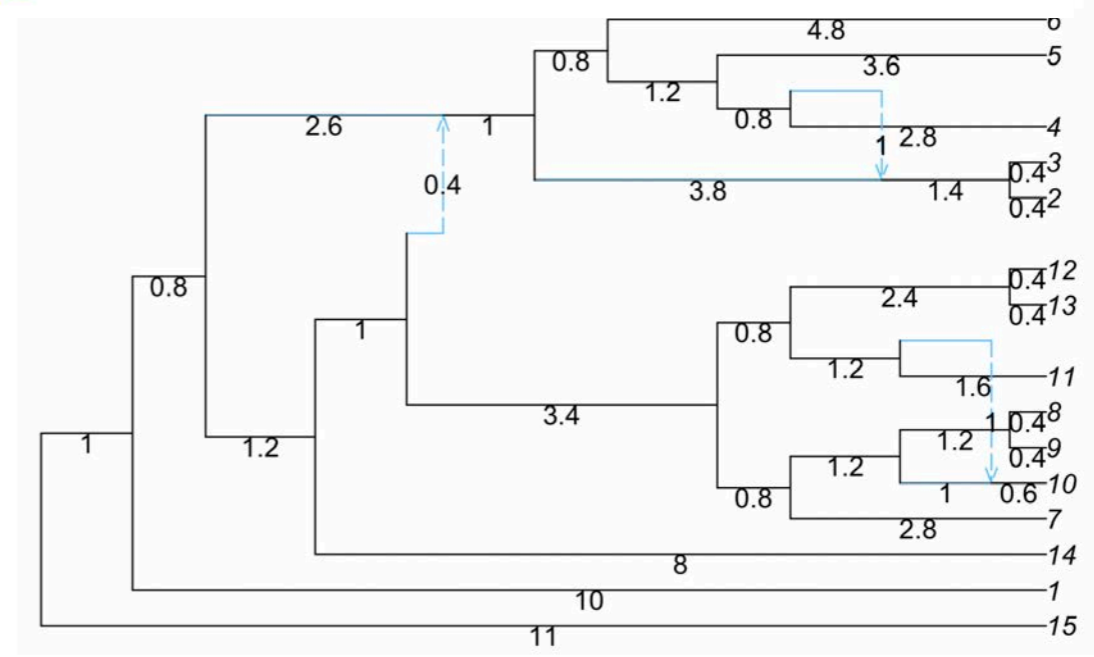
Marianne Bjørner

[Submitted on 1 Nov 2022]

Detectability of Varied Hybridization Scenarios using Genome-Scale Hybrid Detection Methods

Marianne Bjørner, Erin K. Molloy, Colin N. Dewey, Claudia Solis-Lemus

Ancient gene flow distorts discovery rates for hybrid detection methods



● Precision ● False Positive Rate ● False Negative Rate ● Wrong Hybrid Rate

(See also Kong & Kubatko, 2021)

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Hybrid detection methods

**Estimate
explicit
network
under the
coalescent**

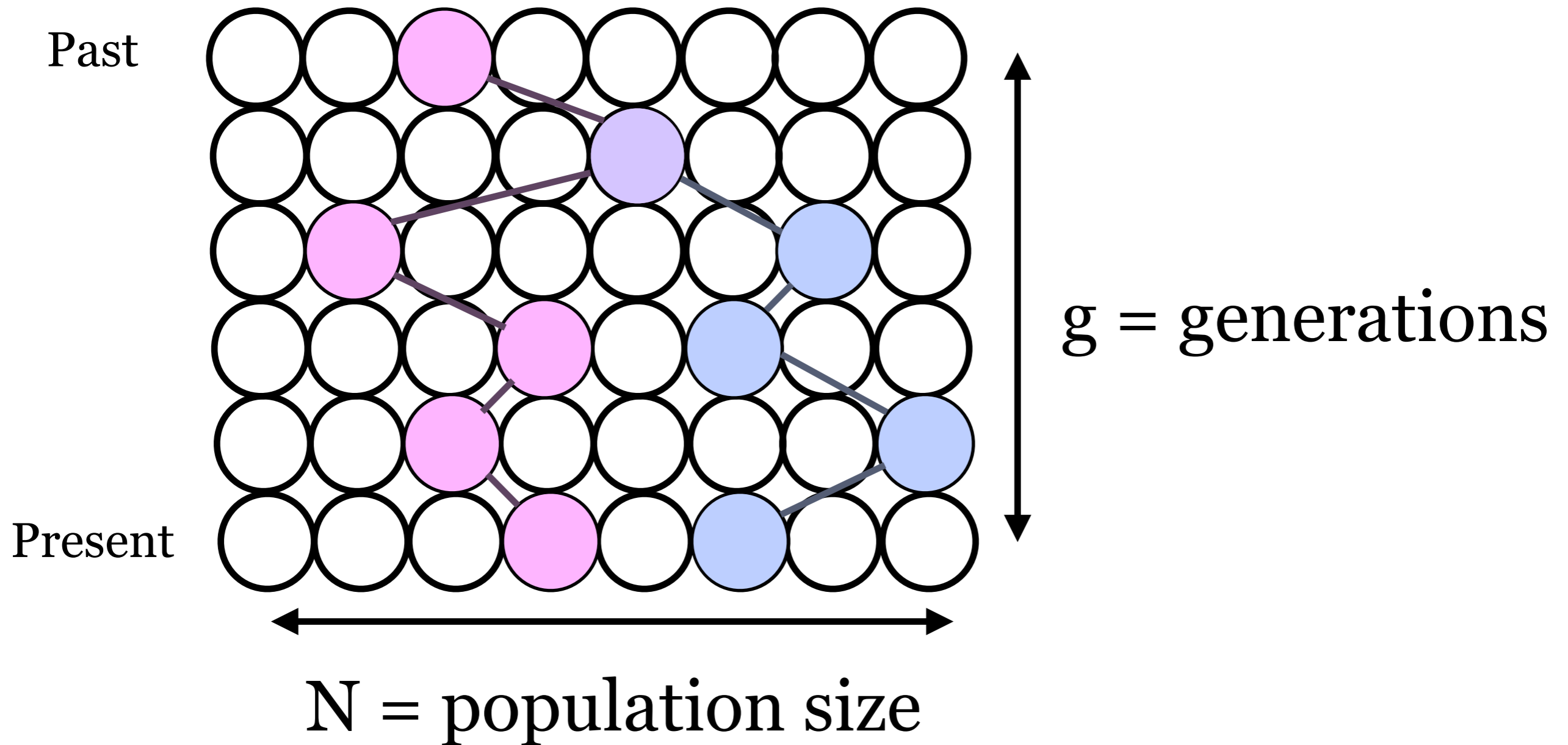


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Estimate explicit network under the coalescent

Hybrid detection methods

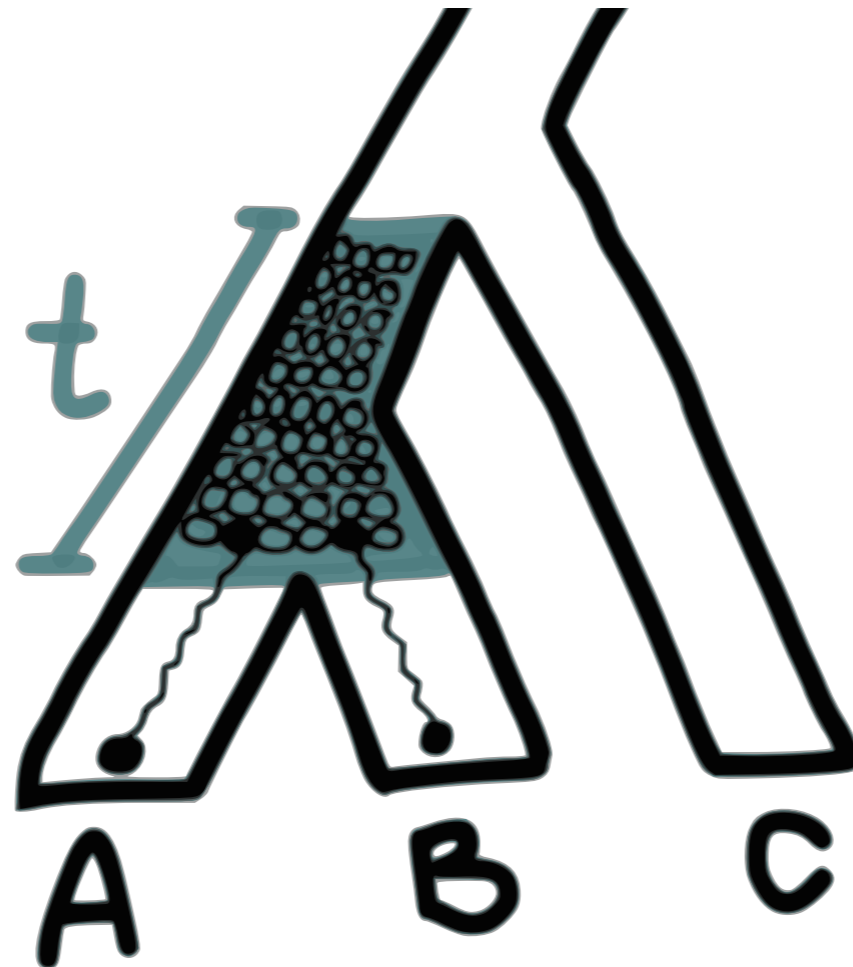
Coalescent model within 1 population



Probability of no coalescence in g generations: $\left(1 - \frac{1}{N}\right)^g$

$$t = g/N \Rightarrow \left(1 - \frac{t}{Nt}\right)^{Nt} \xrightarrow{N \rightarrow \infty} e^{-t}$$

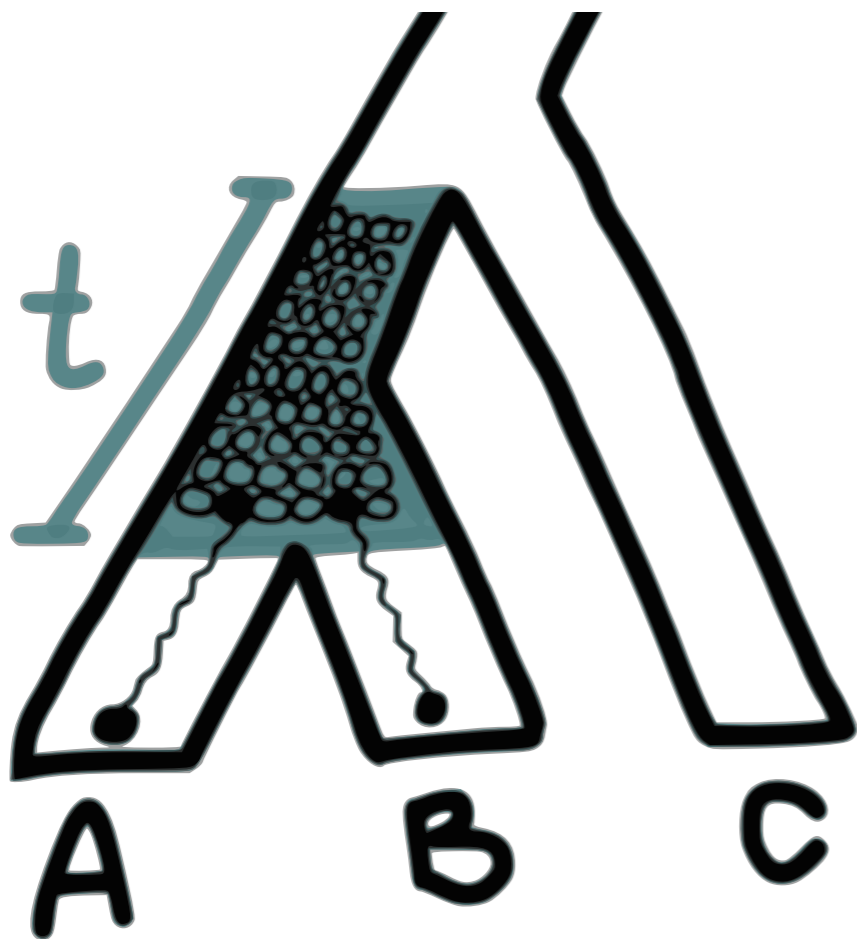
Multispecies coalescent on a tree



$$P(T > t) = e^{-t}$$

$$T = \frac{g}{N} \text{ coalescent units} \sim \text{Exp}(1)$$

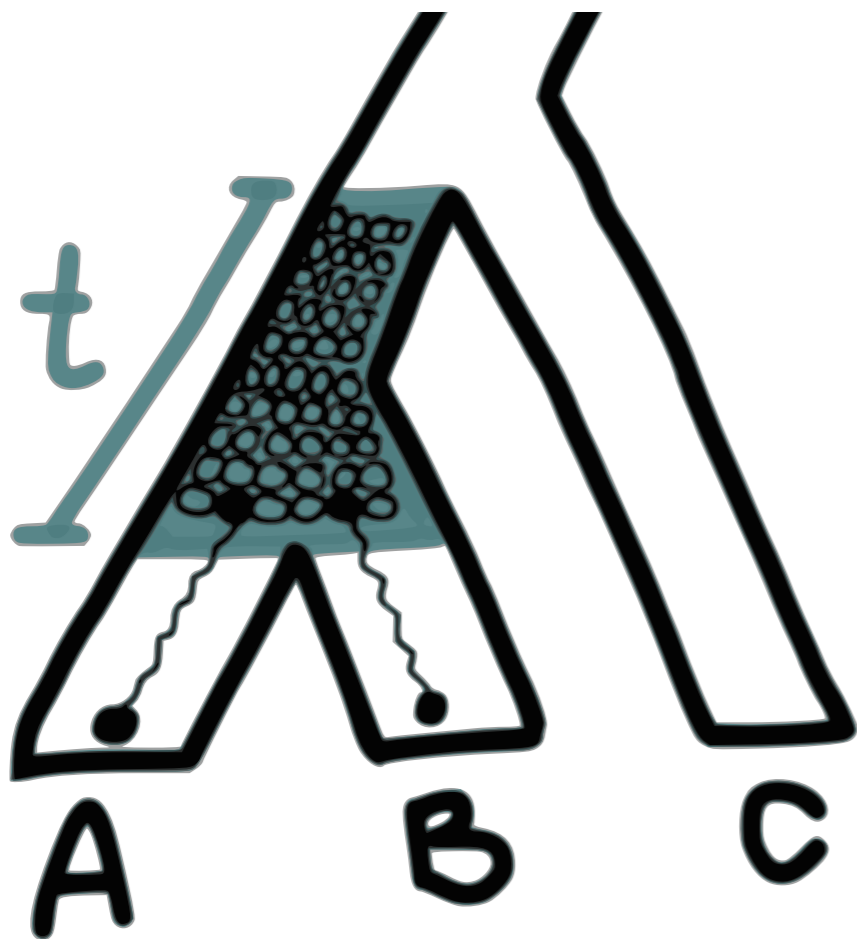
Multispecies coalescent on a tree



$$P \left(\begin{array}{c} \diagup \\ \diagdown \\ A \quad B \quad C \end{array} \right) =$$

$$P(T > t) = e^{-t}$$

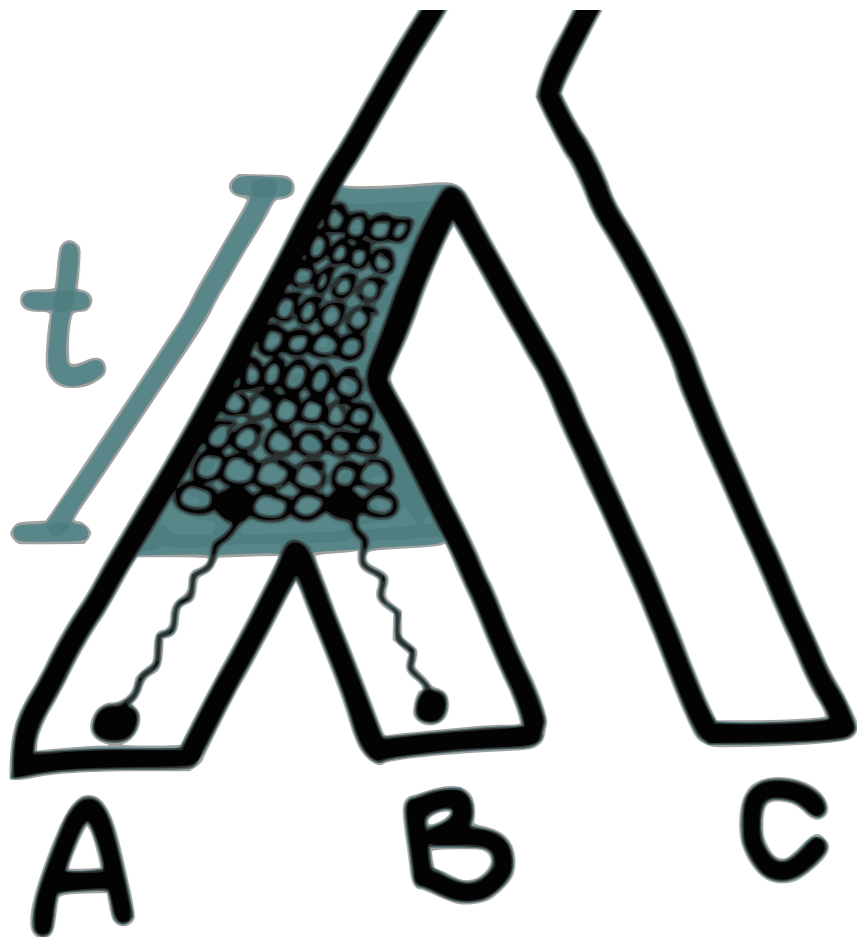
Multispecies coalescent on a tree



$$P \left(\begin{array}{c} \diagup \\ \diagdown \\ A \quad B \quad C \end{array} \right) = 1 - e^{-t}$$

$$P(T > t) = e^{-t}$$

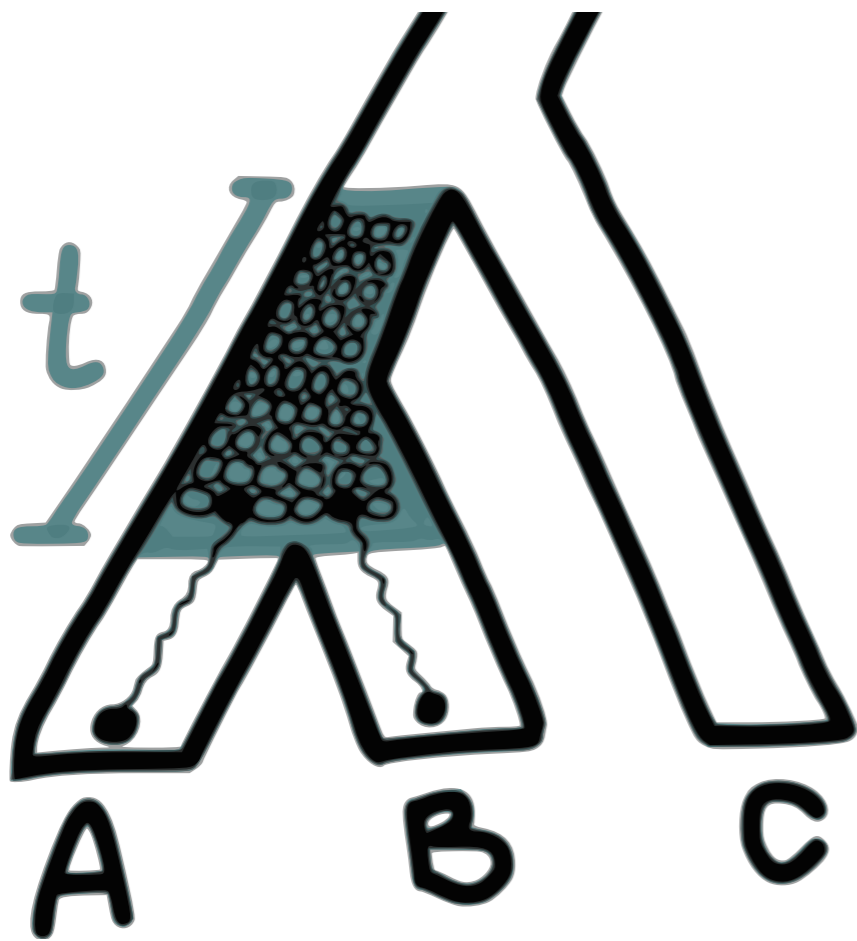
Multispecies coalescent on a tree



$$P \left(\begin{array}{c} \diagup \\ \diagdown \\ A \quad B \quad C \end{array} \right) = 1 - e^{-t} + e^{-t}$$

$$P(T > t) = e^{-t}$$

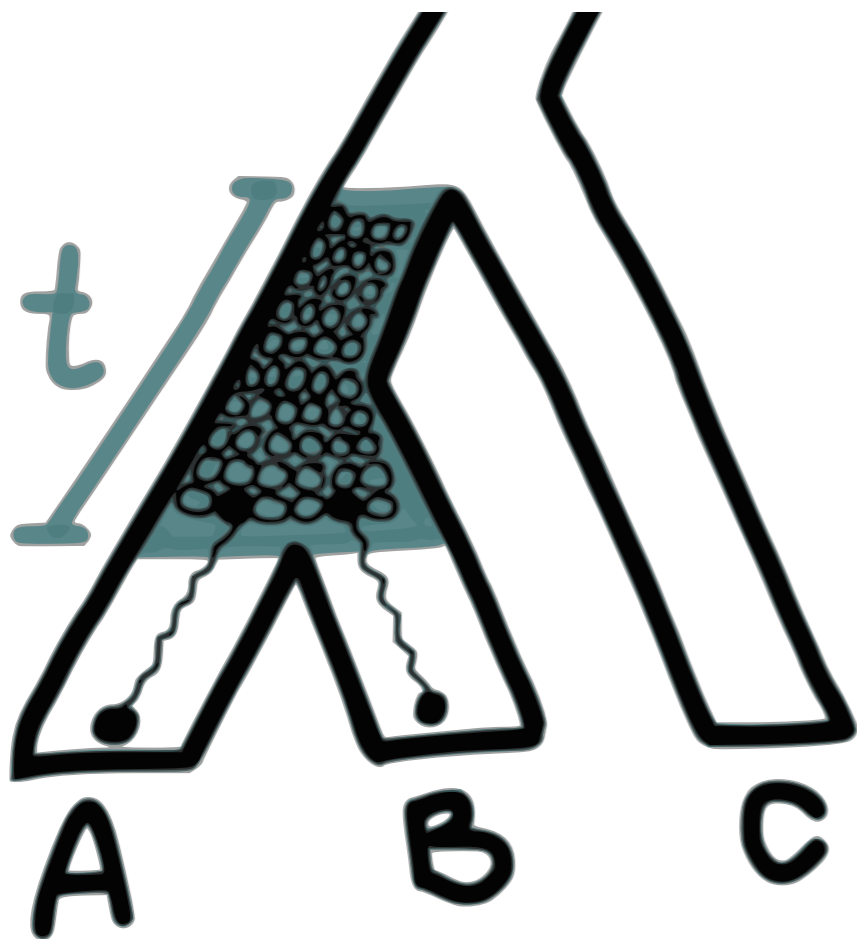
Multispecies coalescent on a tree



$$P(T > t) = e^{-t}$$

$$P\left(\begin{array}{c} \wedge \\ A \quad B \quad C \end{array}\right) = 1 - e^{-t} + e^{-t} \times 1/3$$

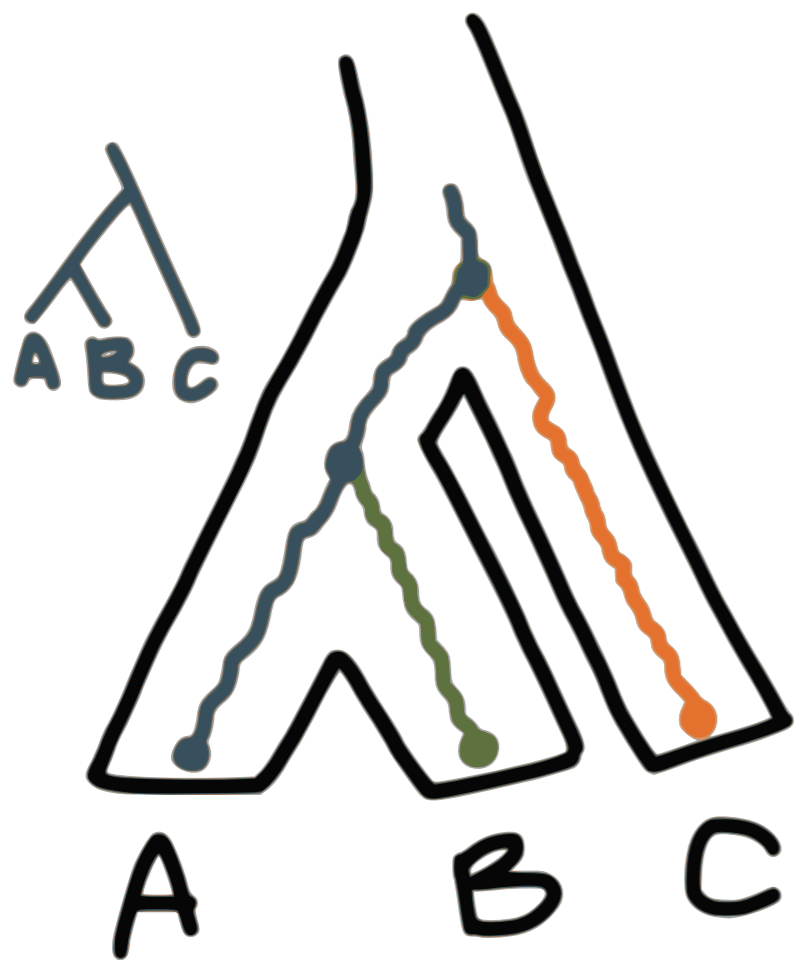
Multispecies coalescent on a tree



$$P(T > t) = e^{-t}$$

$$\begin{aligned} P\left(\begin{array}{c} \wedge \\ A \quad B \quad C \end{array}\right) &= \\ & 1 - e^{-t} \\ & + \\ & e^{-t} \times \frac{1}{3} \\ & = 1 - \frac{2}{3}e^{-t} \end{aligned}$$

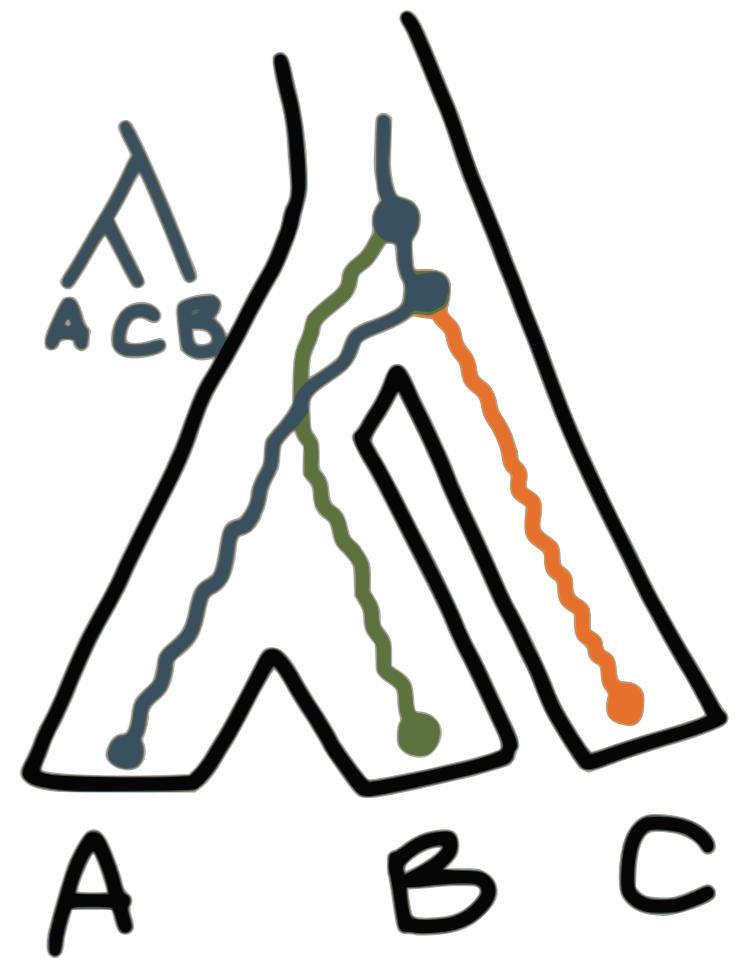
Multispecies coalescent on a tree



$$1 - \frac{2}{3}e^{-t}$$

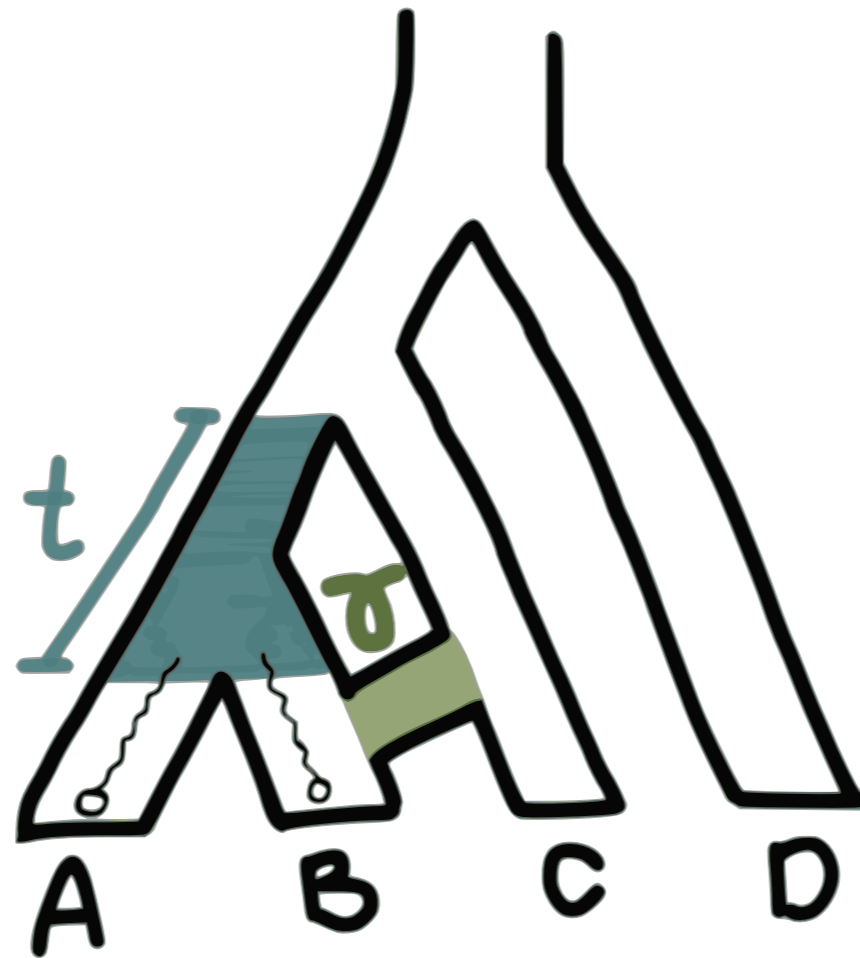


$$\frac{1}{3}e^{-t}$$



$$\frac{1}{3}e^{-t}$$

Multispecies coalescent on a network



(Meng, Kubatko, 2009)
(Yu, Degnan, Nakhleh, 2012)

Multispecies coalescent on a network



(Meng, Kubatko, 2009)
(Yu, Degnan, Nakhleh, 2012)

Multispecies coalescent on a network



$$(1 - \gamma) \frac{1}{3} e^{-t} + \gamma \left(1 - \frac{2}{3} e^{-t_2}\right)$$

(Meng, Kubatko, 2009)
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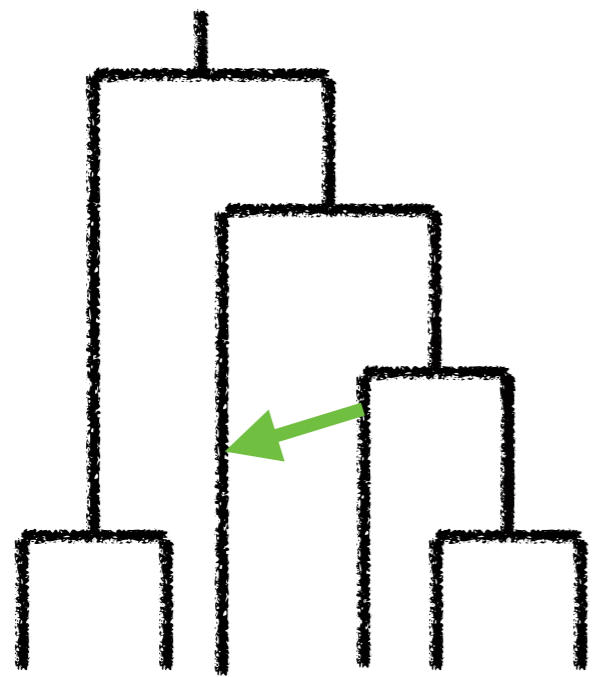
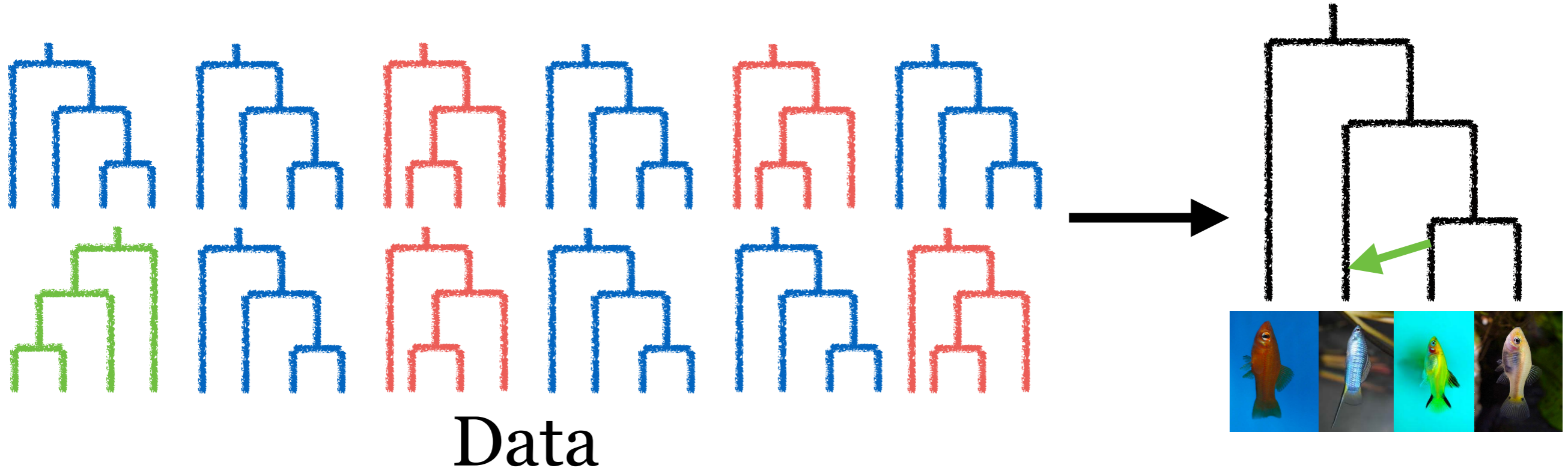
Multispecies coalescent on a network



$$CF_{BC|AD}(t, t_2, \gamma) = (1 - \gamma) \frac{1}{3} e^{-t} + \gamma \left(1 - \frac{2}{3} e^{-t_2}\right)$$

(Meng, Kubatko, 2009)
(Yu, Degnan, Nakhleh, 2012)

Maximum **pseudo**likelihood



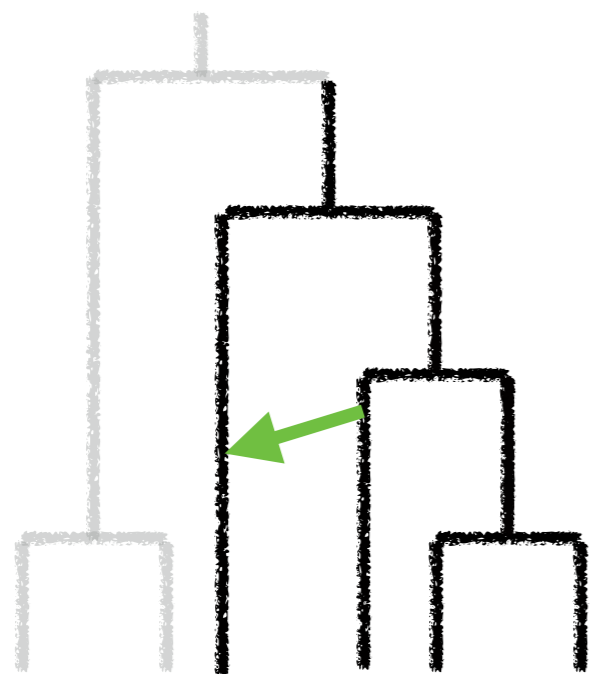
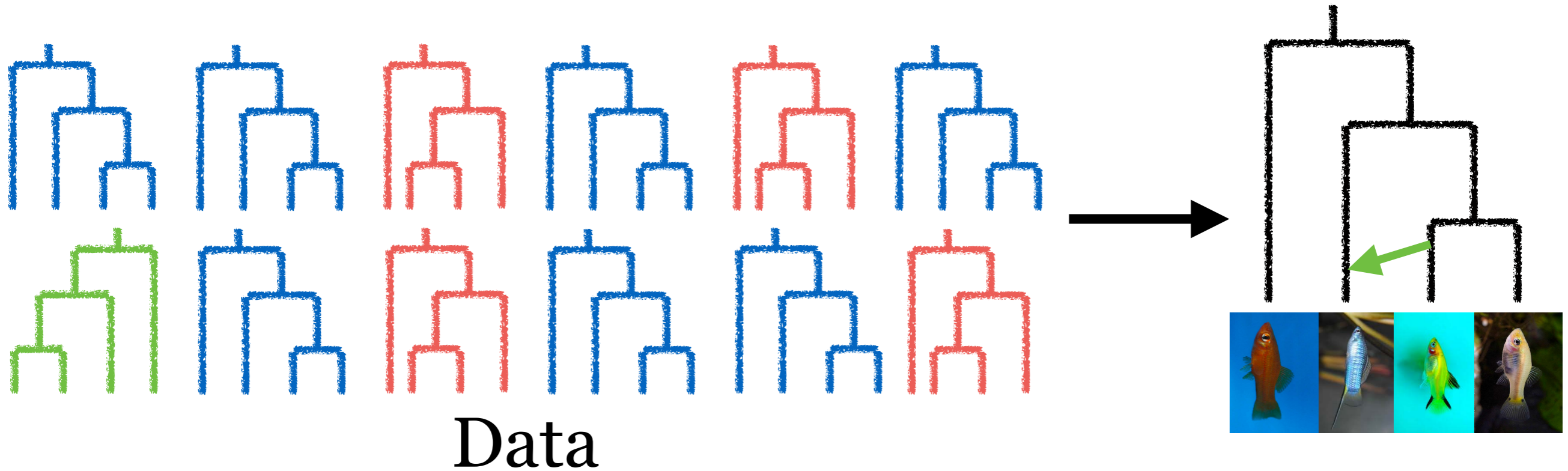
Quartet-based inference

$$\tilde{L}(\text{network}) = \prod L(\text{quartet})$$

(S-L, Ané, 2016, PLoS Genetics)

www.github.com/CRSL4/PhyloNetworks

Maximum **pseudo**likelihood



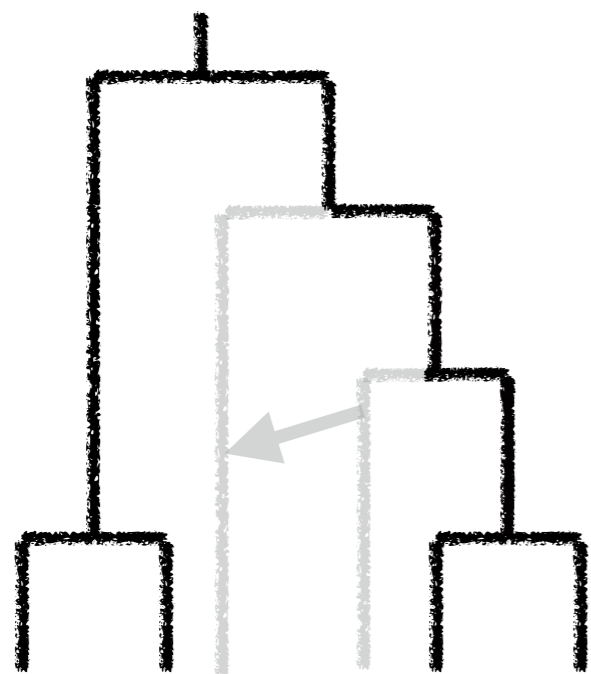
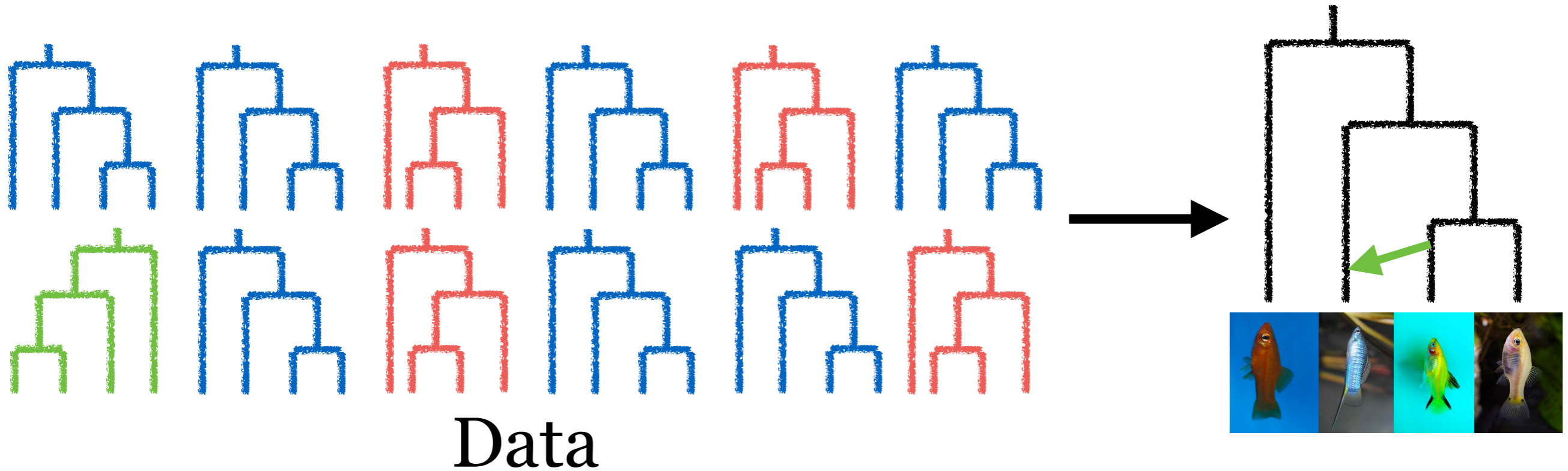
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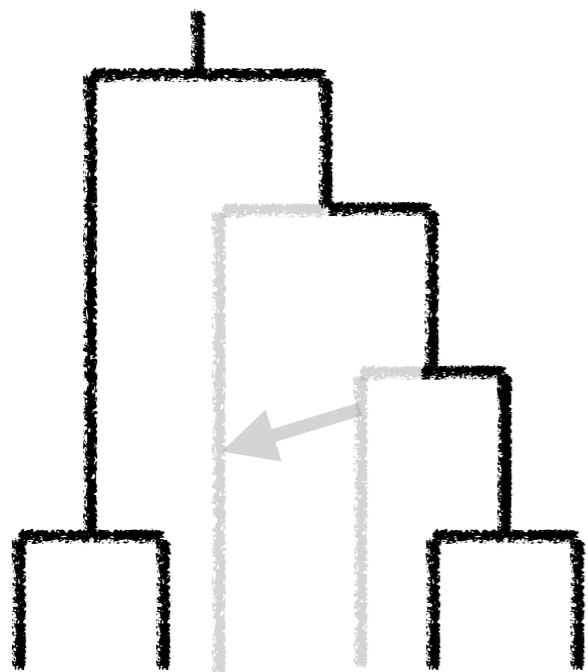
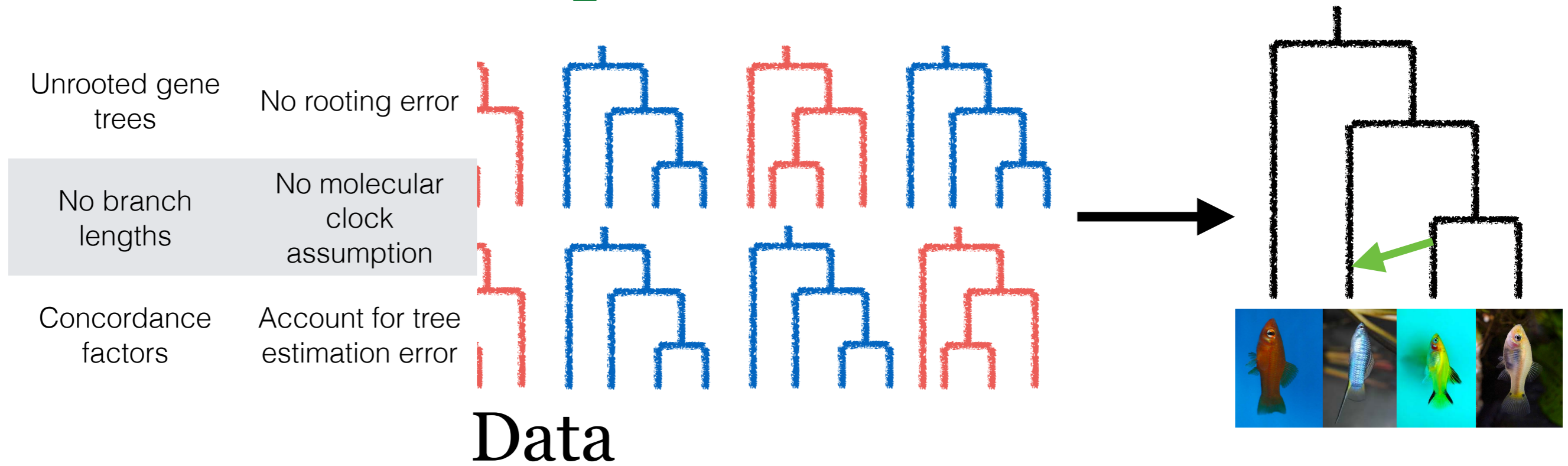
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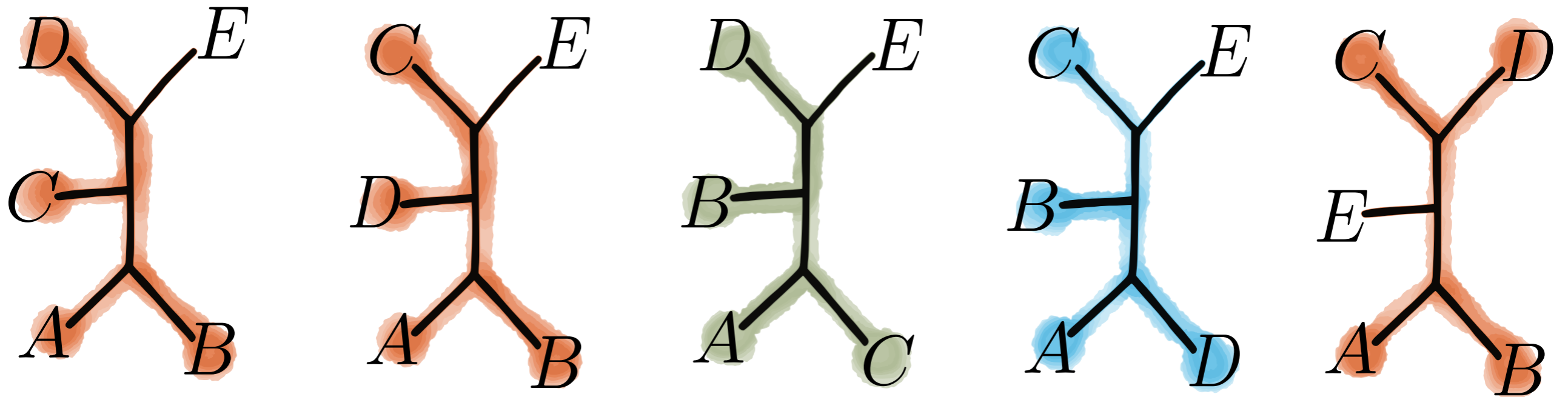
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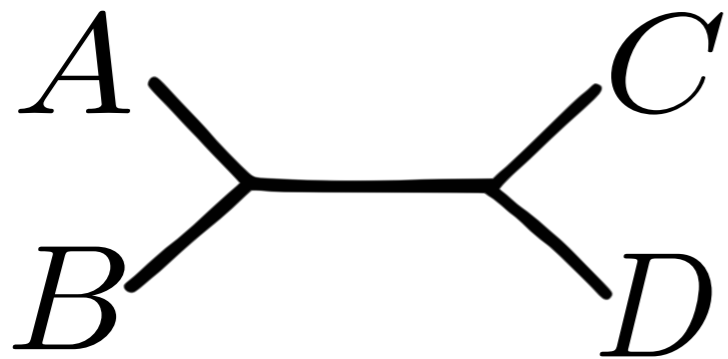
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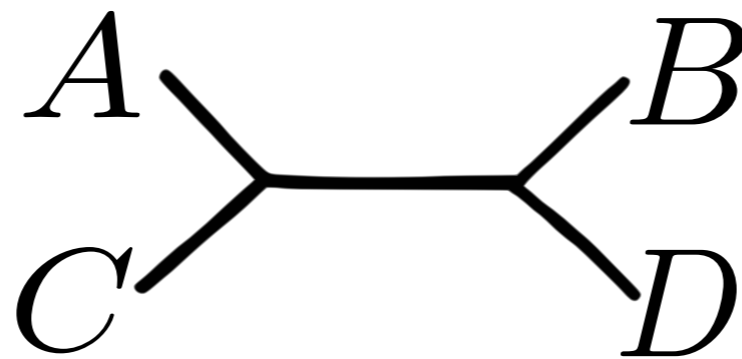
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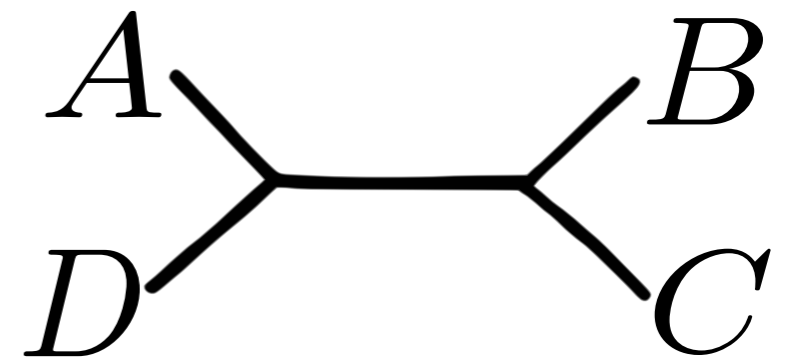
Concordance factors (CF):
% of genes having the quartet in their tree



$3/5$



$1/5$



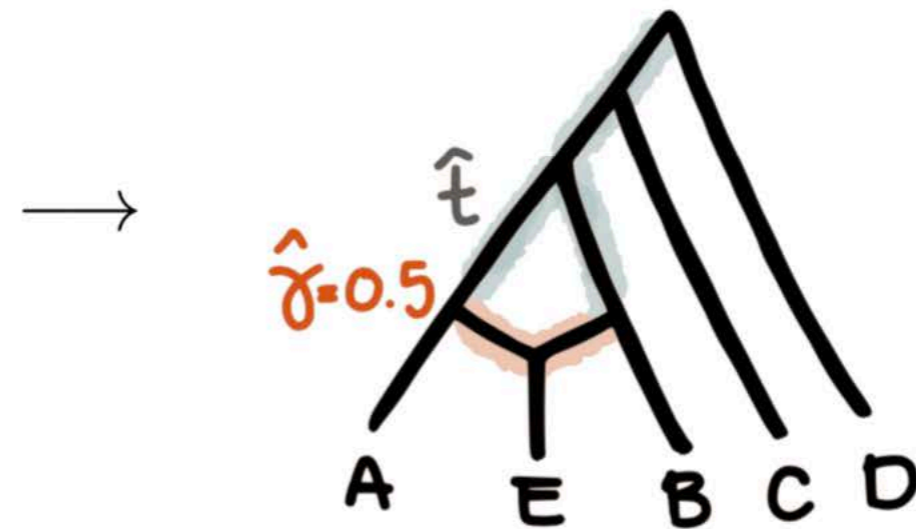
$1/5$

Quartet-based inference

Observed **quartet** CFs:

4 taxon set	CF_1	CF_2	CF_3
A B C D	.80	.10	.10
A B C E	.40	.40	.20
A B D E	.40	.40	.20
A C D E	.84	.08	.08
B C D E	.82	.10	.08

inferred network:

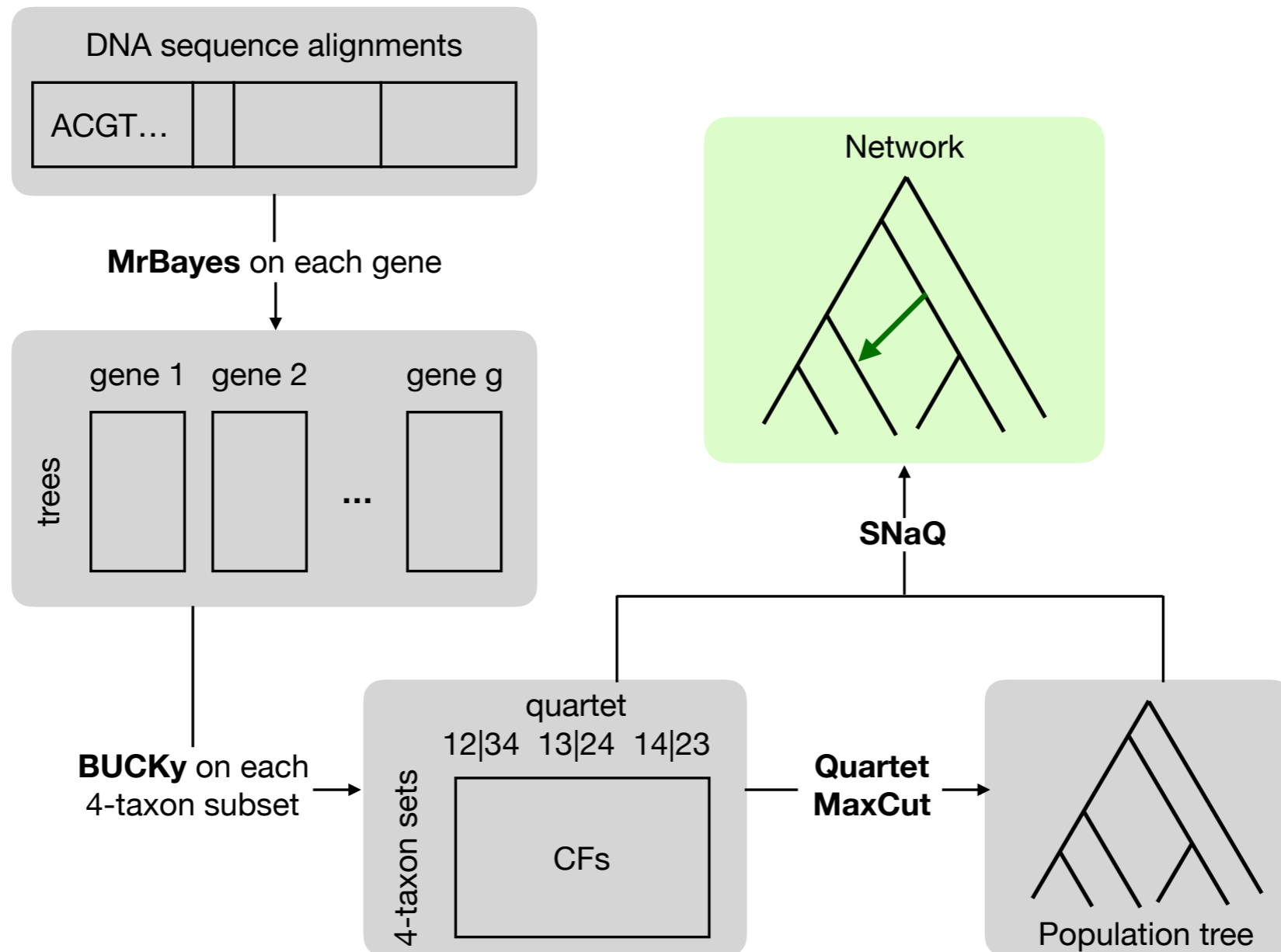


Maximum Pseudo-Likelihood:

$$\log \tilde{L} = \sum_{q \in Q(N)} CF_{in,1} \log(CF_{net,1}) + CF_{in,2} \log(CF_{net,2}) + CF_{in,3} \log(CF_{net,3})$$

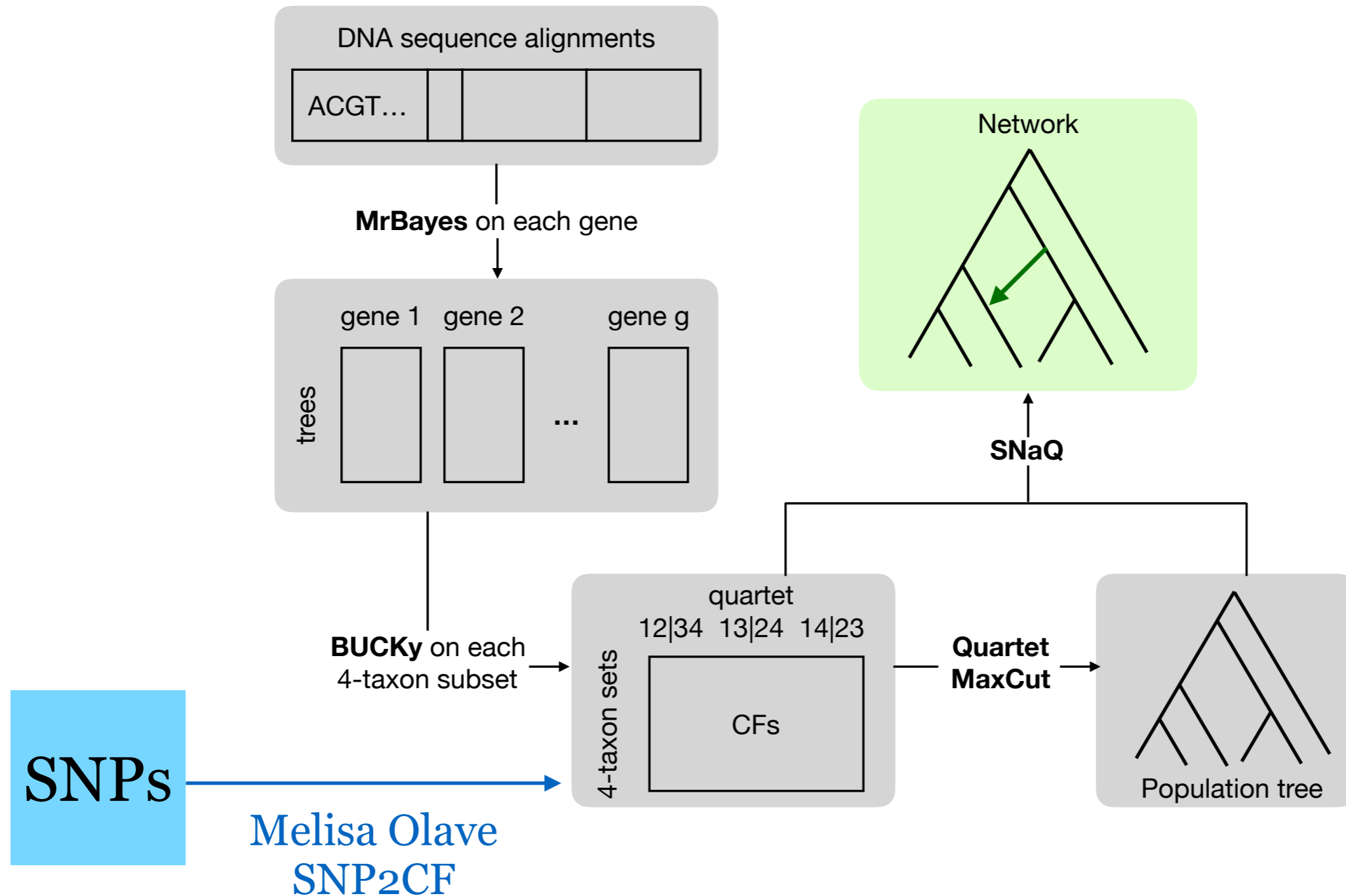
How?

Phylogenetic network



How?

Phylogenetic network



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**Hybrid
detection
methods**

**Hybrid
detection
+
Network
estimation**



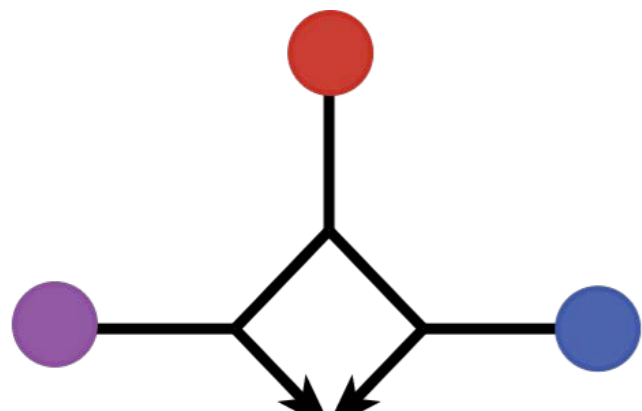
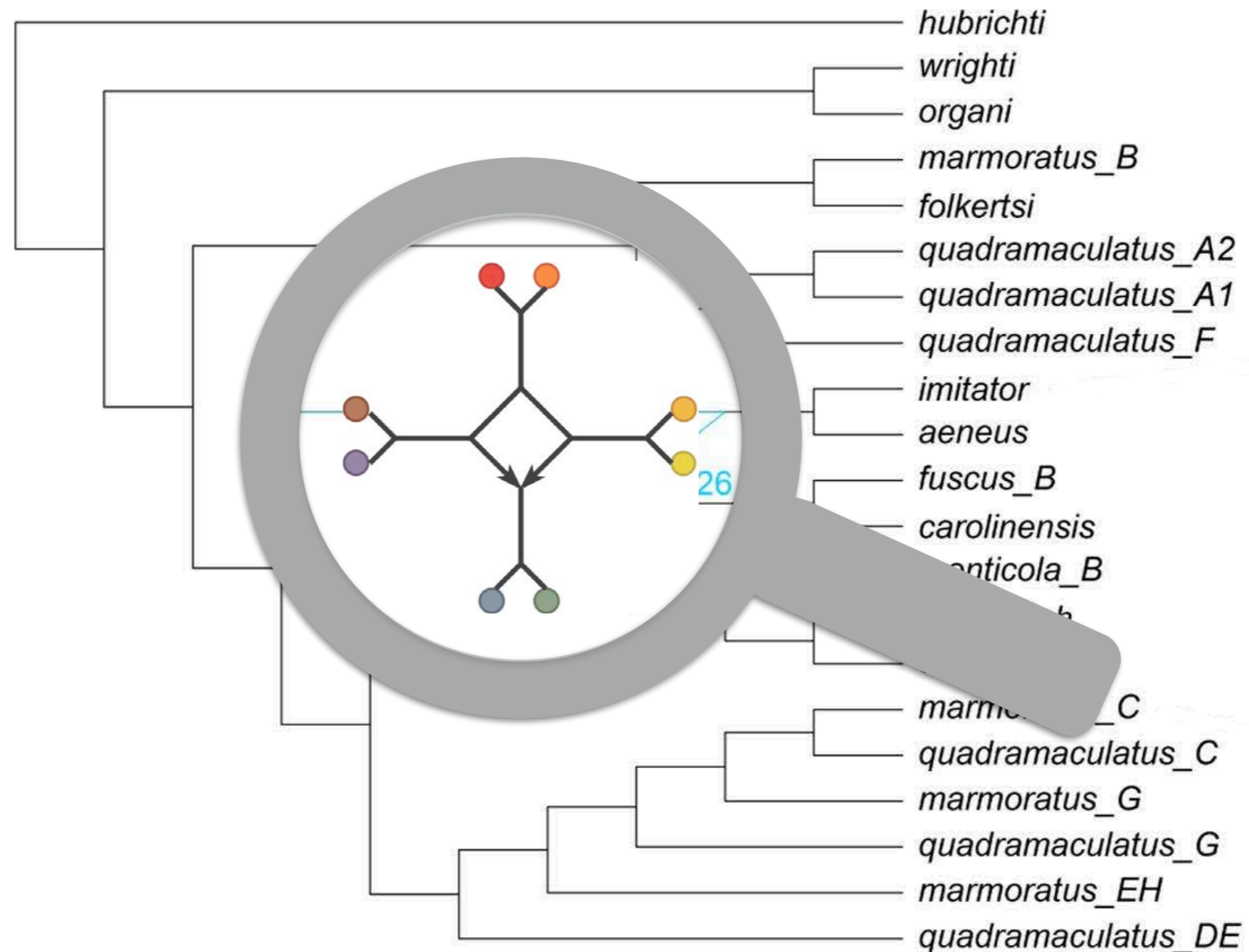
Bella Wu

[Submitted on 30 Nov 2022]

Ultrafast learning of 4-node hybridization cycles in phylogenetic networks using algebraic invariants

Zhaoxing Wu, Claudia Solis-Lemus

Identifies hybridization cycles of 4 nodes



PhyloDiamond.jl



Bella Wu

[Submitted on 30 Nov 2022]

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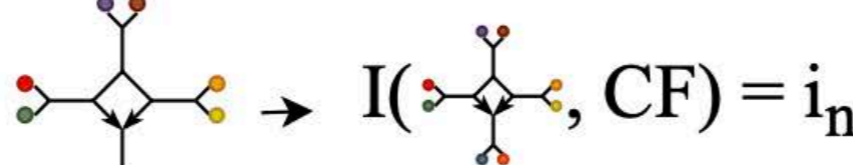
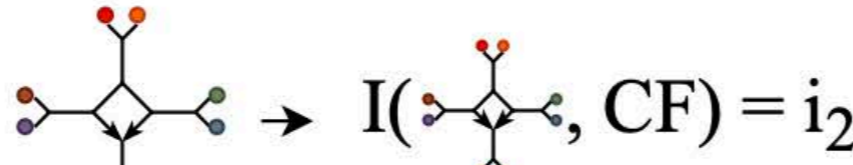
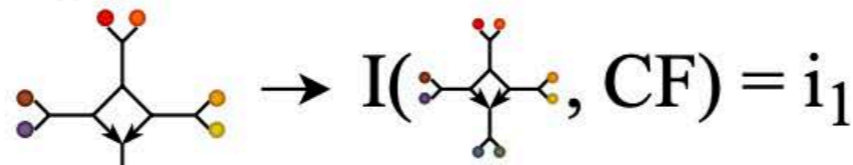
Zhaoxing Wu, Claudia Solis-Lemus

Identifies hybridization cycles of 4 nodes

Iterate through partitions of taxa

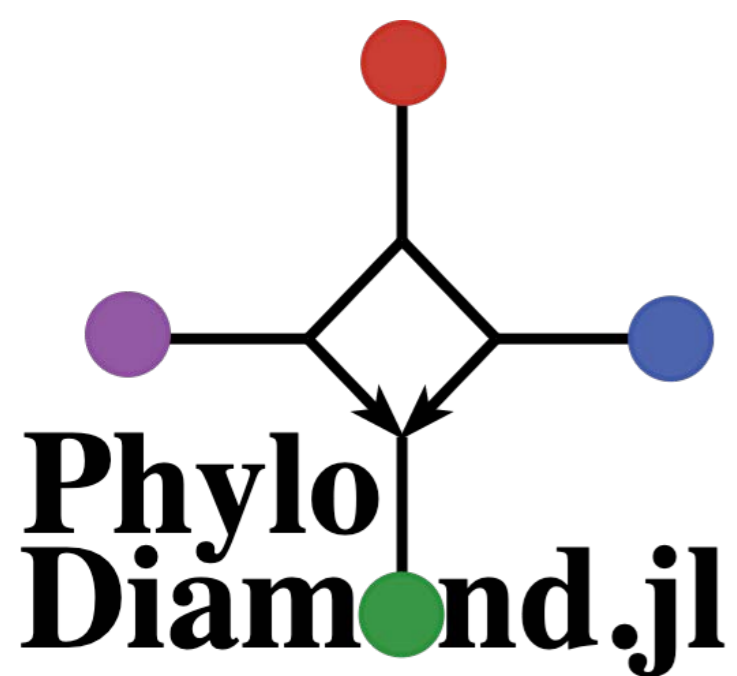
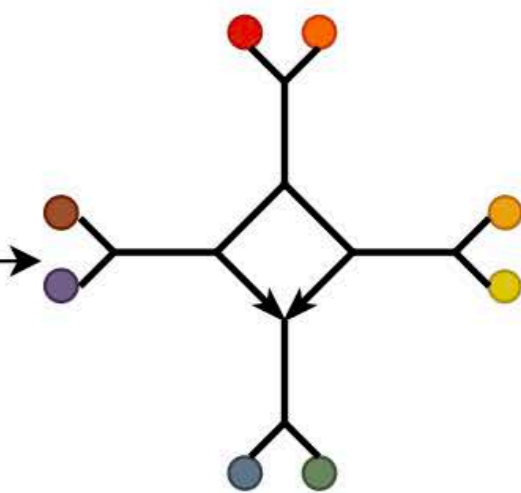
Concordance Factor Table (CF)

	●●	●●	●●	●●
●●●●				
●●●●				
...				
●●●●				



Get Invariant score for each partition

$\min_{[i_1, i_2, \dots, i_n]}$



Note: it cannot resolve relationships among taxa in each of the four clades



Bella Wu

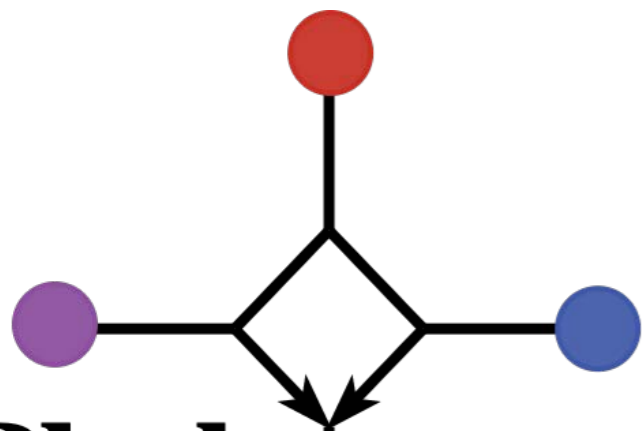
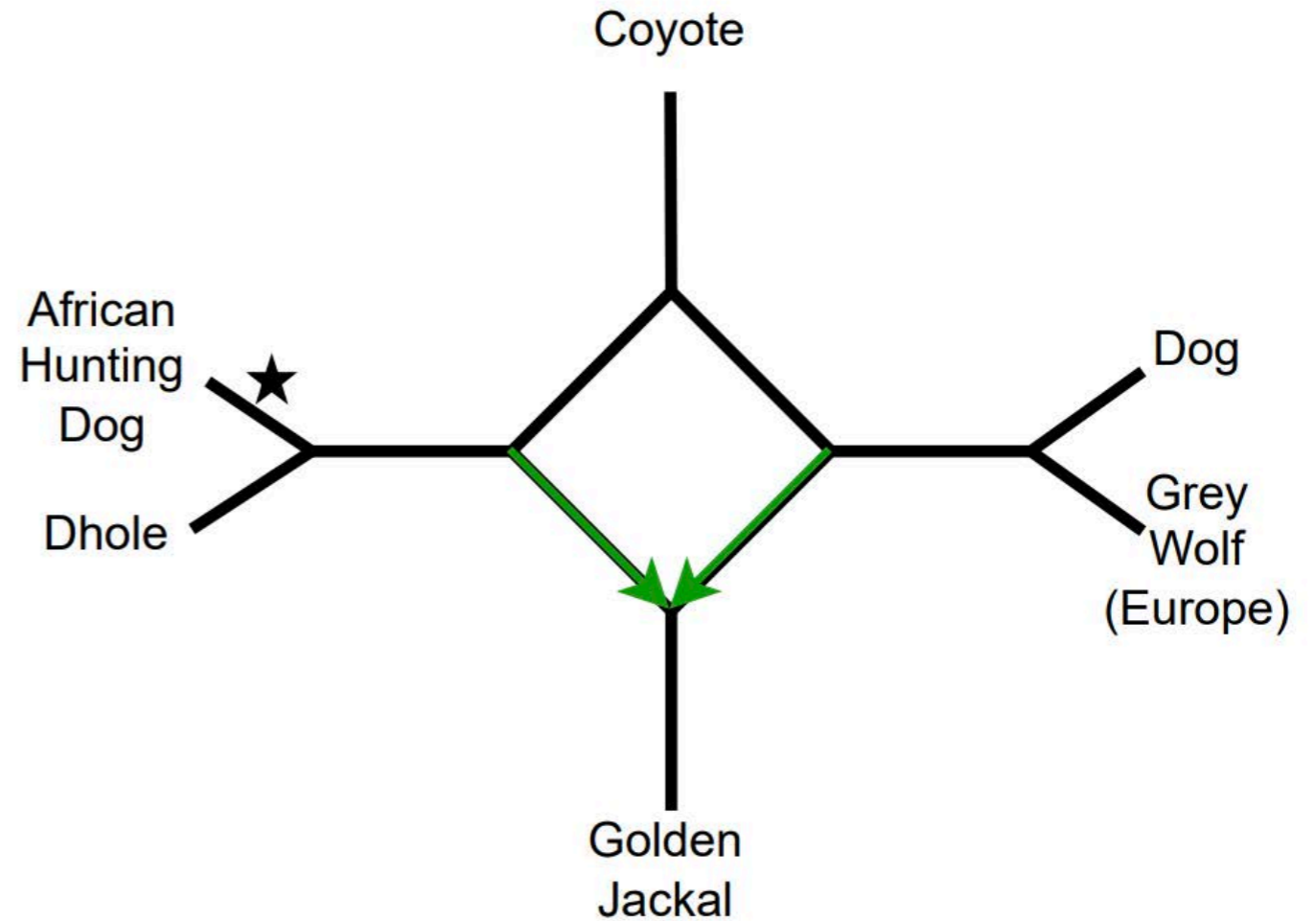
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Ultrafast learning of 4-node hybridization cycles in phylogenetic networks using algebraic invariants

Zhaoxing Wu, Claudia Solis-Lemus

Identifies hybridization cycles of 4 nodes

Method	Time (seconds)
Phylogenetic invariants (our method)	6.78
SNaQ	140.58
PhyloNet ML	2723.99
PhyloNet MPL	281.25



PhyloDiamond.jl

(Data from Gopalakrishnan et al, 2018)

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PhyloNetworks <i>SNaQ</i>	gene trees or quartet CFs	quartet likelihood	level-1 network
PhyloNet <i>MCMC_GT</i>	gene trees rooted	Bayesian	compound prior
PhyloNet <i>MCMC_SEQ</i>	alignments	Bayesian	compound prior no rate variation
BEAST2 <i>SpeciesNetwork</i>	alignments	Bayesian	birth-hyb prior
PhyloNet <i>MLE_BiMarkers</i>	biallelic sites	likelihood	compound prior
PhyloNet <i>MCMC_BiMarkers</i>	biallelic sites	Bayesian	compound prior
HyDe	sites	invariants	4 taxa, 1 hyb.
D-statistics	sites	freq. patterns	4 taxa, 1 hyb.
MSCQuartets	gene trees or quartet CF	quartet likelihood	4 taxa, 1 hyb.
NANUQ	gene trees or quartet CF	quartet likelihood	split (level-1) network
RF-Net	gene trees	min RF distance	No ILS
PhyNEST.jl	sites	quartet likelihood	level-1 network
PhyloDiamond.jl	gene trees or quartet CF	quartet likelihood	level-1 4-cycle network

**Hybrid
detection
methods**

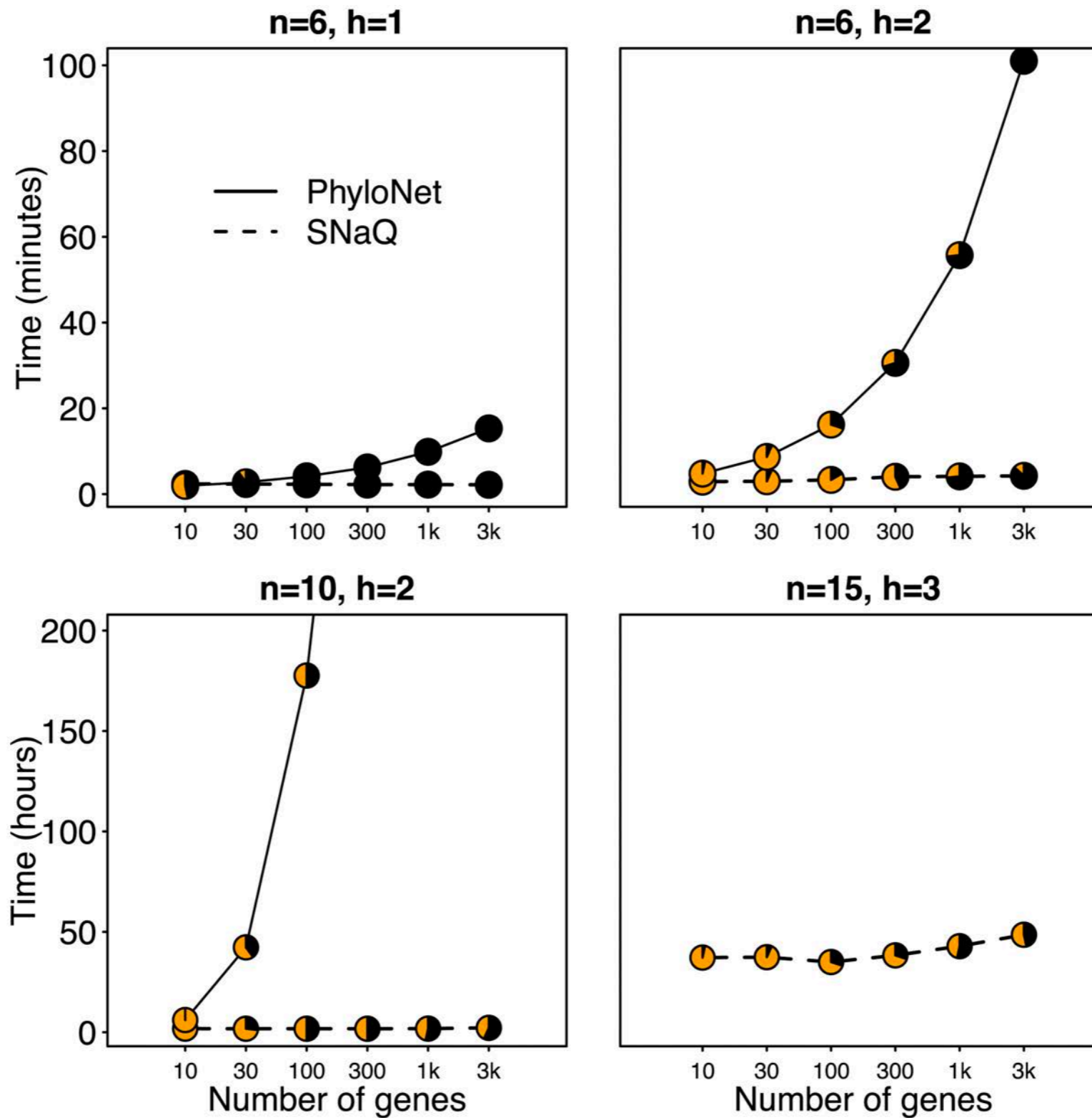
**Estimate
explicit
network
under the
coalescent**

**Hybrid
detection
+
Network
estimation**

Network challenges

- Scalability
- Identifiability
- Network comparison

Scalability



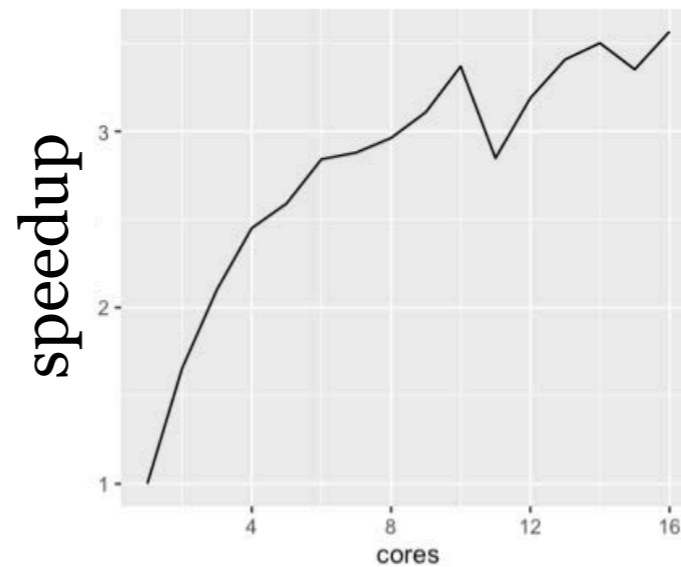
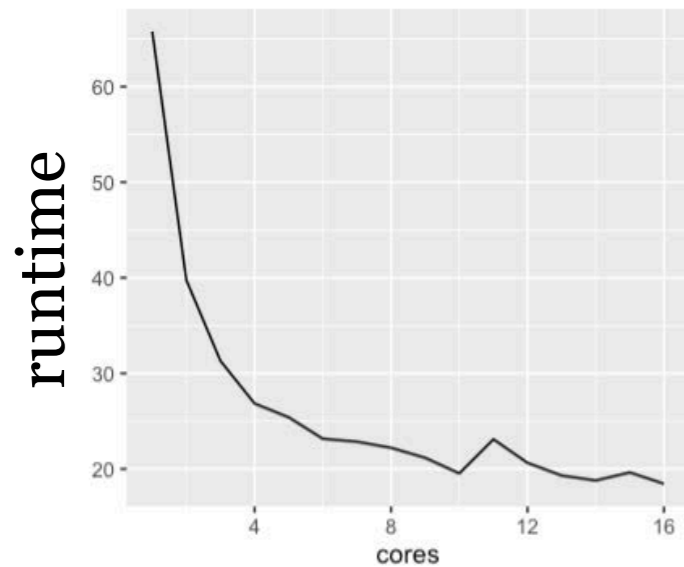
(Solís-Lemus, Ané, 2016, PLoS Genetics)

SNaQ is faster, but is it fast?

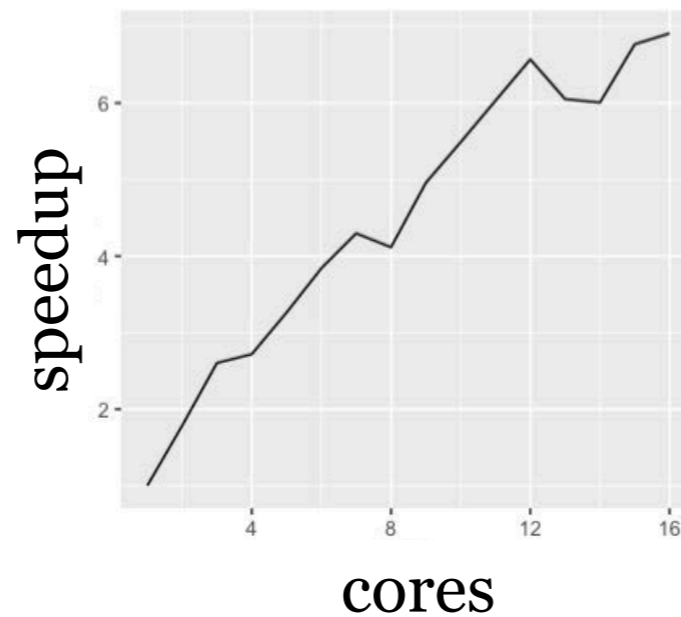
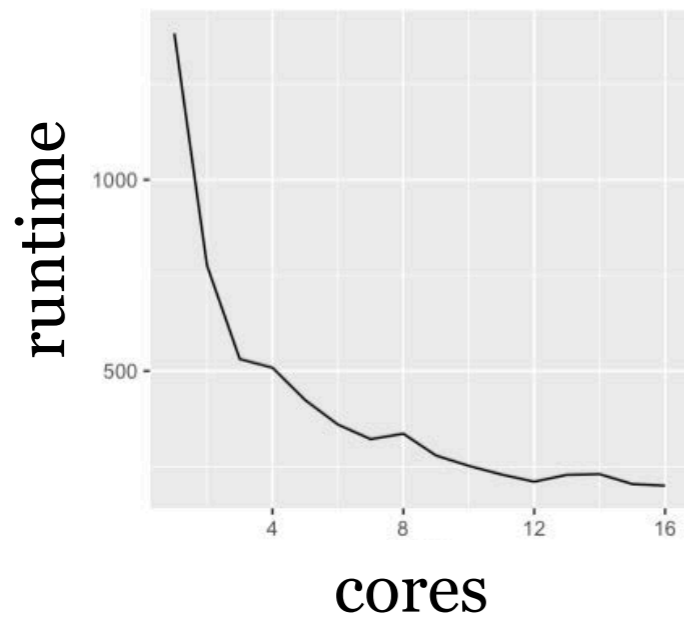


Tyler Chafin

n=10



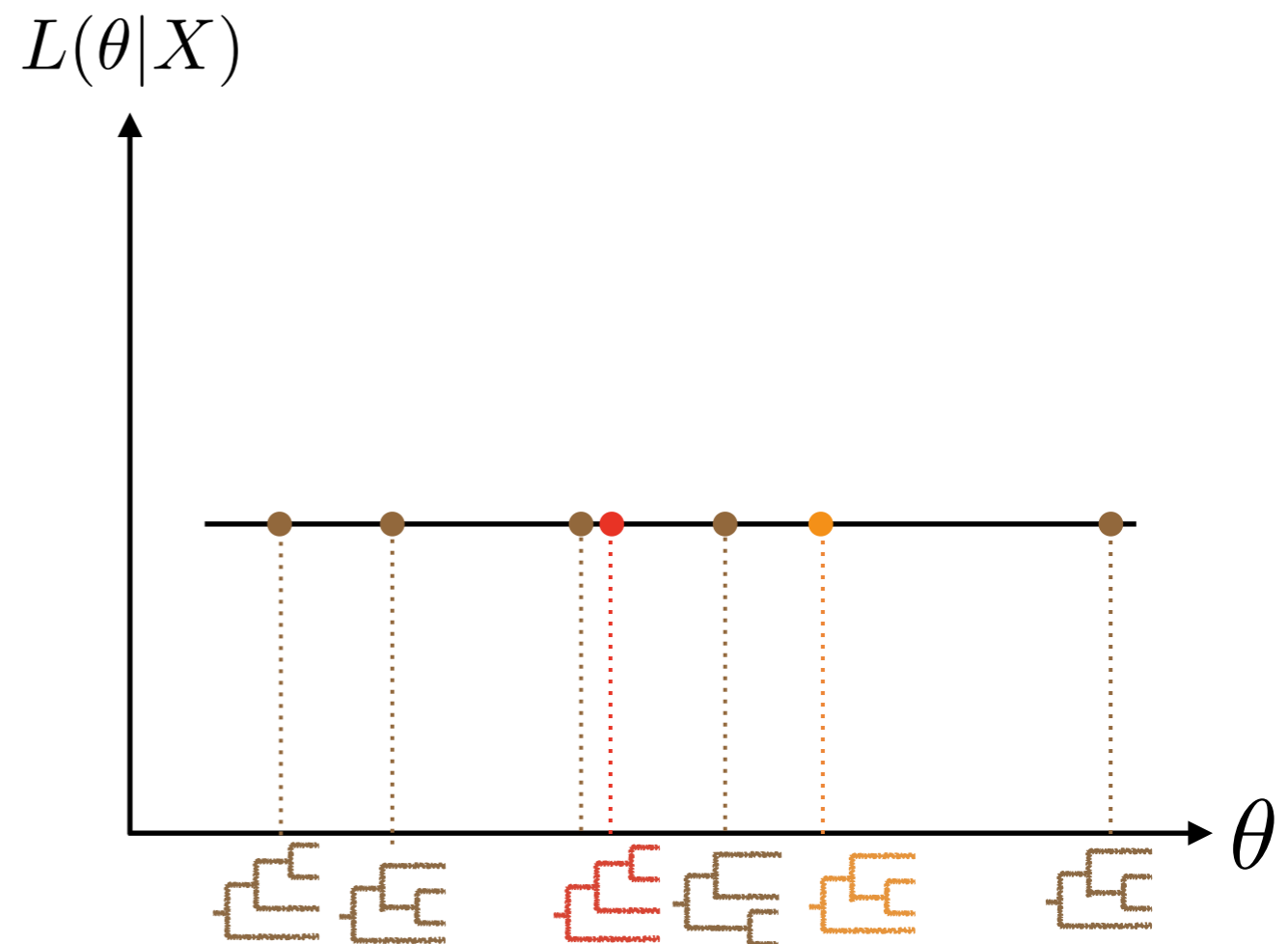
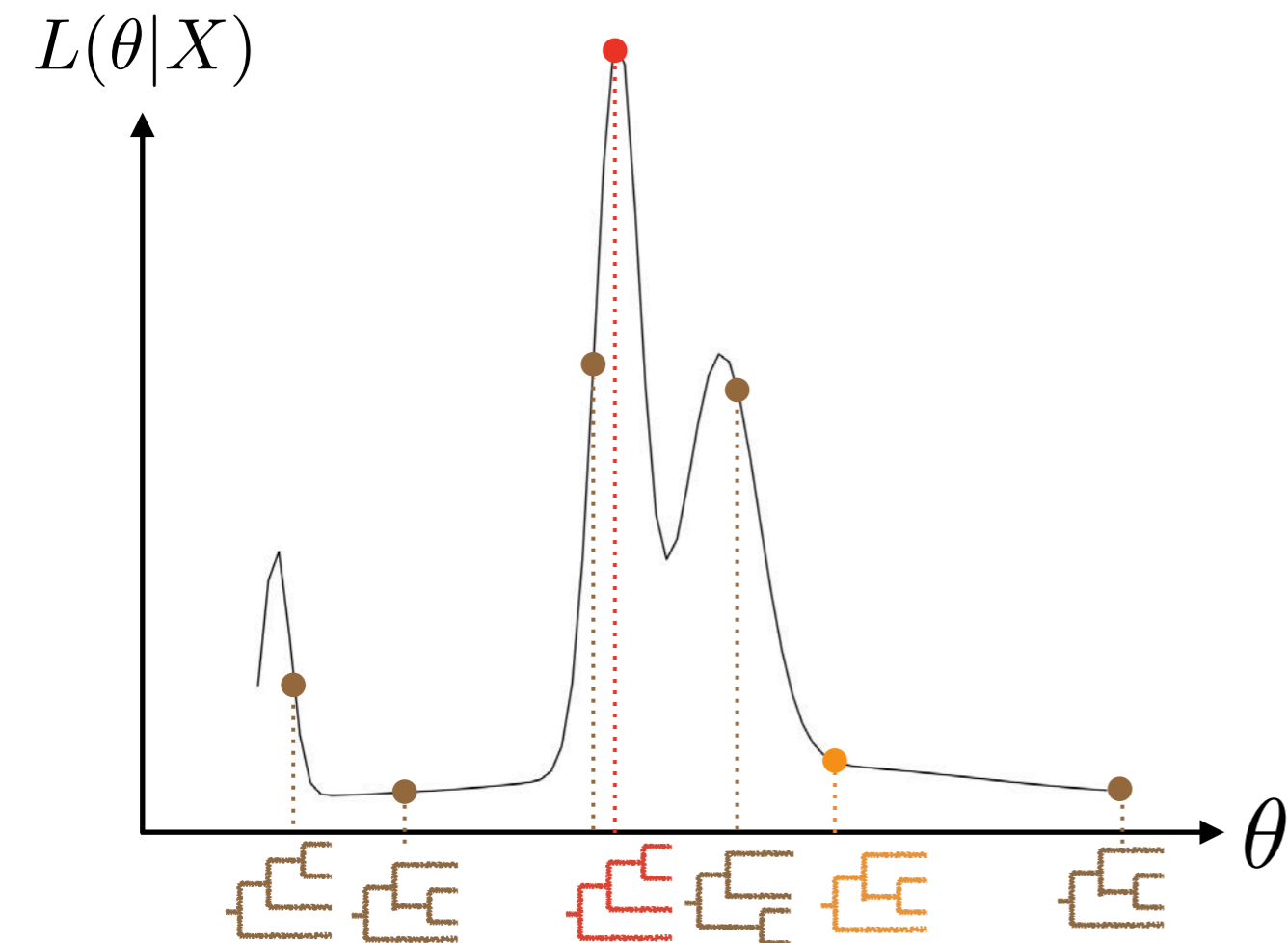
n=20



- Parallel quartet likelihood computation
- Weights to quartets: deviations from expected CFs
- Sampling of quartets without biasing inference

SNaQ 2.0
coming up soon!

Identifiability

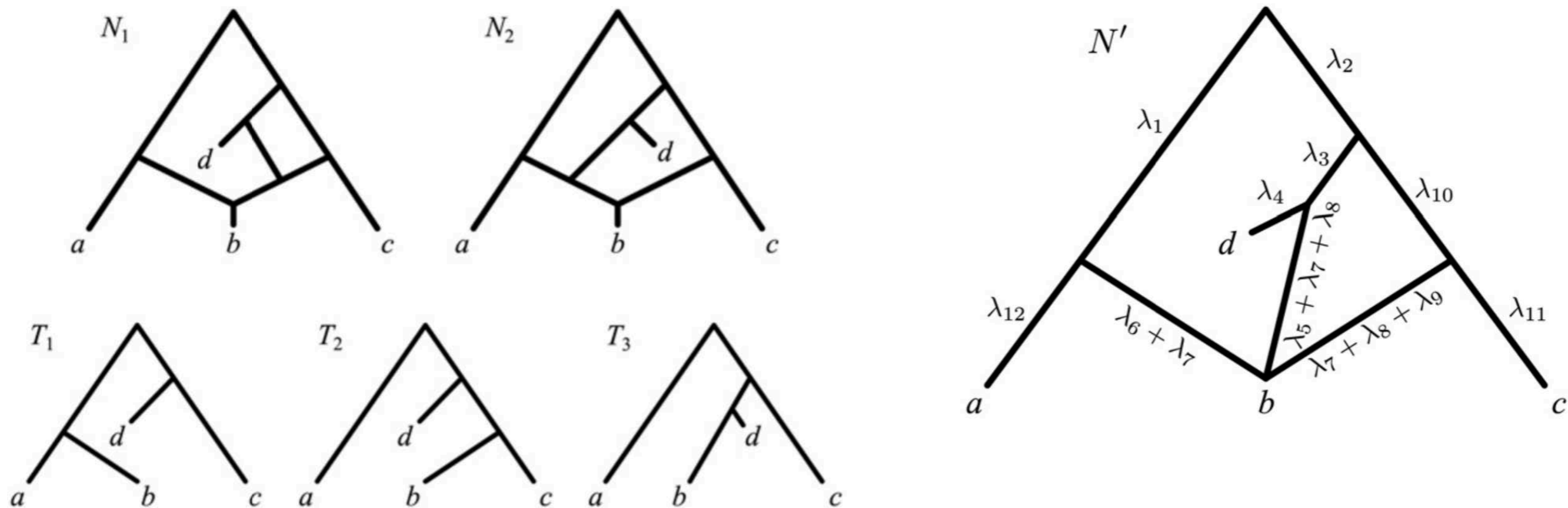


RESEARCH ARTICLE

Reconstructible Phylogenetic Networks: Do Not Distinguish the Indistinguishable

Fabio Pardi^{1,3*}, Celine Scornavacca^{2,3}

1 Laboratoire d'Informatique, de Robotique et de Microélectronique de Montpellier (LIRMM, UMR 5506) CNRS, Université de Montpellier, France, **2** Institut des Sciences de l'Evolution de Montpellier (ISE-M, UMR 5554) CNRS, IRD, Université de Montpellier, France, **3** Institut de Biologie Computationnelle, Montpellier, France

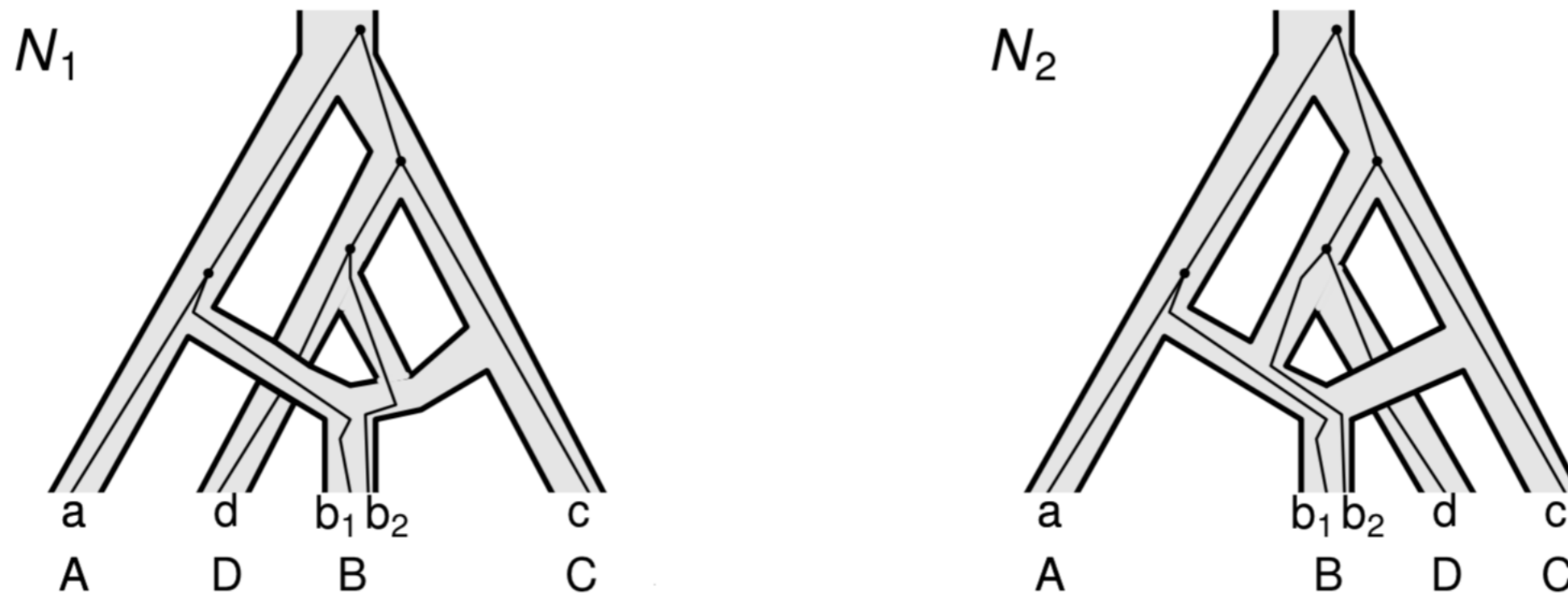


Undistinguishable with the “displayed trees” criterion

Solution: Canonical network (“unzipped”)

Displayed Trees Do Not Determine Distinguishability Under the Network Multispecies Coalescent

Sha Zhu¹, James H. Degnan²



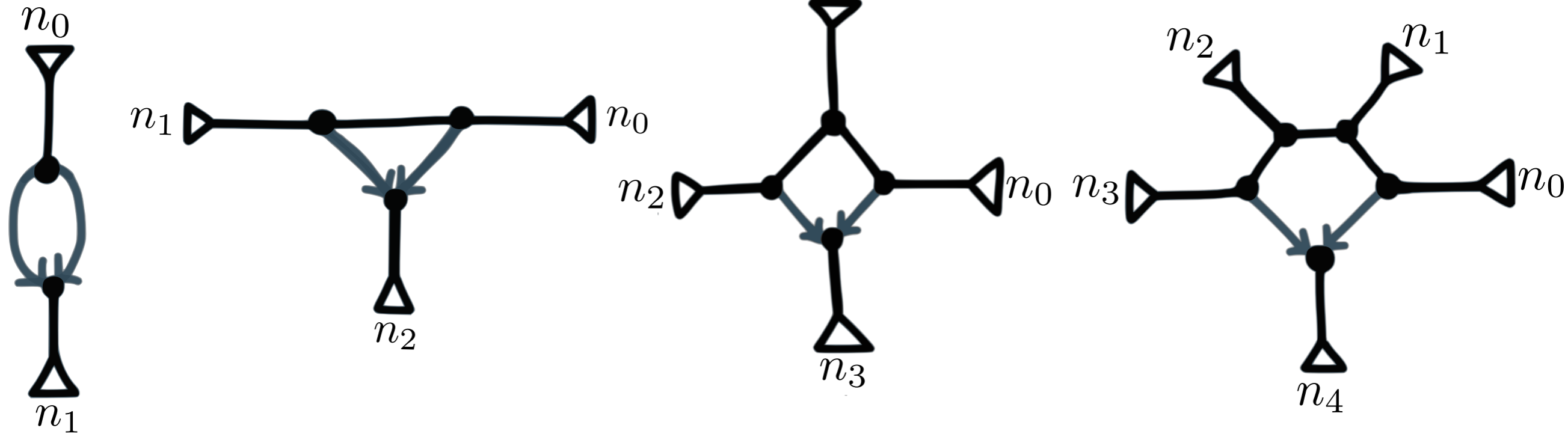
Distinguishable under the MSC

RESEARCH ARTICLE

Inferring Phylogenetic Networks with Maximum Pseudolikelihood under Incomplete Lineage Sorting

Claudia Solís-Lemus^{1*}, Cécile Ané^{1,2}

Can we detect the presence of hybridization in level-1 networks?



No

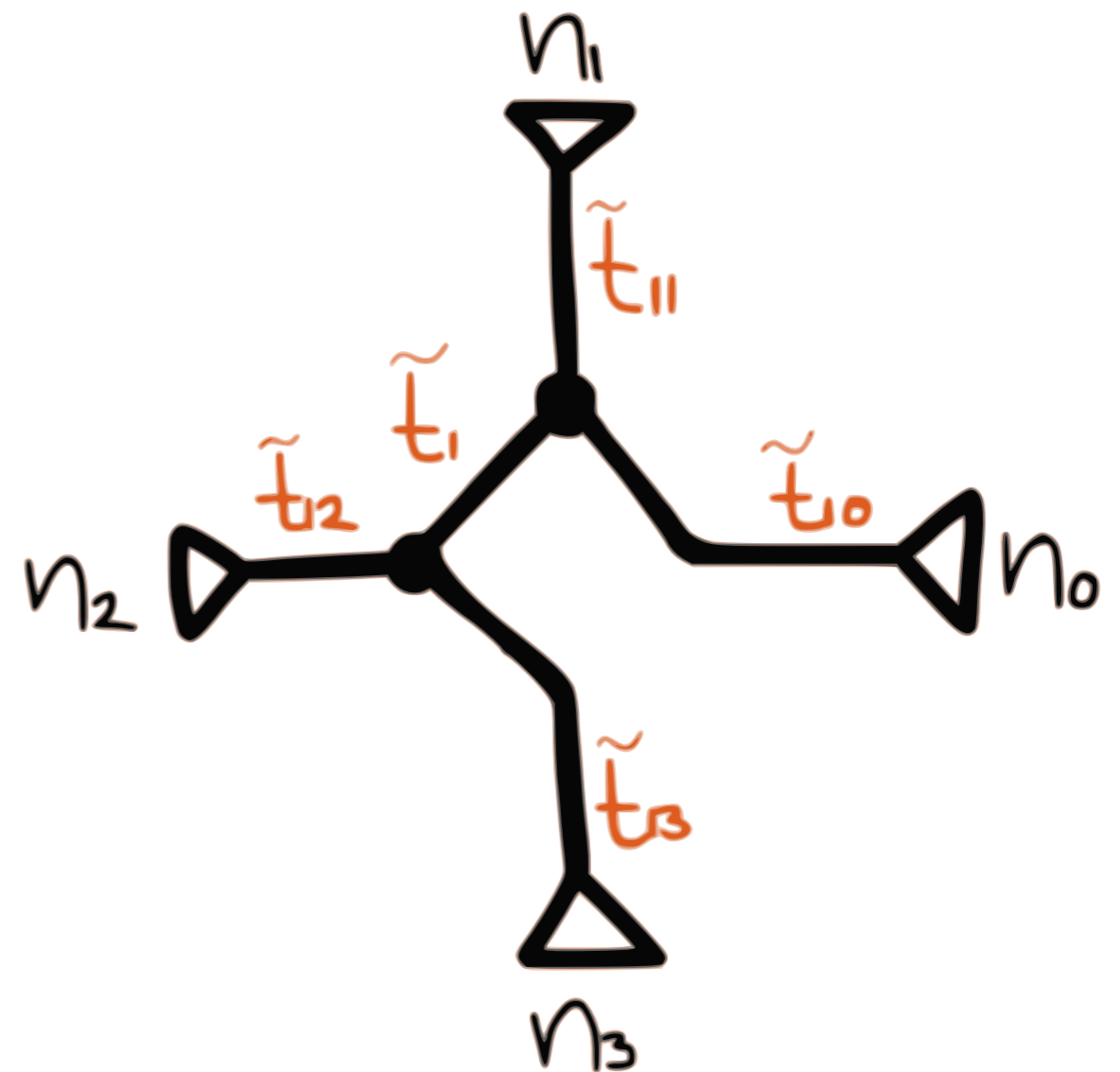
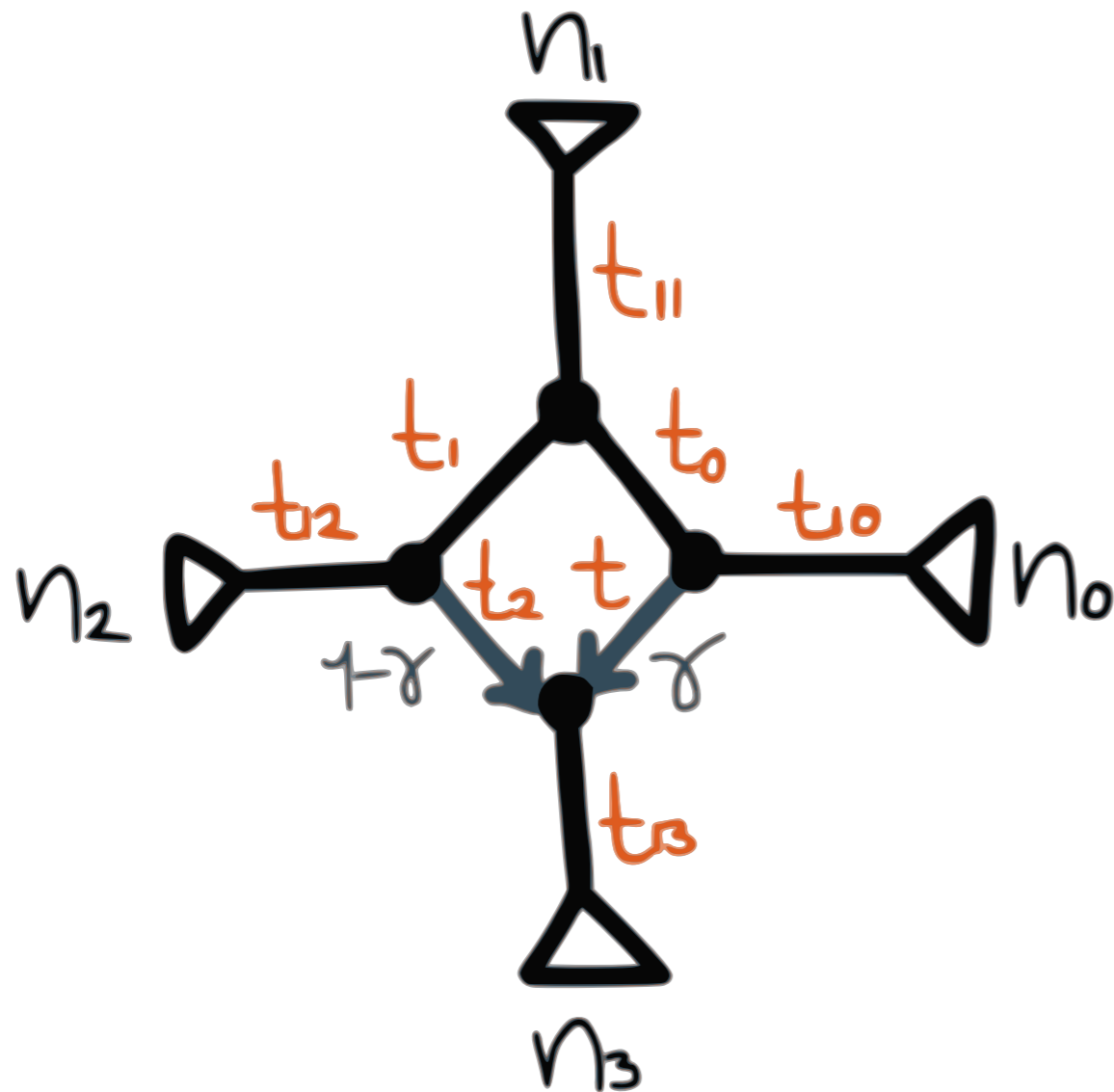
Yes
 $(n_i, n_j \geq 2)$

Yes
 $(n_i \geq 2)$

Yes

Generic Identifiability $t_i \in (0, \infty), \gamma \in (0, 1)$

Idea of proof of identifiability: hybridization



System of equations

System of equations

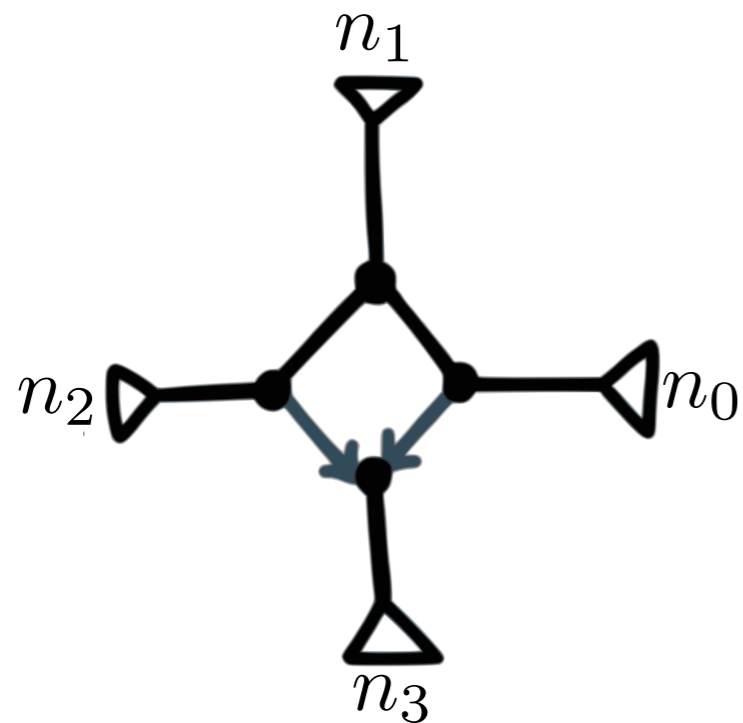
$\{\text{CF}_{\text{network}}\}$

(Solís-Lemus & Ané, 2016;
Solís-Lemus et al, 2020)

$\{\text{CF}_{\text{tree}}\}$

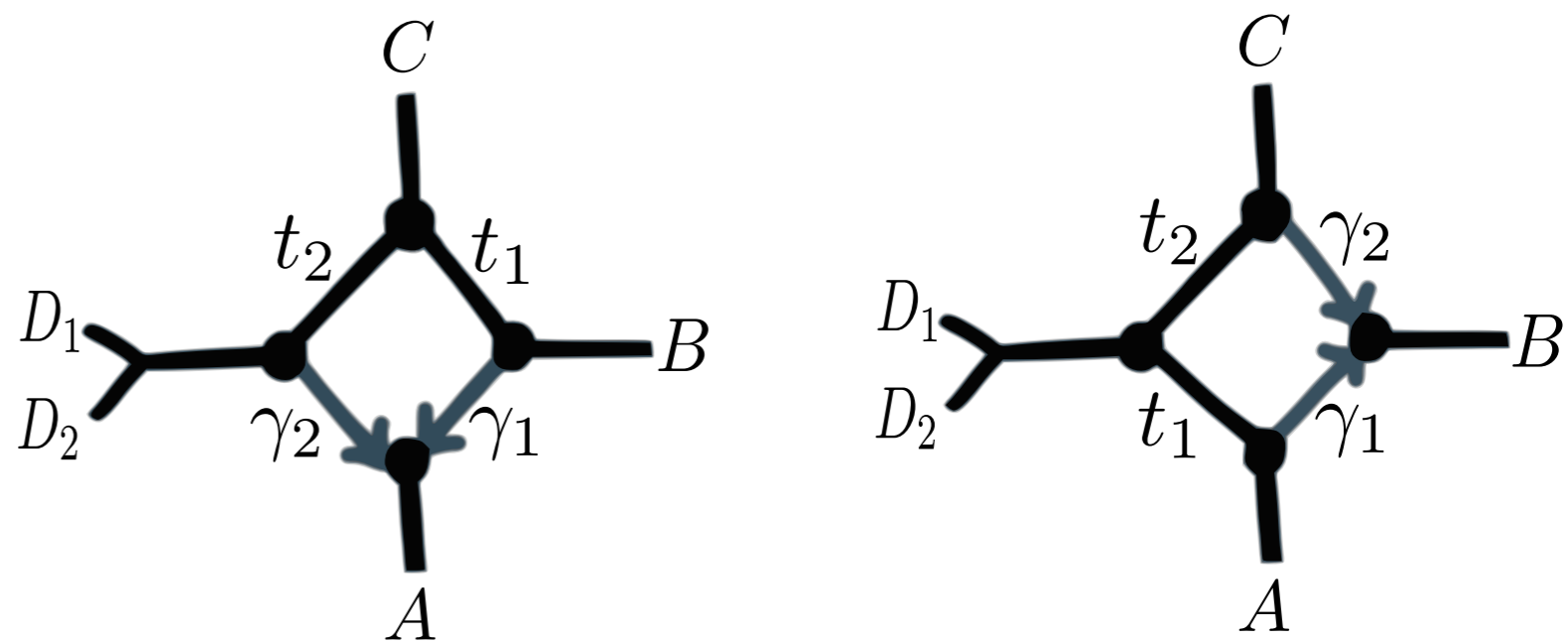
Can we detect the presence of hybridization in level-1 networks?

In theory



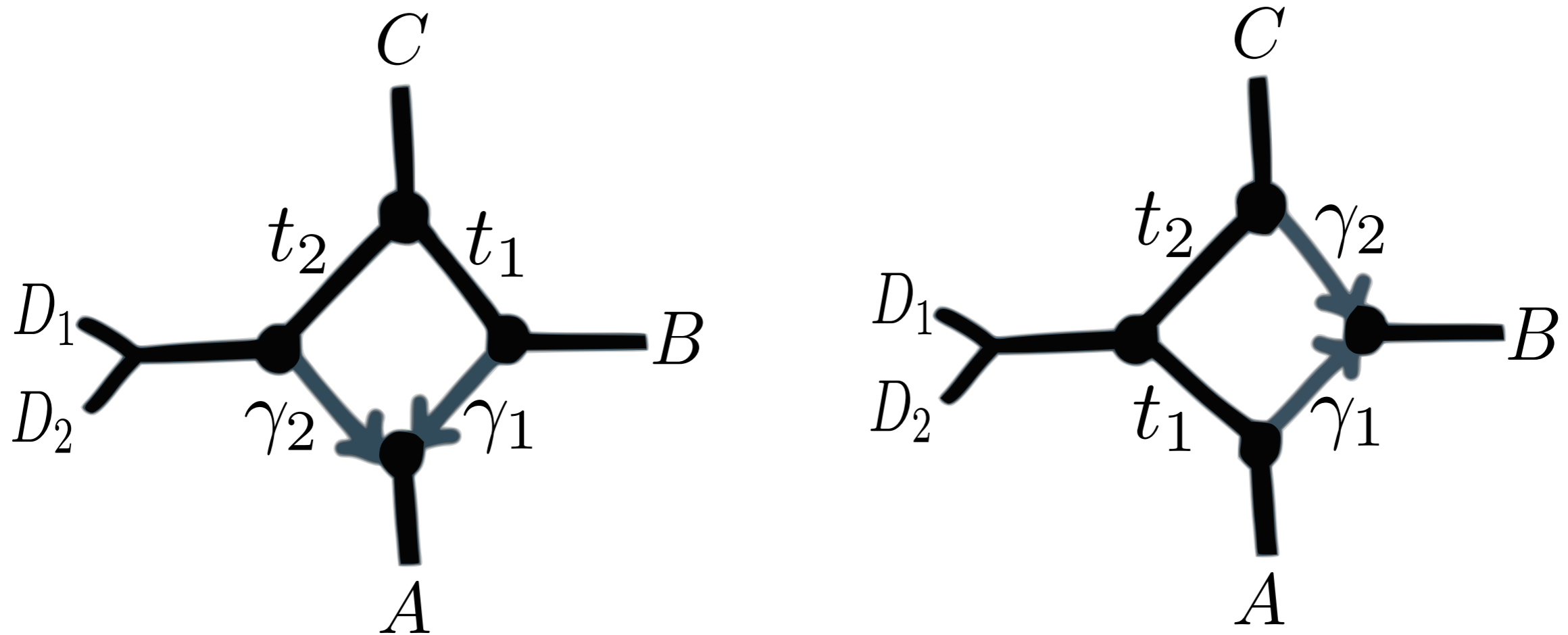
Yes
($n_i \geq 2$)

In practice



Sometimes

In practice: flat pseudolikelihood



(S.-L., Ané, 2016, PLoS Genetics)



Diamond identifiability

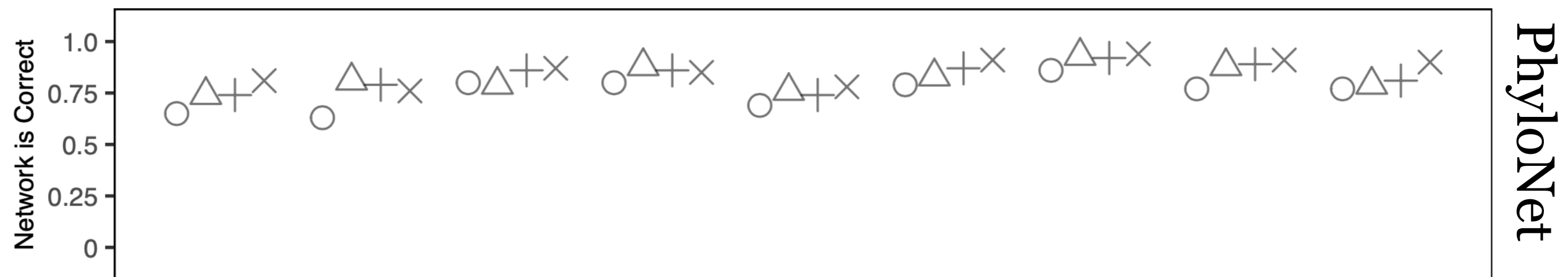


George Tiley

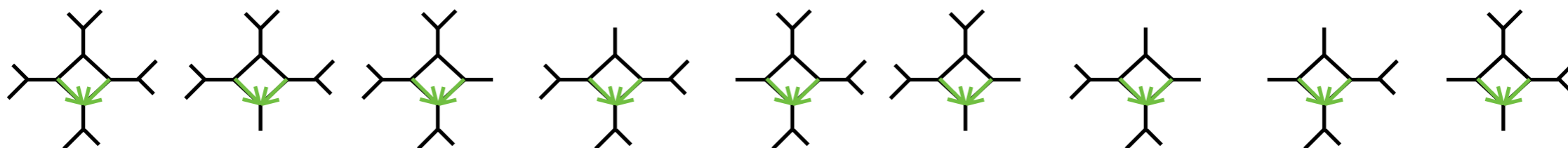
nTrees ○ 100 △ 500 + 1000 × 5000



SnpAQ

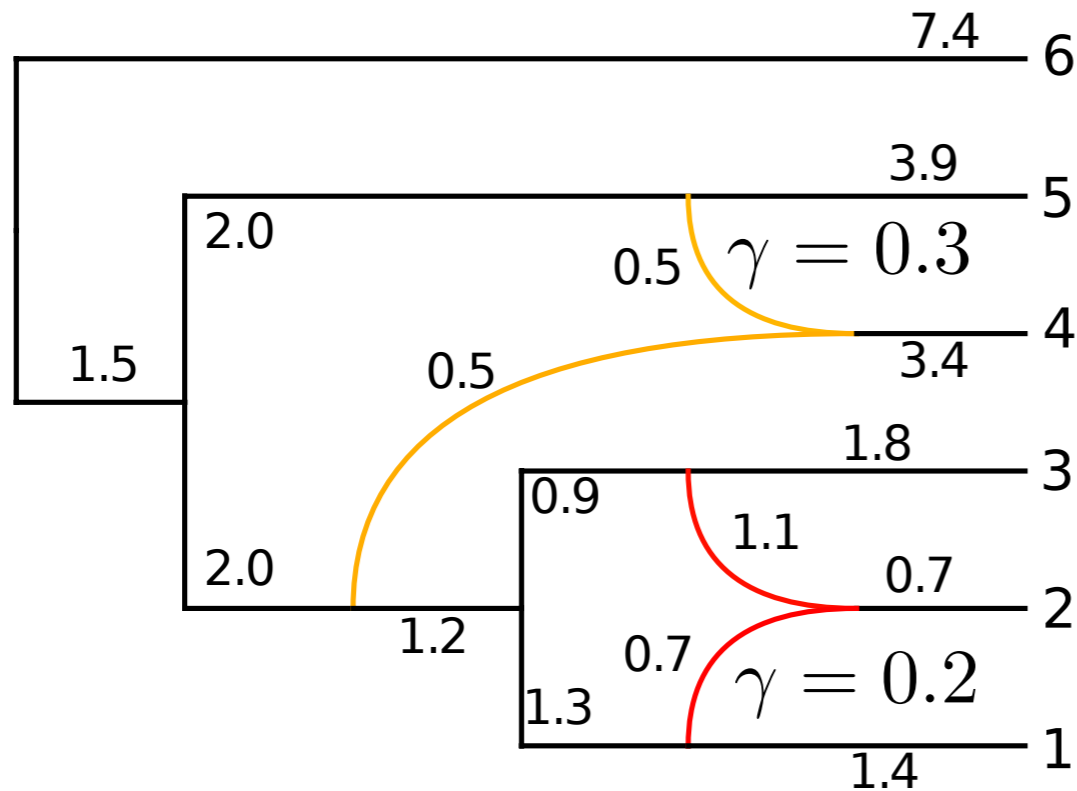


PhyloNet

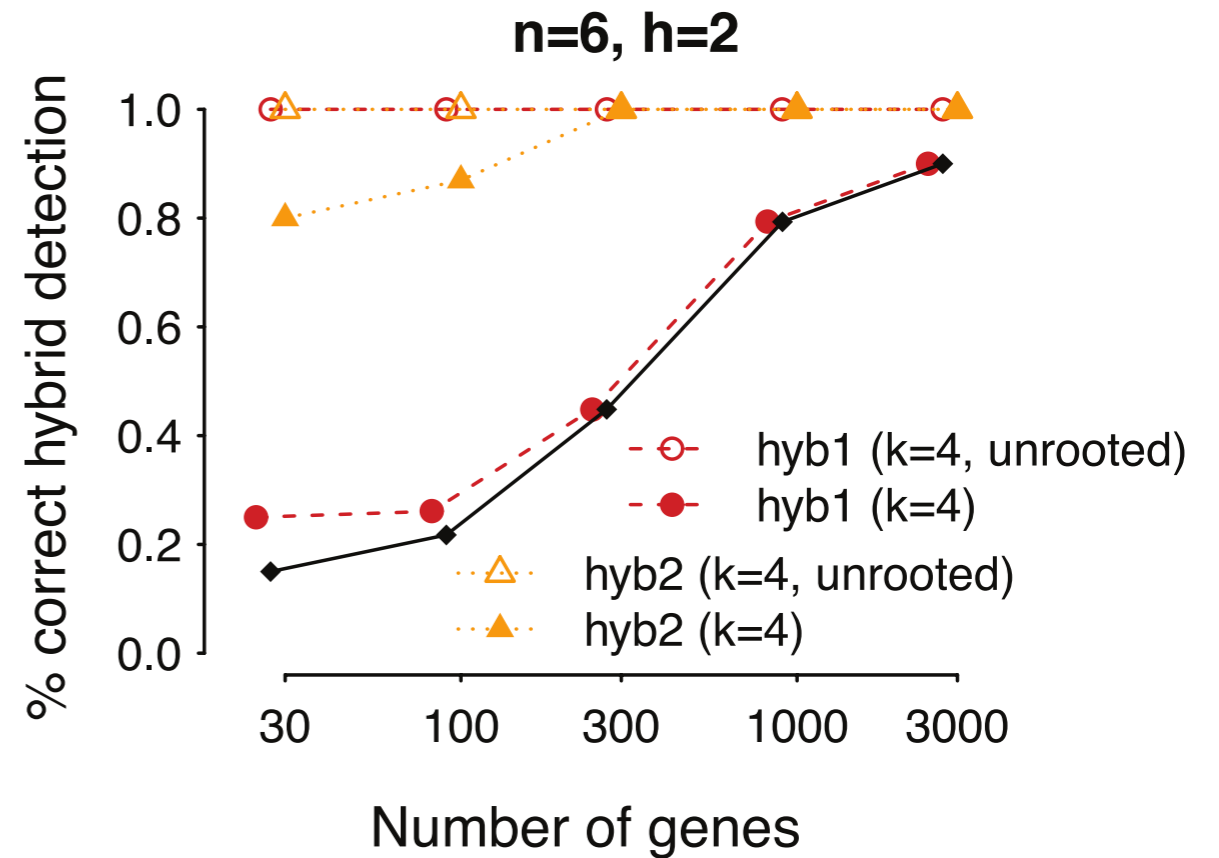


Identifiability matters: SNaQ performance

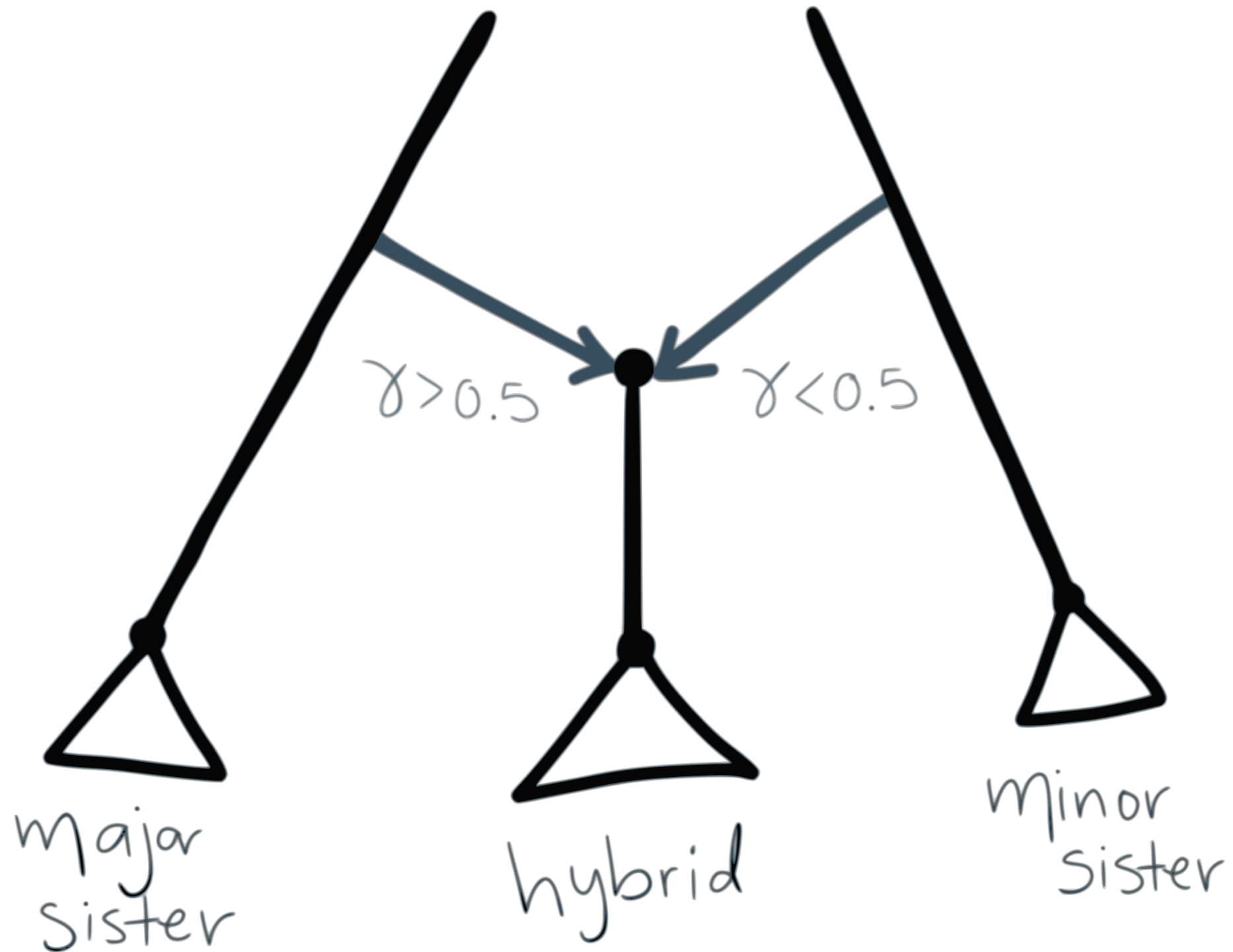
Good diamond



Bad diamond

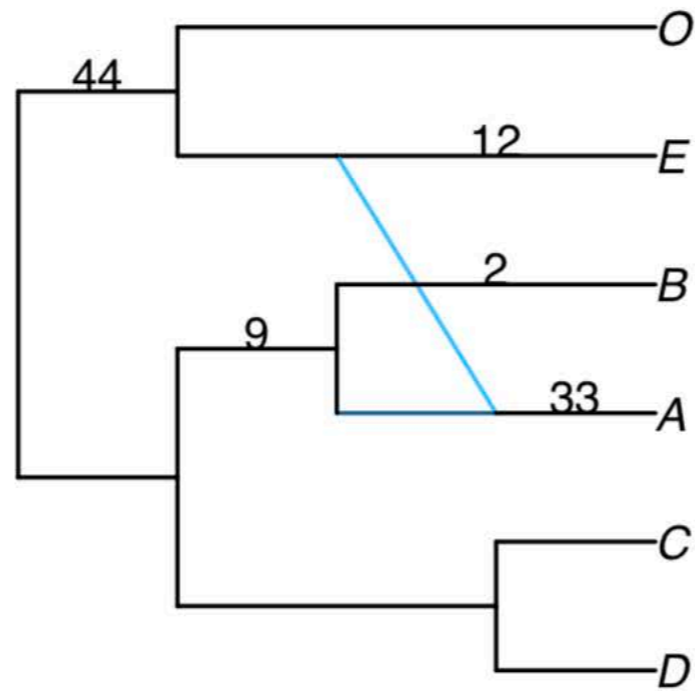
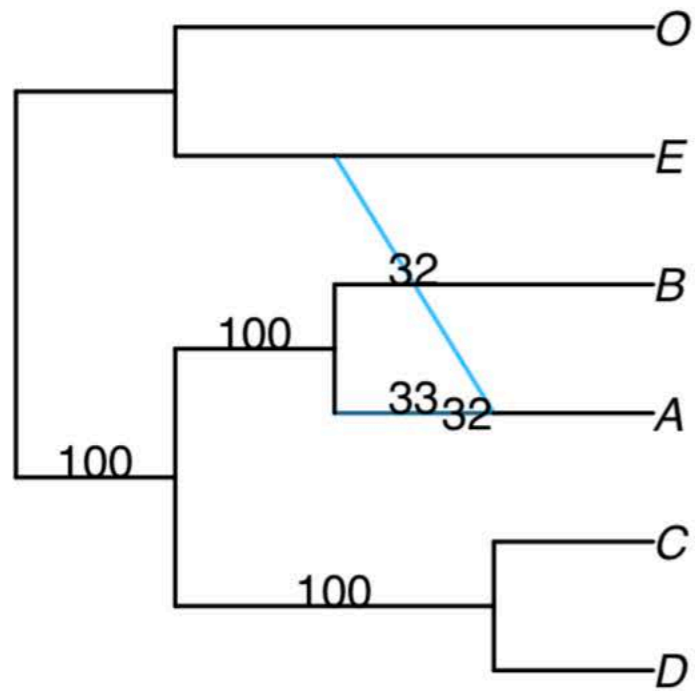


Network Comparison

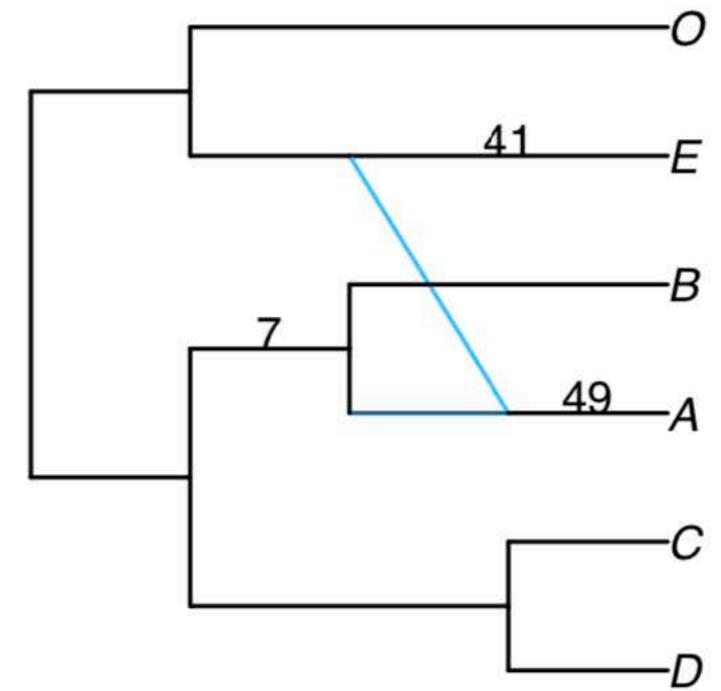


(S.-L. et al, 2017, MBE)

Network summary



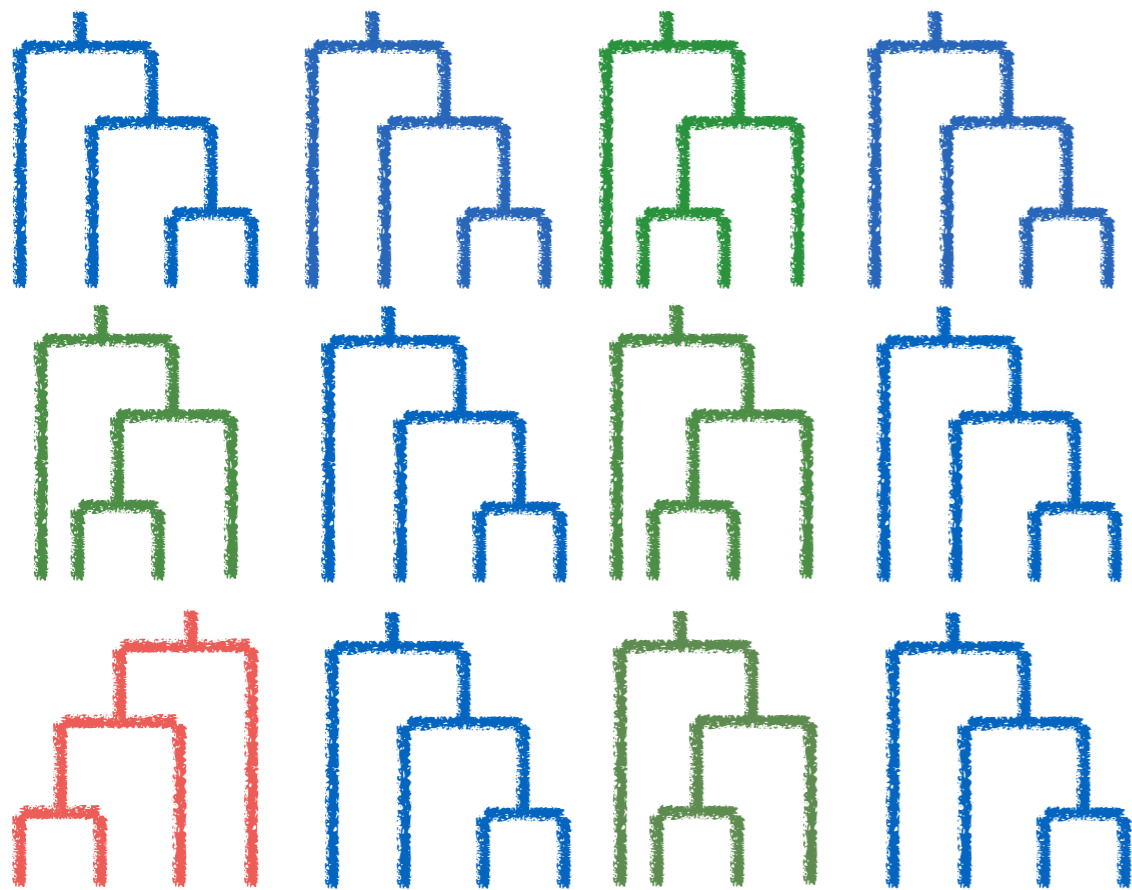
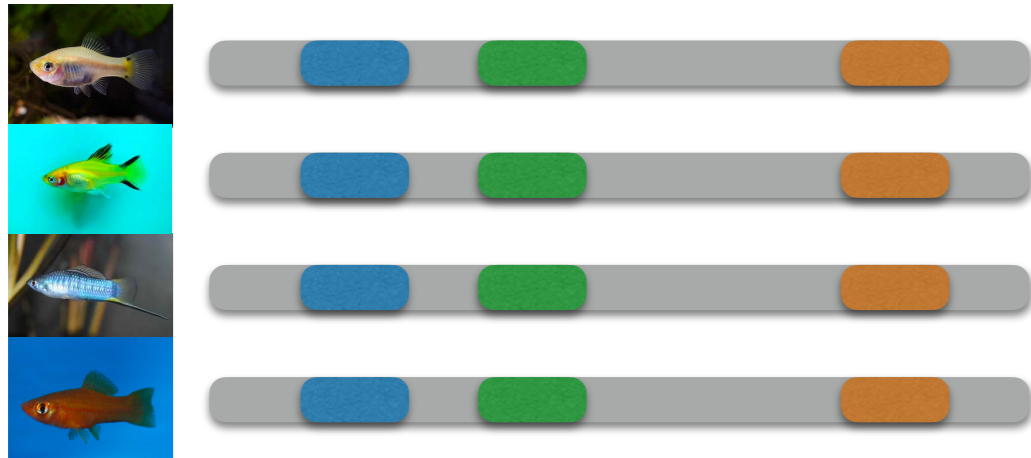
Hybrid
clades



Minor
sister
clades

When?

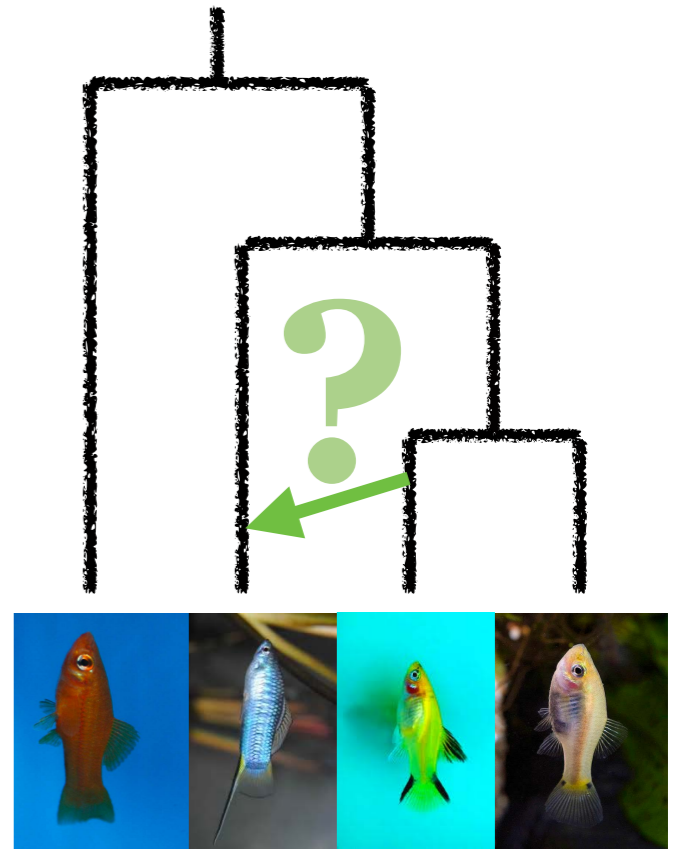
Phylogenetic network



Data

Goodness-of-fit test

Hypothesis test:
Is a tree a good fit?



<https://github.com/nstenz/TICR>

(Stenz et al, 2015, Syst Bio)

Practical advice

- Do multiple runs
- Do bootstrap
- Check the .networks output file (especially if hybridization conflicts with outgroup)
 - Choice of outgroup important!
- Interpretation of ghost lineages
- What is the quality of my input data (gene trees/CFs)?
- Run SNaQ sequentially: $h=0, h=1, h=2, \dots$

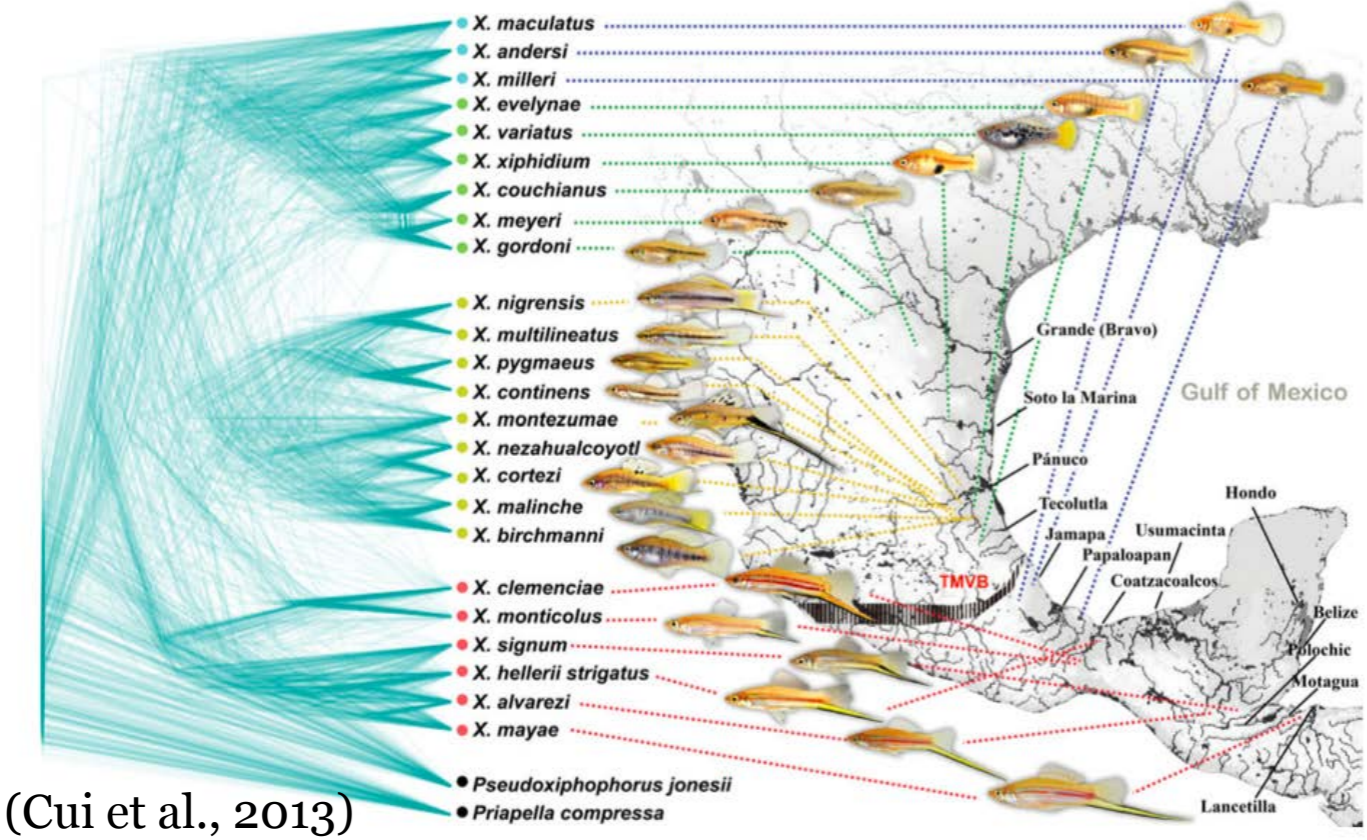
Practical advice

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- Do bootstrap
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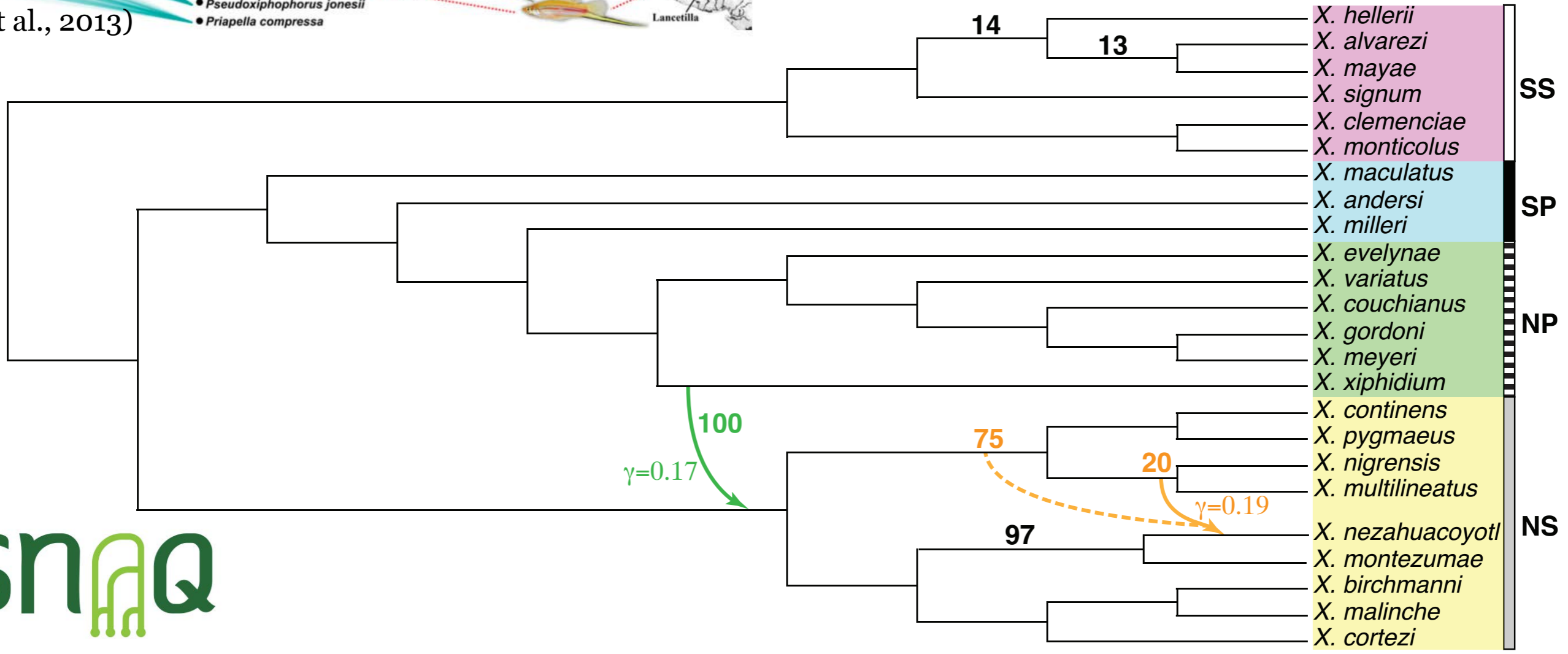
When to stop?
(Cai and Ané, 2020)

1183 genes, 24 swordtails and platyfish

Xiphophorus fish data



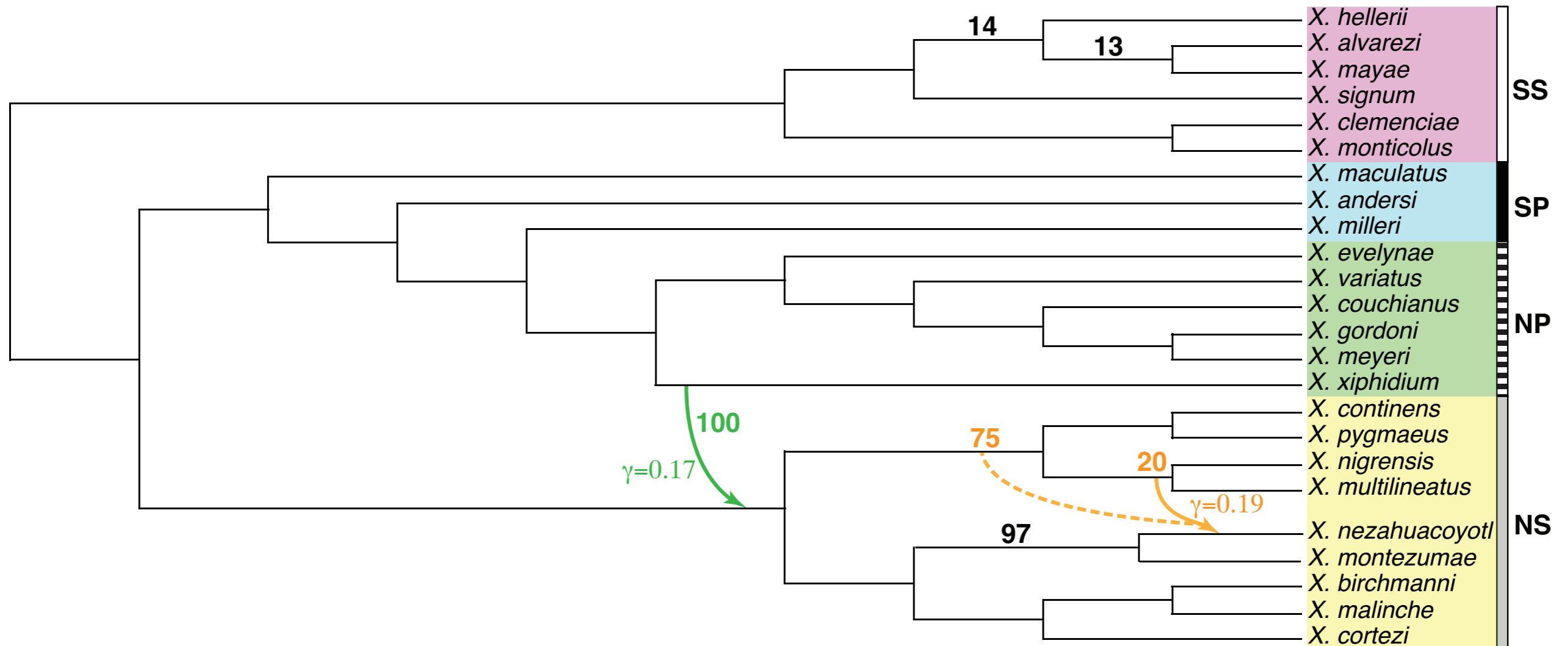
(Cui et al., 2013)



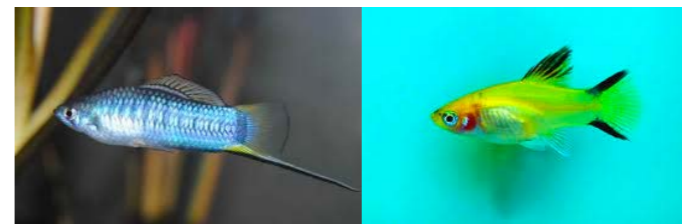
(Solís-Lemus, Ané, 2016, PLoS Genetics)

Part II

I have the network, now what?



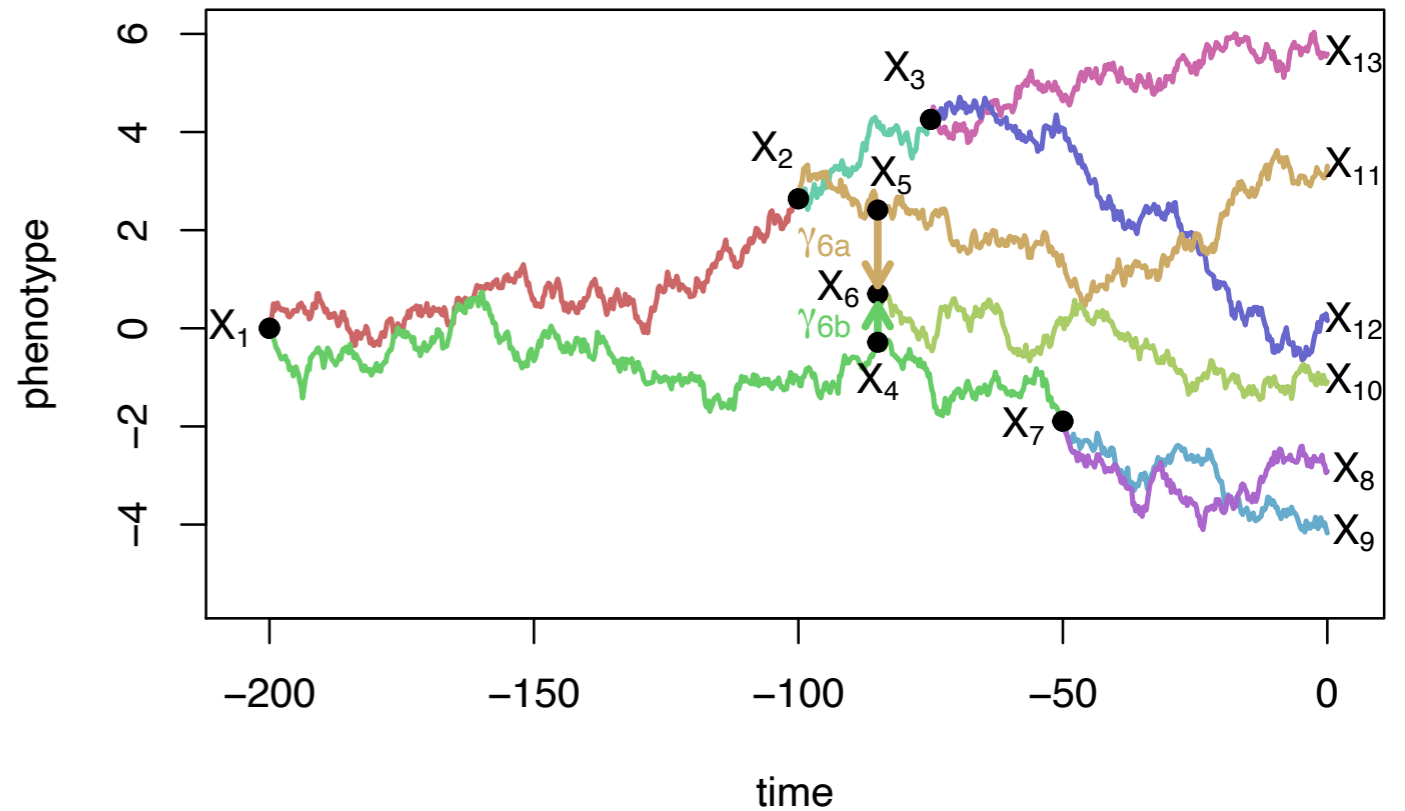
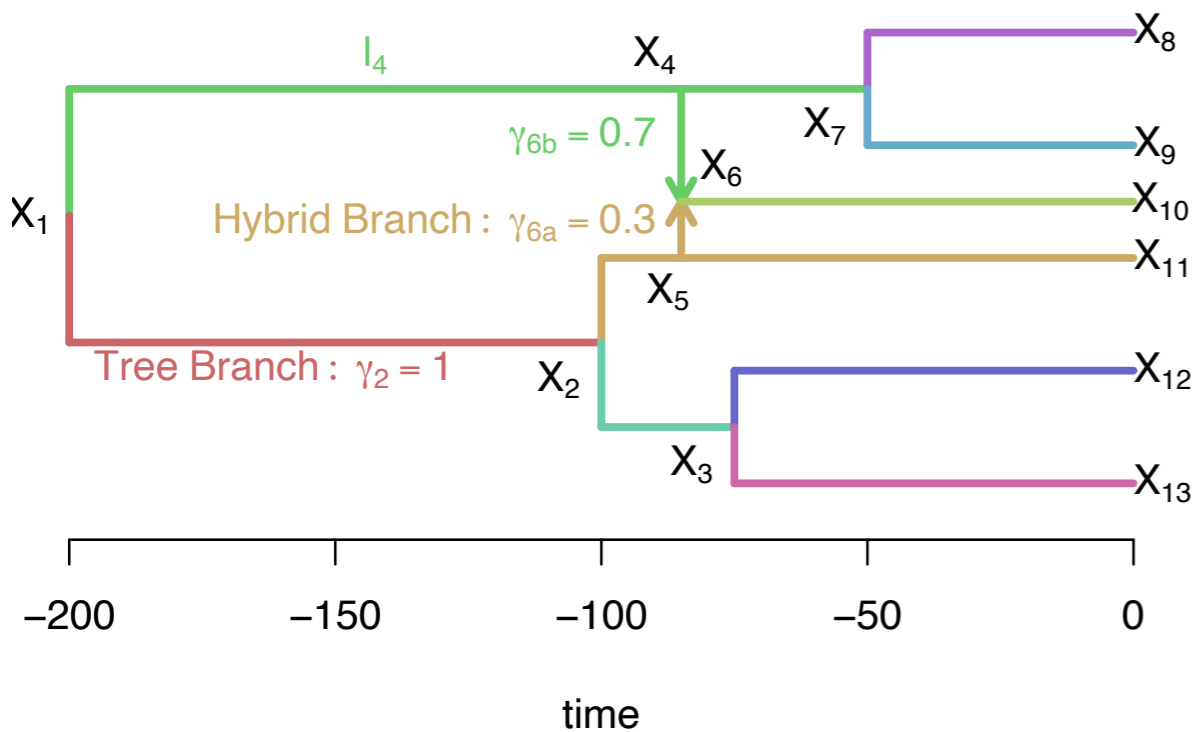
- Sword index
- Female preference



(Cui et al., 2013)

(Solís-Lemus, Ané, 2016, PLoS Genetics)

Trait models of evolution in networks



Brownian Motion
+ weighted
average in hybrid

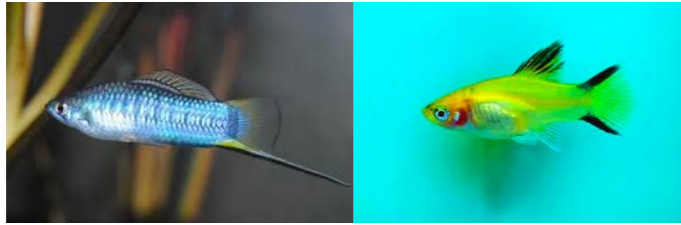
$$X_h = \gamma_1 X_{p_1} + \gamma_2 X_{p_2}$$

(Bastide et al, 2018, Syst Bio)

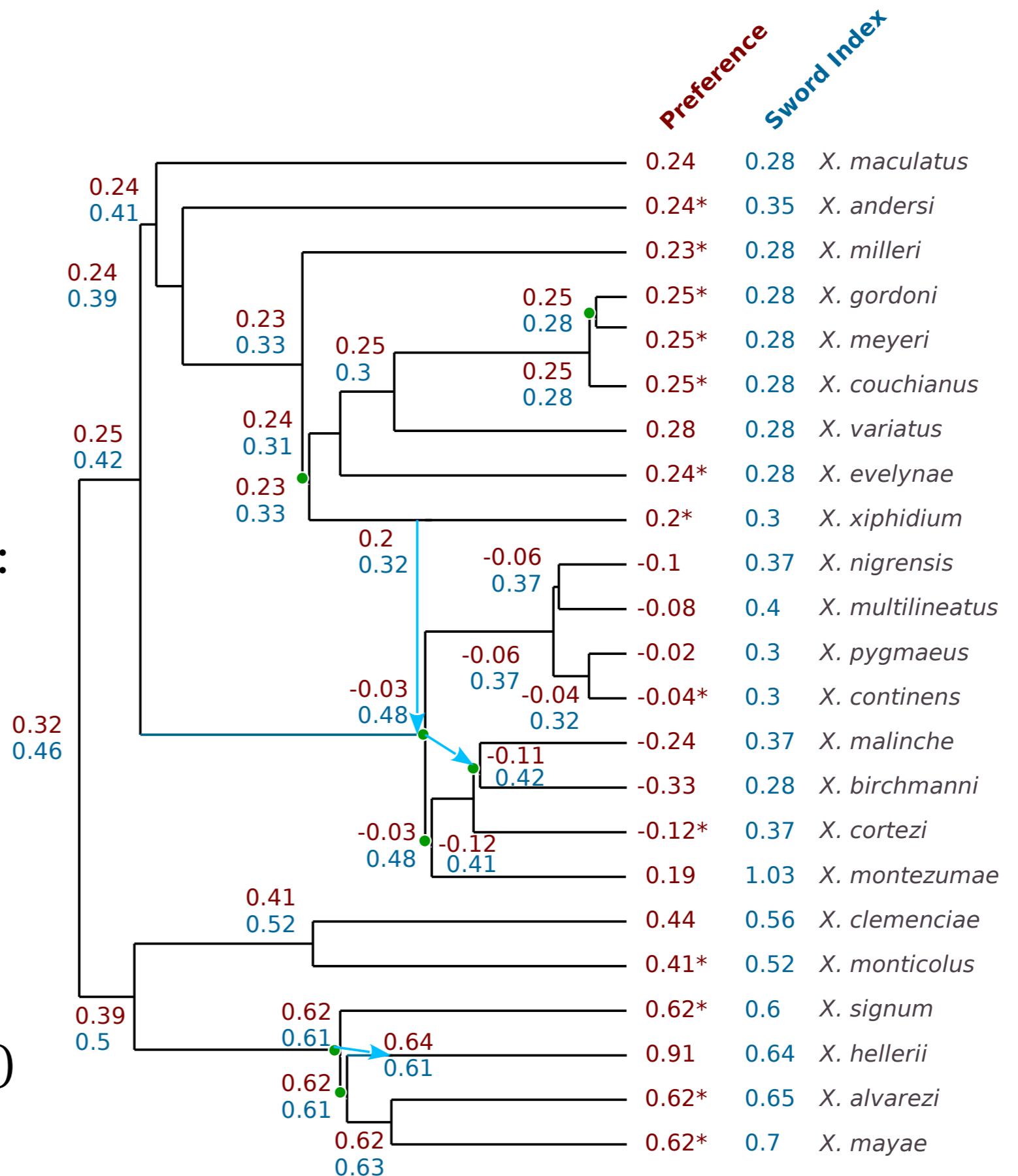
$$\mathbf{X} \sim N(X_{root}, \sigma^2 \mathbf{V})$$

- Phylogenetic signal
- Ancestral reconstruction
- Phylogenetic regression
- Phylogenetic ANOVA

- Sword index
- Female preference

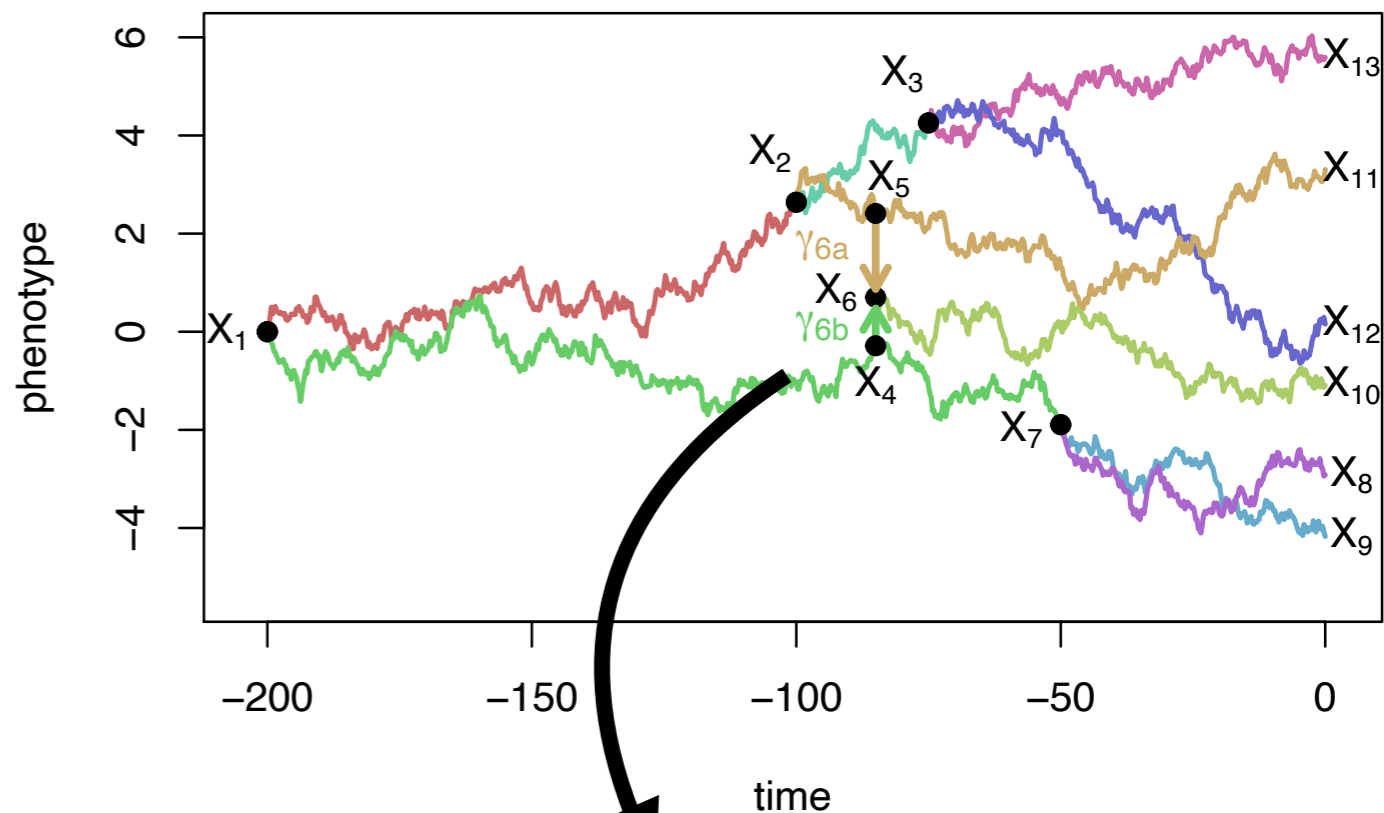
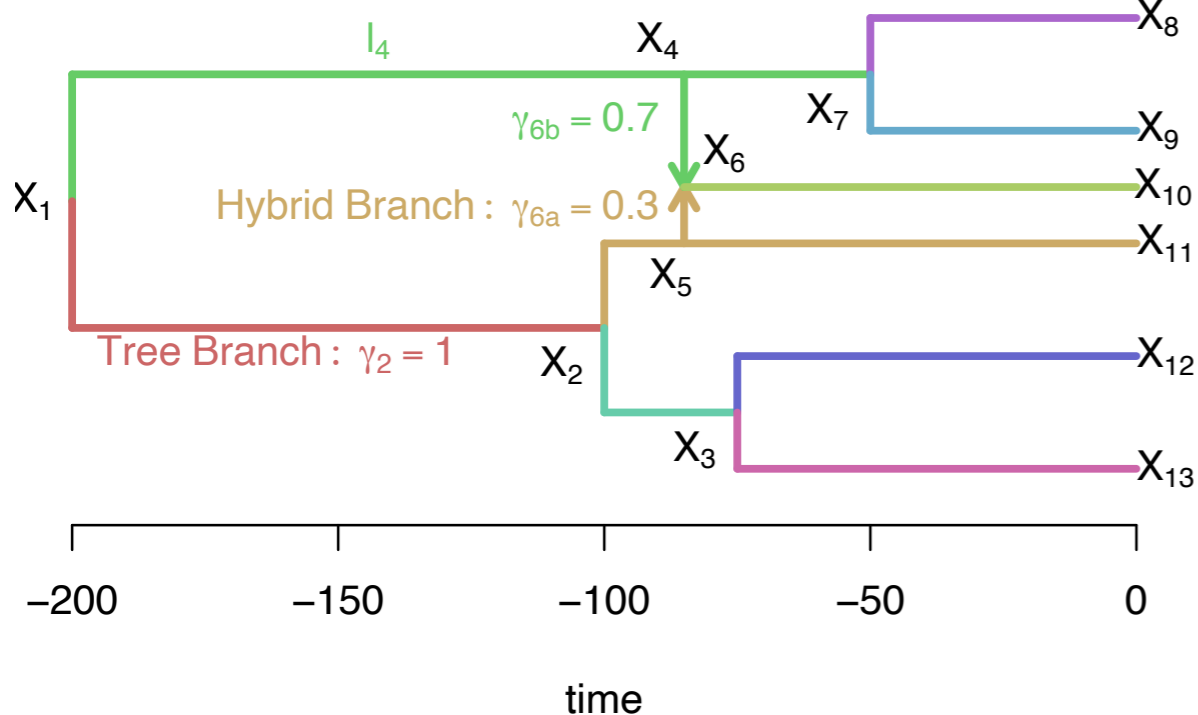


- **Ancestral reconstruction:**
common ancestor likely had sword
- **Phylogenetic regression:**
positive association between sword index and female preference
but not significant ($p = 0.106$)



Test for transgressive evolution

$$X_h = \gamma_1 X_{p_1} + \gamma_2 X_{p_2} + \Delta_h$$



$\Delta_h = 0$ No transgressive evolution

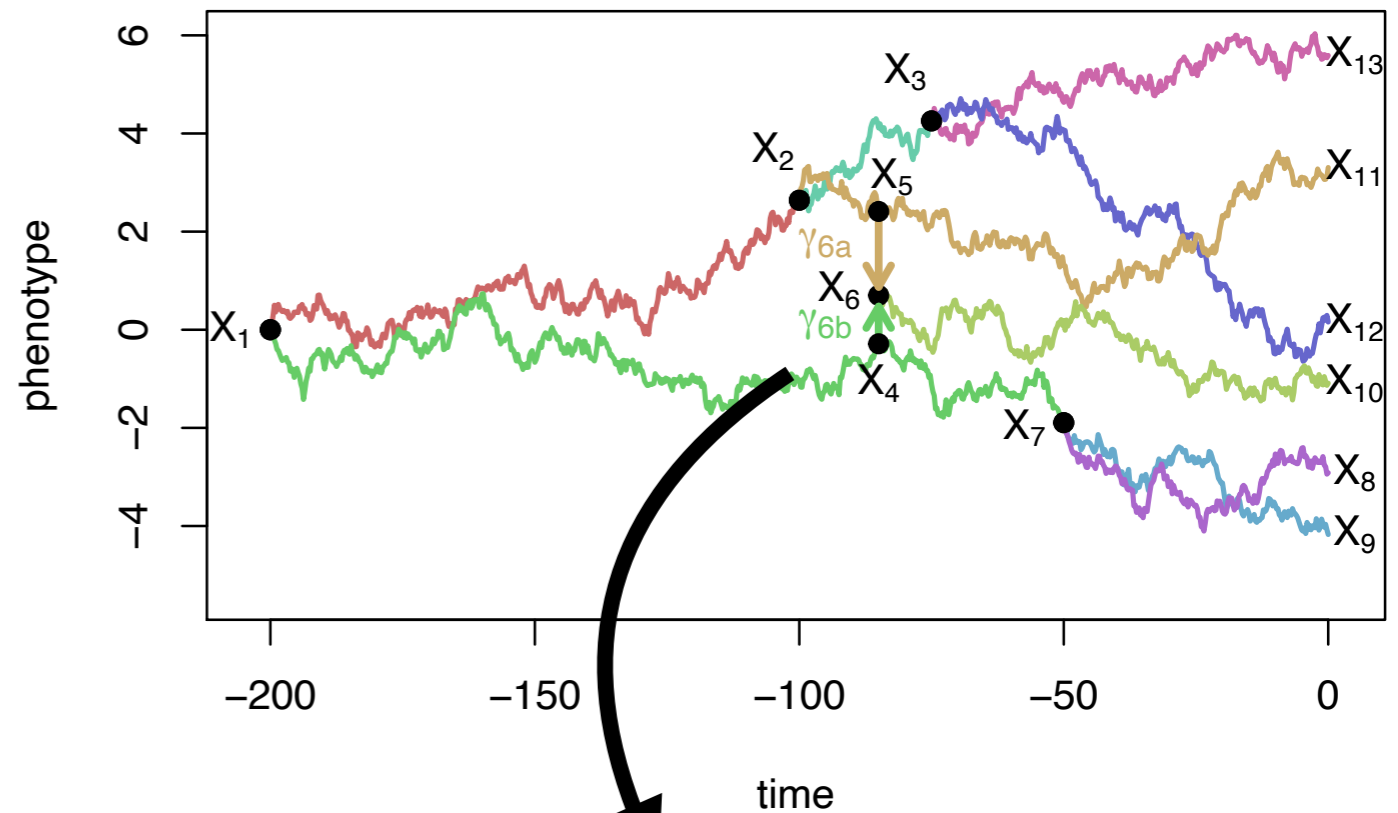
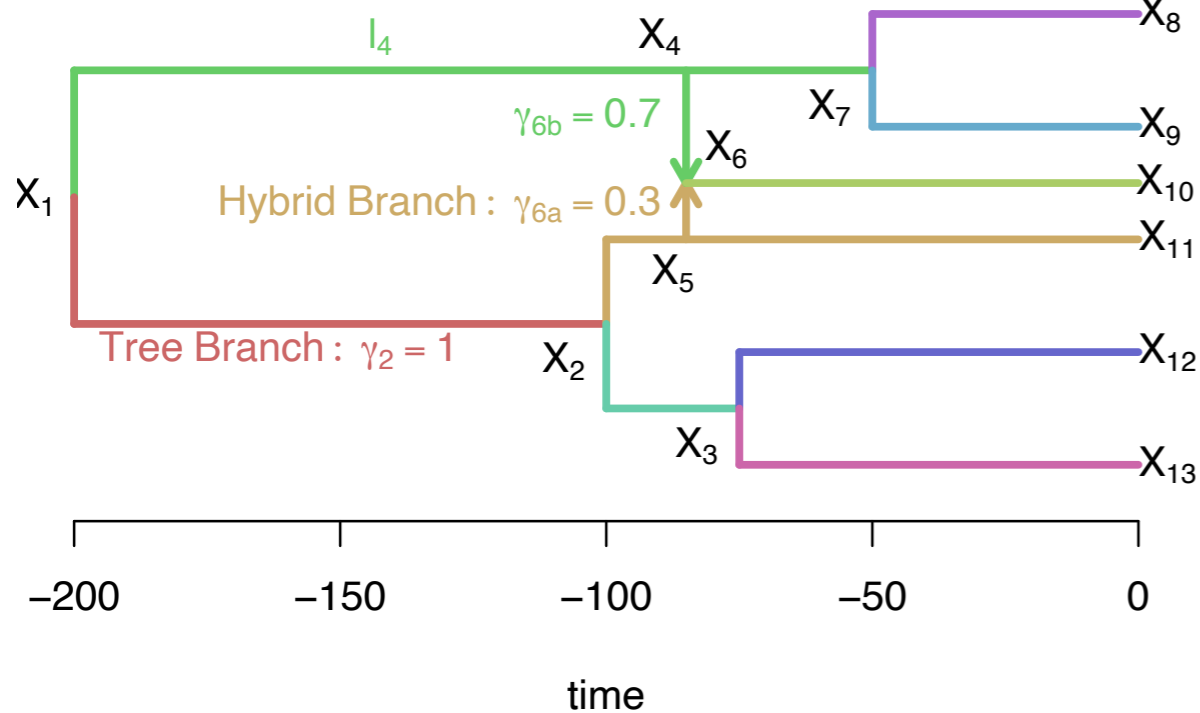
$\Delta_h = \Delta$ Single-effect transgressive evolution

Δ_h Multi-effect transgressive evolution

F tests

Hybrid value:
shift from
parents range

Test for transgressive evolution



- Sword index: $p=0.55$
- Female preference: $p=0.0064$

Hybrid value:
shift from
parents range

PhyloNetworks: analysis for phylogenetic networks

build passing docs stable docs dev codecov 81% coverage 67%

Overview

Get your stickers!



PhyloNetworks is a [Julia](#) package with utilities to:

- read / write phylogenetic trees and networks, in (extended) Newick format. Networks are considered explicit: nodes represent ancestral species. They can be rooted or unrooted.
- manipulate networks: re-root, prune taxa, remove hybrid edges, extract the major tree from a network, extract displayed networks / trees
- compare networks / trees with dissimilarity measures (Robinson-Foulds distance on trees)
- summarize samples of bootstrap networks (or trees) with edge and node support
- estimate species networks from multilocus data (see below)
- phylogenetic comparative methods for continuous trait evolution on species networks / trees



GitHub

- Step-by-step tutorial
- Online documentation
- Google user group



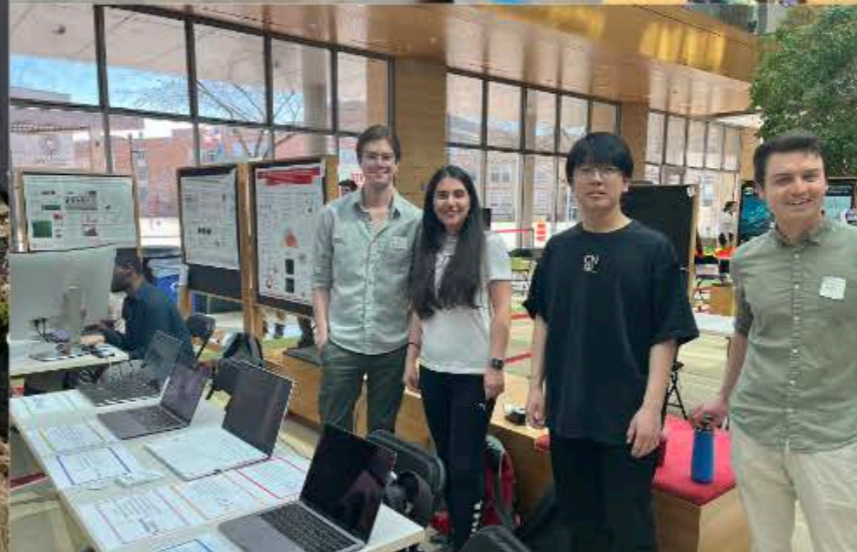
(Solis-Lemus & Ane, 2016; Solis-Lemus. et al, 2017)



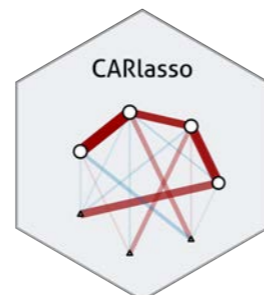
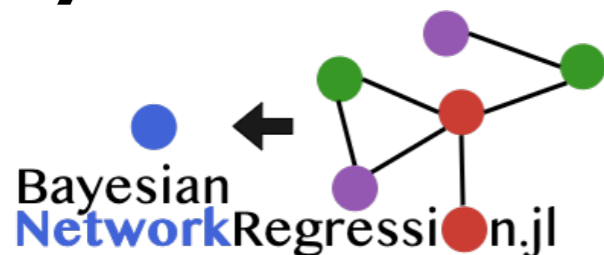
Solis-Lemus lab



WISCONSIN
UNIVERSITY OF WISCONSIN-MADISON



Thank you!



<https://solislemuslab.github.io/>



mstdn.social/@solislemuslab



[solislemuslab](https://github.com/solislemuslab)



[@thestatistician](https://www.instagram.com/thestatistician)

Questions?